# Developing drag models for non-spherical particles through machine learning

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#### **Motivation: coal and biomass gasification**

- Thermal conversion systems are very challenging to model:
  - Particles have complex shapes, a broad range of sizes, shapes and density.
  - Non-spherical particle interact with other particles.
  - Force closures are needed for non-spherical particles, i.e. drag and lift (maybe even other unsteady forces such as added mass and history force)







# Drag Coefficient on Single Spherical and Non-Spherical Particle

Different drag correlations proposed by different groups based on the Reynolds number and sphericity ( $\Phi$ ) projected to different directions.



Sphere (Stokes flow):  $c_D = \frac{24}{Re}$ 

Non-spherical particle (Stokes flow):  $c_D = rac{8}{\mathrm{Re}} rac{1}{\sqrt{\Phi_\perp}} + rac{16}{\mathrm{Re}} rac{1}{\sqrt{\Phi}}$ D. Leith, Aerosol Sci. Tech. 6 (1987) 153 Non-spherical particle ( $Re < 10^5$ ):  $rac{c_{
m d}}{K_2} = rac{24}{{
m ReK_1}\,K_2} \Big(1 + 0.1118 ({
m ReK_1}K_2)^{0.0567} \Big)$ 0.4305 $+\frac{1}{1+\frac{3305}{\text{ReK}_{4}K_{2}}}$  $K_2 = 10^{1.8148(-\log\phi)^{0.5743}}$  (Newton factor) G. H. Ganser, Powder Technol. 77 (1993) 143

Non-spherical particle (
$$Re < 10^5$$
):  
 $c_D = \frac{8}{\text{Re}} \frac{1}{\sqrt{\Phi_{\parallel}}} + \frac{16}{\text{Re}} \frac{1}{\sqrt{\Phi}} + \frac{3}{\sqrt{\text{Re}}} \frac{1}{\Phi^{\frac{3}{4}}} + 0.4210^{0.4(-\log\Phi)^{0.2}} \frac{1}{\Phi_{\perp}}$   
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#### **Drag Coefficient on Packed Spherical Particle**



Wen & Yu (1966) for dilute suspensions and Ergun's equation (Ergun 1952) for denser systems are the earliest experimental efforts.

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Hill et al. (2001); Beetstra et al. (2007); Gidaspow (1986); Syamlal and O'Brien (1987);

Tenneti et al. (2011)

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#### **Drag Coefficient on Packed Non-spherical Particle**





Normalized mean drag force from current simulation compare to F&H, T&H and T&Z correlation.

L. He et al. / Powder Technology 313 (2017) 332-343

$$F(\phi, \mathrm{Re}_m) = rac{F_\mathrm{isol}\,(\mathrm{Re}_m)}{(1-\phi)^3} + F_\phi(\phi) + F_{\phi, Re_m}(\phi, \mathrm{Re}_m)$$

$$egin{aligned} F_{\phi}(\phi) &= rac{5.81 \phi}{(1-\phi)^3} + 0.48 rac{\phi^{-7/6}}{(1-\phi)^4} \ F_{\phi, ext{Re}_m}(\phi, ext{Re}_m) &= \phi^3 \, ext{Re}_m \Big( 0.95 + rac{0.61 \phi^3}{(1-\phi)^2} \Big). \end{aligned}$$

