



THE UNIVERSITY OF TEXAS AT EL PASO
COLLEGE OF ENGINEERING



A Guideline for the Assessment of Uniaxial Creep and Creep-Fatigue Data and Models

Calvin M. Stewart and Jack Chessa

NETL Kick-Off Meeting

October 6, 2016

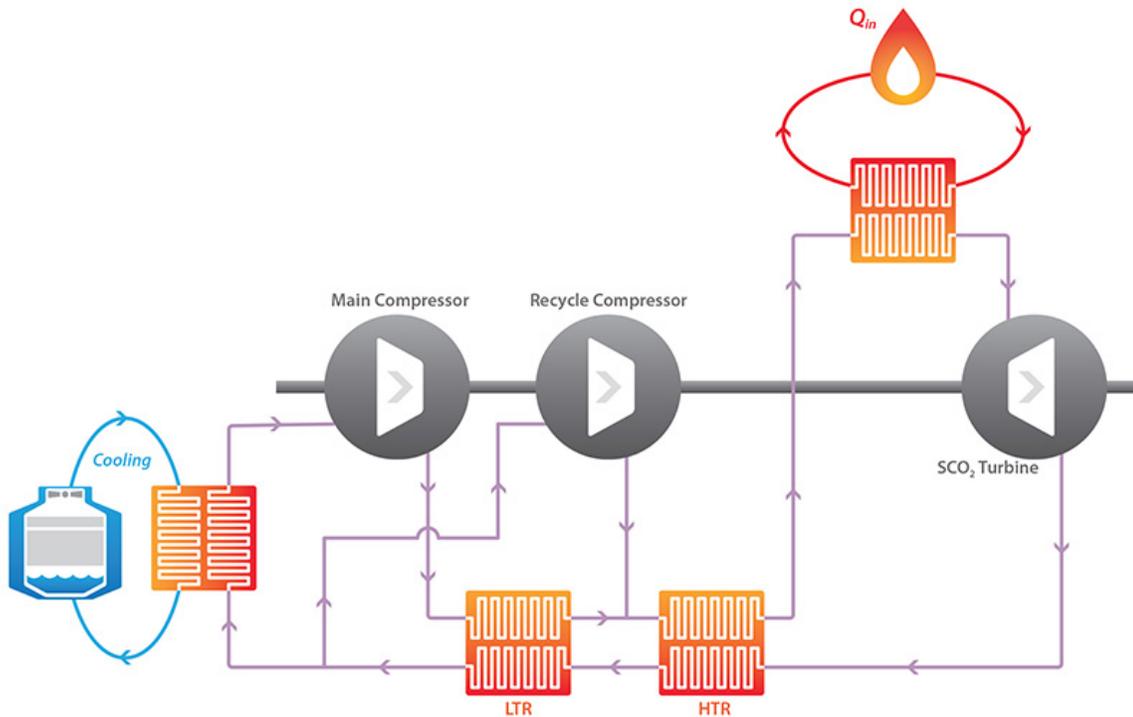


Outline

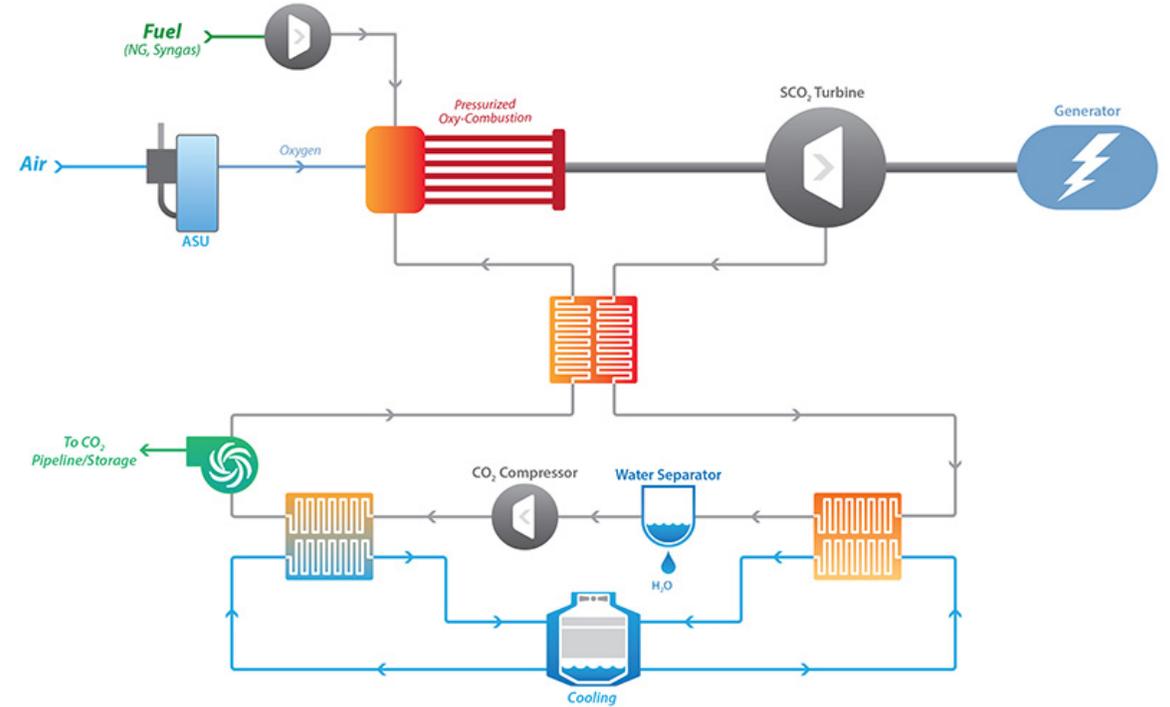
- Motivation
- Research Objectives
- Team
- Systematic Approach to Assessment
 - Task 2: Locate, Digitize, Sort, Store Experimental Data
 - Task 3: Uncertainty and Integrity of Experimental Database
 - Task 4: Mathematical Analysis and FEA of the Models
 - Task 5: Calibration & Validation – Fit, Interpolation, Extrapolation of the Models
 - Task 6: Post-Audit Validation of the Models
 - Task 7: Uncertainty Analysis of the Models
- Gantt Chart
- Milestones
- Questions

Motivation

- Recent drives to increase the efficiency of existing fossil energy (FE) power plants and the development of **Advanced Ultrasupercritical (A-USC) power plants**, have led to designs with steam pressures **above 4000 psi** and temperatures **exceeding 1400°F**.



Indirect-Fire Supercritical CO₂ Recompression Brayton Cycle



Oxy-Fueled Directly-Fired Supercritical CO₂ Cycle

Motivation

- The existing FE fleet has an **average age of 40 years**.
- The Department of Energy has outlined a strategy of life extension for US coal-fired power plants where many plants will operate for **up to 30 additional years of service**.

In Service Hours....

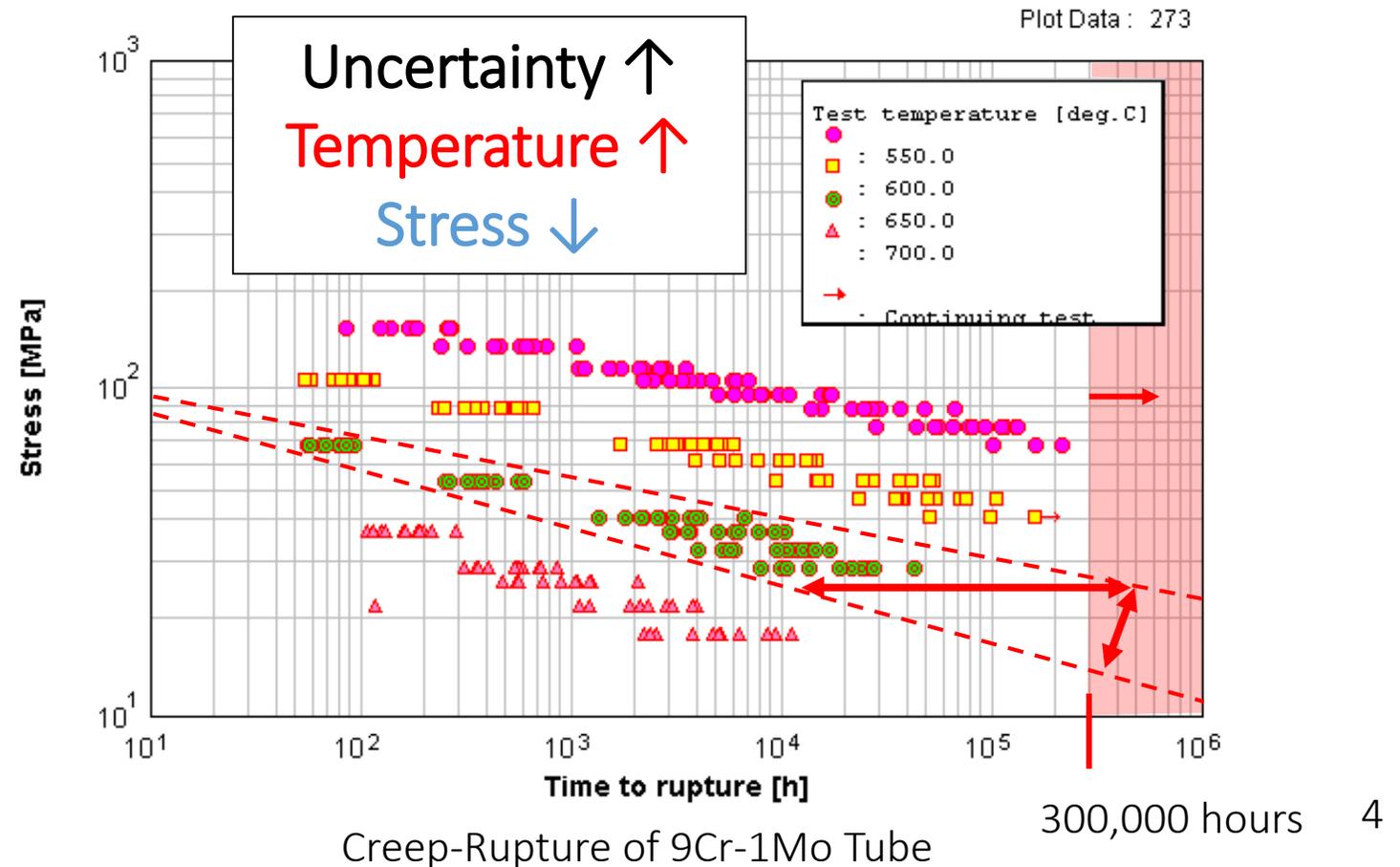
30 Years = 262,974 hours



40 Years = 350,634 hours

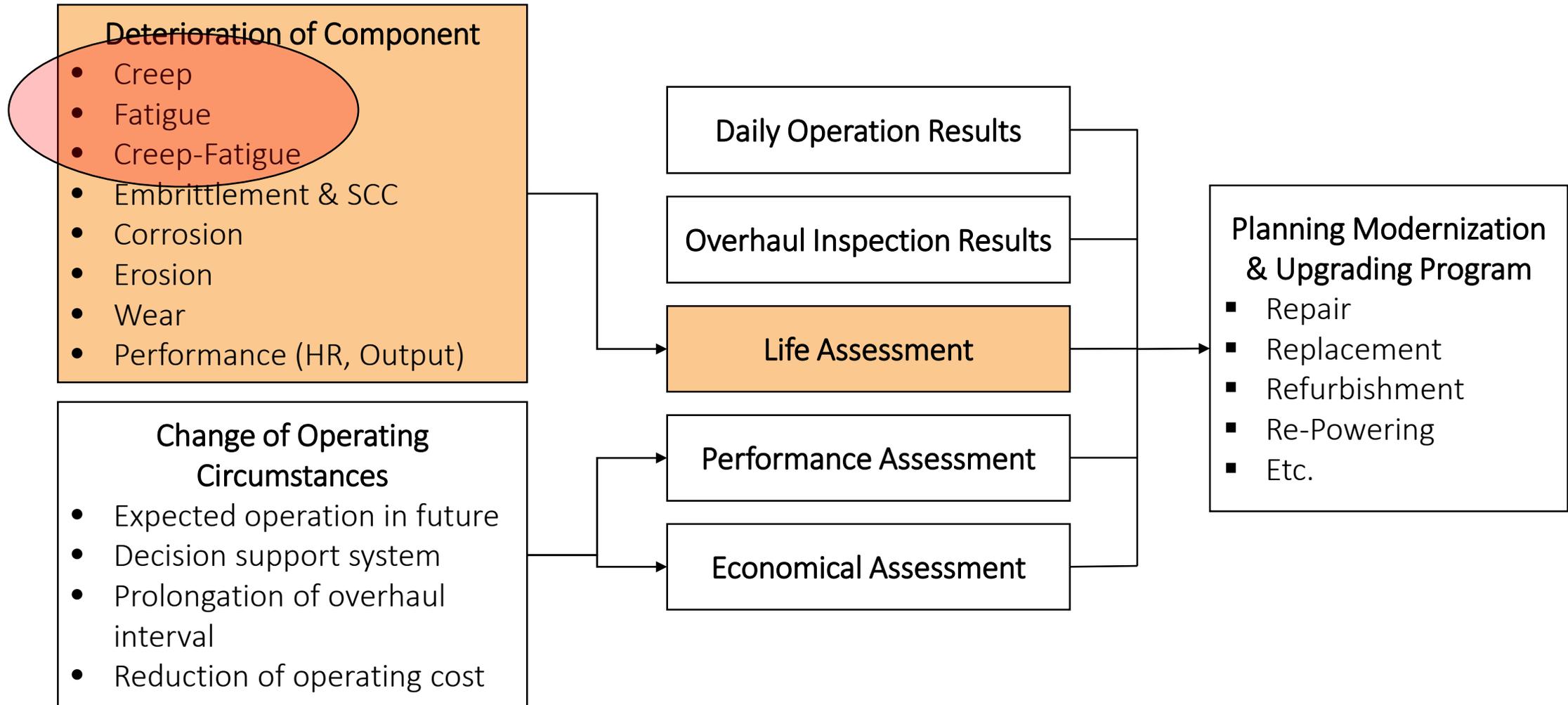


70 Years = 613,607 hours



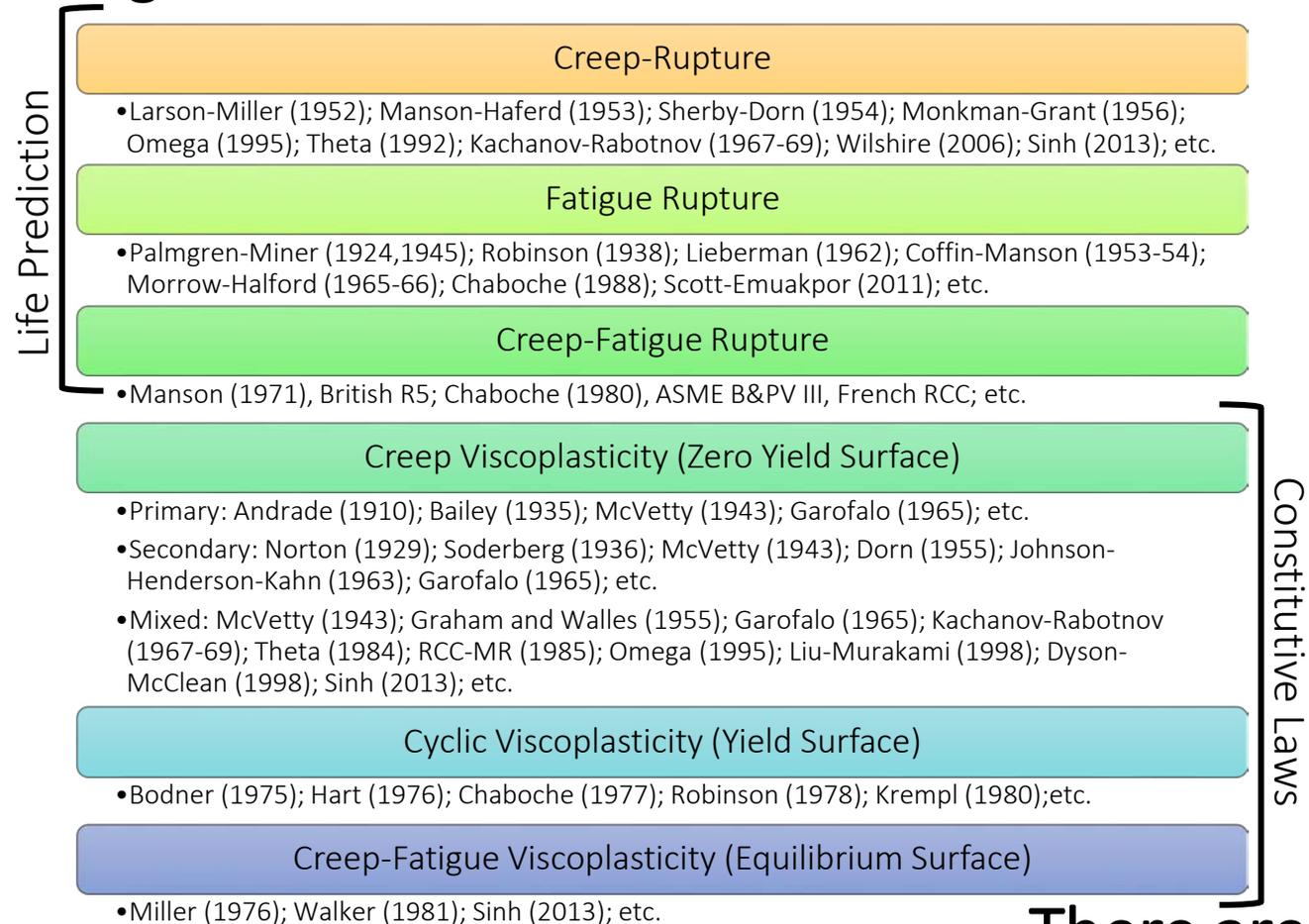
Plant Life Extension Program

- During Life Assessment, the integrity of components is assessed and the remaining service life estimated.



Motivation

- An immense number of models have been developed to predict the deformation, damage evolution, and rupture of structural alloys subjected to Creep and Creep-Fatigue.



There are Many More!...

Research Objectives