Re	Φ	IBM	F&H	% diff	T&H	% diff	T&Z	% diff
10	10%	3.58	2.78	-22.51%	3.65	1.99%	3.49	-2.72%
50		5.82	5.66	-2.80%	6.26	7.47%	5.92	1.67%
100		8.46	8.76	-3.58%	9.14	8.14%	8.29	- 1.96%
200		14.10	14.45	2.53%	14.60	3.61%	12.32	- 12.62%
10	20%	6.87	4.39	-35.10%	6.57	-4.34%	6.30	-8.37%
50		11.13	8.95	- 19.66%	10.43	-6.28%	9.88	-11.29%
100		15.81	13.66	- 13.57%	14.74	-6.75%	13.41	- 15.16%
200		24.97	22.02	- 11.78%	22.89	-8.30%	19.47	-22.01%
10	30%	13.14	7.46	- 43.18%	11.98	-8.81%	11.57	- 11.89%
50		20.20	15.38	- 23.83%	18.38	-9.02%	17.56	- 13.06%
100		27.58	23.29	- 15.56%	25.59	-7.21%	23.63	- 14.31%
200		42.82	36.77	- 14.11%	39.34	-8.13%	34.27	- 19.97%
10	35%	19.38	10.85	- 44.01%	16.41	- 15.32%	15.99	-17.46%
50		26.83	21.42	- 20.16%	25.02	-6.75%	24.20	-9.83%
100		36.59	34.39	- 6.01%	34.81	-4.86%	32.66	- 10.75%
200		57.76	60.34	4.46%	53.52	-7.34%	47.64	- 17.53%

$$c_D = rac{8}{ ext{Re}} rac{1}{\sqrt{\Phi_{\parallel}}} + rac{16}{ ext{Re}} rac{1}{\sqrt{\Phi}} + rac{3}{\sqrt{ ext{Re}}} rac{1}{\Phi^rac{3}{4}} + 0.4210^{0.4(-\log\Phi)^{0.2}} rac{1}{\Phi}$$

 $F_{isol}(Re_m)$  is the isolated drag model.

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#### Human Learning versus Machine Learning

#### **Human Learning**

Sphere (Stokes flow):  $c_D = \frac{24}{R_c}$ add non-spherical shape Non-spherical particle (Stokes flow):  $c_D = rac{8}{ ext{Re}} rac{1}{\sqrt{\Phi_\perp}} + rac{16}{ ext{Re}} rac{1}{\sqrt{\Phi}}$ D. Leith, Aerosol Sci. Tech. 6 (1987) 153 add large Re Non-spherical particle ( $Re < 10^5$ ):  $F_{\rm isol} \,({\rm Re}_m)$ add concentration  $F(\phi, \operatorname{Re}_m) = rac{F_{ ext{isol}}\left(\operatorname{Re}_m
ight)}{(1-\phi)^3} + F_{\phi}(\phi) + F_{\phi, Re_m}(\phi, \operatorname{Re}_m)$ **NI RESEARCH GROUP** 

**Machine Learning** 

$$F_{i} = \langle F_{i} \rangle (Re, \phi) + \Delta F_{i}(Re, \phi, \{r_{j=1}, \dots, r_{j=M}\}),$$
$$T_{i} = \Delta T_{i}(Re, \phi, \{r_{j=1}, \dots, r_{j=M}\}),$$
Seved-Ahmadi and Wachs (2020)

Neighbor configuration input features for ANN

 $[Re, \phi, x_1, y_1, z_1, x_2, y_2, z_2...x_n, y_n, z_n]$ 



He and Tafti 2019 Still spherical particles



#### **Problems**

#### Curse of dimensionality:

As the number of features or dimensions grows, the amount of data we need to generate grows exponentially.

1 neighbor	Input: $\mathbf{r}_j = (x_j, y_j, z_j)$	Output: $F_d$ , $c_d$	$D_1 = 3,  N_1 = 1000$
15 neighbor	Input: $15 \times 3 = 45$	Output: $F_d$ , $c_d$	$D_2 = 45, N_2 = N_1^{D_2/D_1} = 1000^{15}$
Table 1 Number of spherical part	ticles tested at each solid fraction.		
Number of particles (1	$\phi = 0.1$	191	Overfitting
	$\phi = 0.2$ $\phi = 0.3$	573	÷ € - ∧
	$\phi = 0.35$	669	ete
			ame

each particle are collected, to yield 21,780 data points. All forces are further normalized using the Stokes-Einstein relation:

The input is a vector containing 47 features (1 Reynolds number, 1 solid fraction, relative distance in(x,y,z) from the nearest 15 neighboring particles).