- Of primary concern to FE practitioners is a determination of which constitutive models are the “best”, capable of reproducing the mechanisms expected in an intended design accurately; as well as what experimental datasets are proper or “best” to use for fitting the constitutive parameters needed for the model(s) of interest.

RO1

Development of Aggregated
Experimental Databases of
Creep and Creep-Fatigue
Data

RO2

Computational Validation
and Assessment of Creep
and Creep-Fatigue
Constitutive Models for
Standard and Non-Standard
Loading Conditions

Team



Dr. Stewart is an Assistant Professor in the Department of Mechanical Engineering at the University of Texas at El Paso. He directs the *Materials at Extremes Research Group (MERG)*. He has over 10 years of experience in the theoretical development and numerical implementation of constitutive models for creep, fatigue, oxidation, and creep-fatigue-oxidation interaction phenomenon.



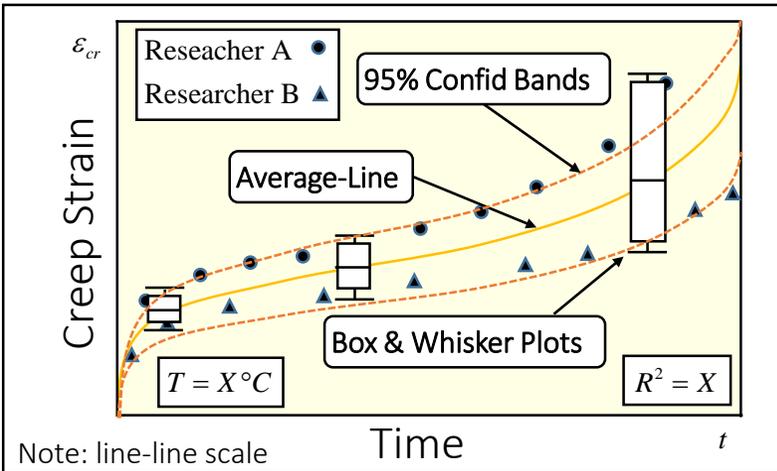
Dr. Jack Chessa is currently an Associate Professor of Mechanical Engineering at the University of Texas at El Paso. His research interest has been focused on the development of novel numerical methods for solving several challenging areas such as fracture mechanics, durability of high temperature ceramics as well as oxidation reactions of evolving interfaces.

Recent Work

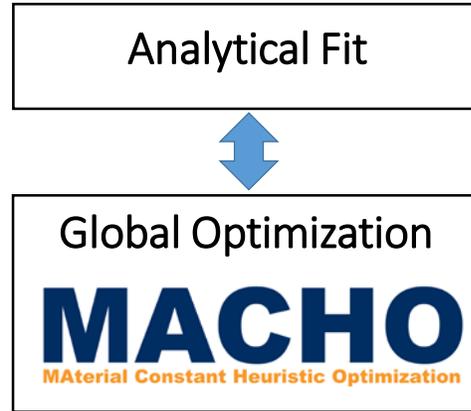
- Haque, M. S., and Stewart, C. M., 2016, “**Finite Element Analysis of Waspaloy Using Sinh Creep-Damage Constitutive Model under Triaxial Stress State**”, *ASME Journal of Pressure Vessel Technology*, **138**(3). doi: 10.1115/1.4032704
- Varela, L. A., and Stewart, C. M., 2016, “**Modeling the Creep of Hastelloy X and the Fatigue of 304 Stainless Steel using the Miller and Walker Unified Viscoplastic Constitutive Models**,” *Journal of Engineering Materials and Technology*, **138**(2). doi: 10.1115/1.4032319
- Haque, M. S., and Stewart, C. M., 2016, “**Exploiting Functional Relationships between MPC Omega, Theta, and Sinh-Hyperbolic Models**” *ASME PVP 2016*, PVP2016-63089, Vancouver, BC, Canada, July 17-21, 2016.
- Haque, M. S., and Stewart, C. M., 2016, “**Modeling the Creep Deformation, Damage, and Rupture of Hastelloy X using MPC Omega, Theta, and Sin-Hyperbolic Models**,” *ASME PVP 2016*, PVP2016-63029, Vancouver, BC, Canada, July 17-21, 2016.

Systematic Approach to Assessment

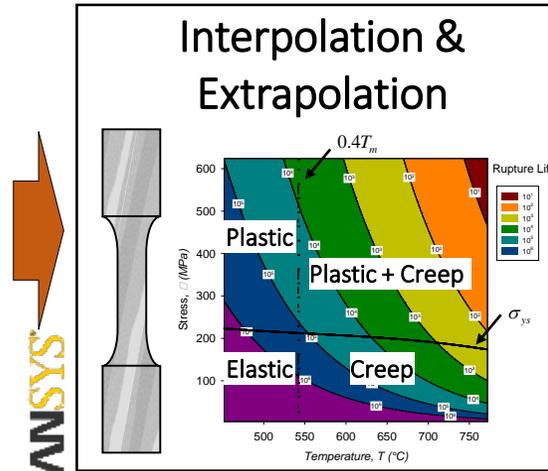
Example for Creep Deformation



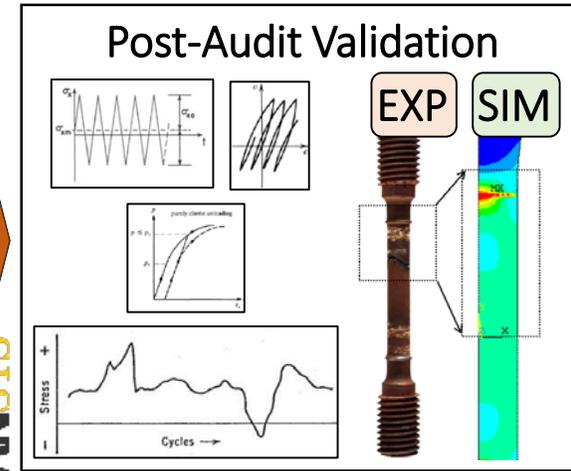
Aggregate Datasets with Uncertainty



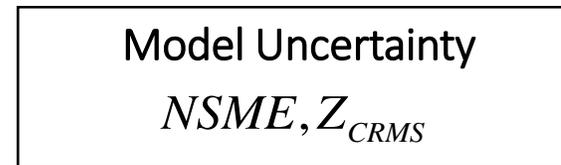
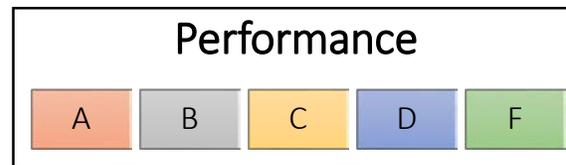
Model Fit to Datasets