Input parameter



He and Tafti 2019

- Reduce the number of dimensions 1
- Increase the sample size 2.





#### Introduce our team and methodology



# Using Machine Learning for closure terms in multiphase flow modeling



For turbulent flow, the fluxes depend both on resolved variables like void fraction and vertical velocity and on variables describing the average state of the unresolved state.





# Using Machine Learning for closure terms in multiphase flow modeling



### Flow around a falling solid sphere





Solid motion is computed by solving the fluid equations for the whole domain, with the correct density in the solid and the fluid.

A solid body motion is imposed in the solid by correcting the velocity in an iterative manner.

Collision is accounted for by adding repulsion forces. Proximity is determined using index functions on the grid used for the solving the fluid equations.







The unsteady motion of 8 spheres in a periodic domain, viewed from above



The trajectories of the centroids of spheres in a periodic domain viewed from above. The circles denote the initial conditions. Trajectories leave and enter the domain





The Reynolds number of 8 solid spheres falling in a periodic domain versus time

The instantaneous drag coefficient of each sphere versus time, computed from the slip velocity and the acceleration of each sphere



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Domain Size: 2.0 x 2.0 x 2.0; Resolution: 180 x 180 x 180; Gravity: 0.6081; Fluid/solid density: 1.0 / 10.0 Fluid viscosity: 0.005 Number of Solid Spheres: 50 Diameter of Spheres: 0.30 Volume Fraction of Solids: 8.84%

The volume fraction is high, so the spheres collide frequently



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The spheres and the fluid velocity in one plane

The vorticity around the spheres, visualized by the  $\lambda_2$ = -4.0 contour





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# Falling solid ellipsoids

Domain Size: 2.0 x 2.0 x 2.0; Resolution: 200 x 200 x 200; Gravity: 0.6081; Fluid/solid density: 1.0 / 10.0 Fluid viscosity: 0.005 Number of Solid Spheres: 50 Size of Ellipsoids: 0.32 x 0.16 x 0.16 Volume Fraction of Solids: 2.68%

Notice that the volume fraction is lower than for the spheres. Although many fall broadside on, not all do







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# Falling solid ellipsoids



The ellipsoids and the fluid velocity in one plane



The vorticity around the ellipsoids, visualized by the  $\lambda_2$ = -4.0 contour

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# **Non-spherical particles**



Formlabs Form2 3D printer

- Stereolithography technology
- $145 \times 145 \times 175$  mm build volume
- 25  $\mu m$  minimum layer thickness

#### Non-spherical particles also exist in nature



The aspect ratios from left to right are roughly 5, 3.5 and 1.5.



This is a 3D printed particle with supporting material. It has a 2.5 mm major diameter and 0.5 mm minor diameter.





### **Preliminary drop tower**



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The goals of preliminary setup:

- Automated experiment procedure
- Data acquisition system
- Post-processing algorithm

#### Control Parameters:

- Particle shape
- Particle size
- Particle material density
- Particle number density

	Test section dimension	Funnel volume	Total number of cameras rack
• •	0.25×0.25×3 m	350 ml	4

## Water channel



The goals of this setup:

- Use tracer and LED backlighting to obtain fluid phase data.
- Experimentally investigate pair particle interaction with controlled initial conditions.
- Experimentally investigate fluid flow within a free-falling anisotropic particle swarm.
  - Fluid phase is quiescent water
  - Anisotropic particle is rice





## **Preliminary experimental tests**

#### Water channel:

Left panel: 4 mm rice Right panel: 7.5 mm rice

Images taken at ~5cm below particle release location

Preliminary drop tower: Left panel: 4 mm rice Right panel: 7.5 mm rice

Images taken at ~1m below particle release location







### **2D particle tracking velocimetry**







#### Plan



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