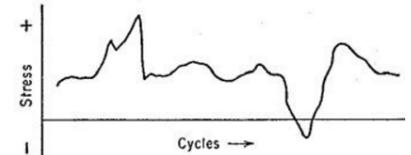
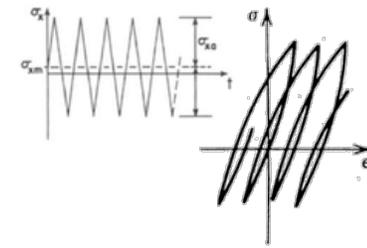
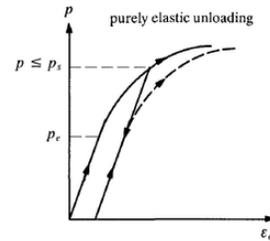
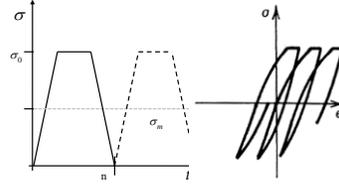
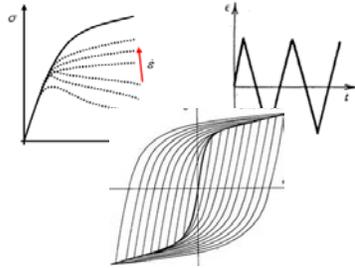
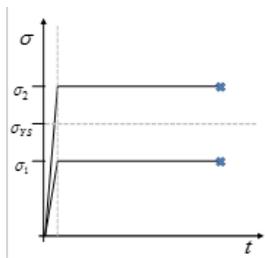
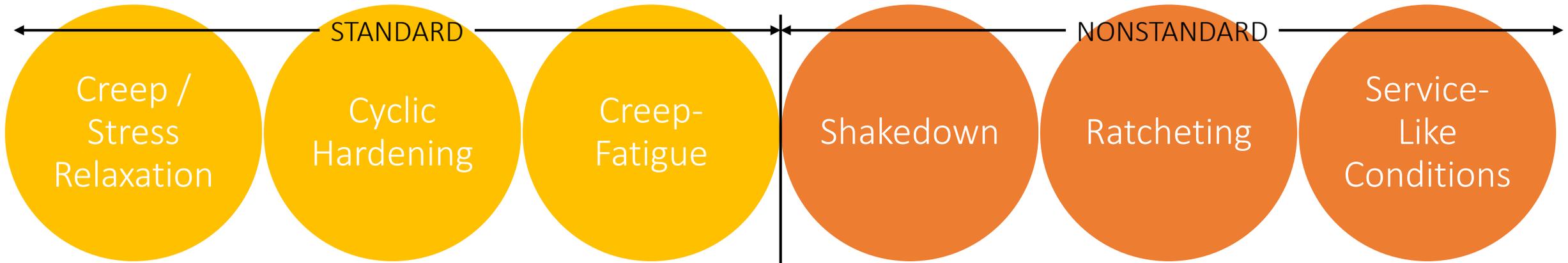
Standard Performance



NonStandard Performance



DEF: Standard and NonStandard



Data

High Availability

Models

Often Calibrated

Limited Availability

Rarely Calibrated

Systematic Approach to Assessment

Task 1: Maintain Project Management Plan

Task 2: Locate, Digitize, Sort, Store Experimental Data

Task 3: Uncertainty and Integrity of Experimental Database

Task 4: Mathematical Analysis and FEA of the Models

Task 5: Calibration & Validation – Fit, Interpolation, Extrapolation of the Models

Task 6: Post-Audit Validation of the Models

Task 7: Uncertainty Analysis of the Models

Locate, Digitize, Sort, and Store Data

Creep Data

Creep-rupture

Minimum creep strain rate

Time to creep strain

Creep deformation

Stress relaxation

Fatigue Data

Strain-Life

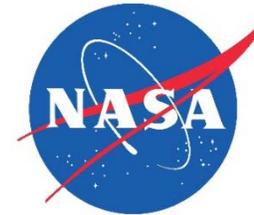
Cyclic Hysteresis loops

Stress Amplitude per Cycle

Creep-Fatigue Data

Tensile Hold Tests

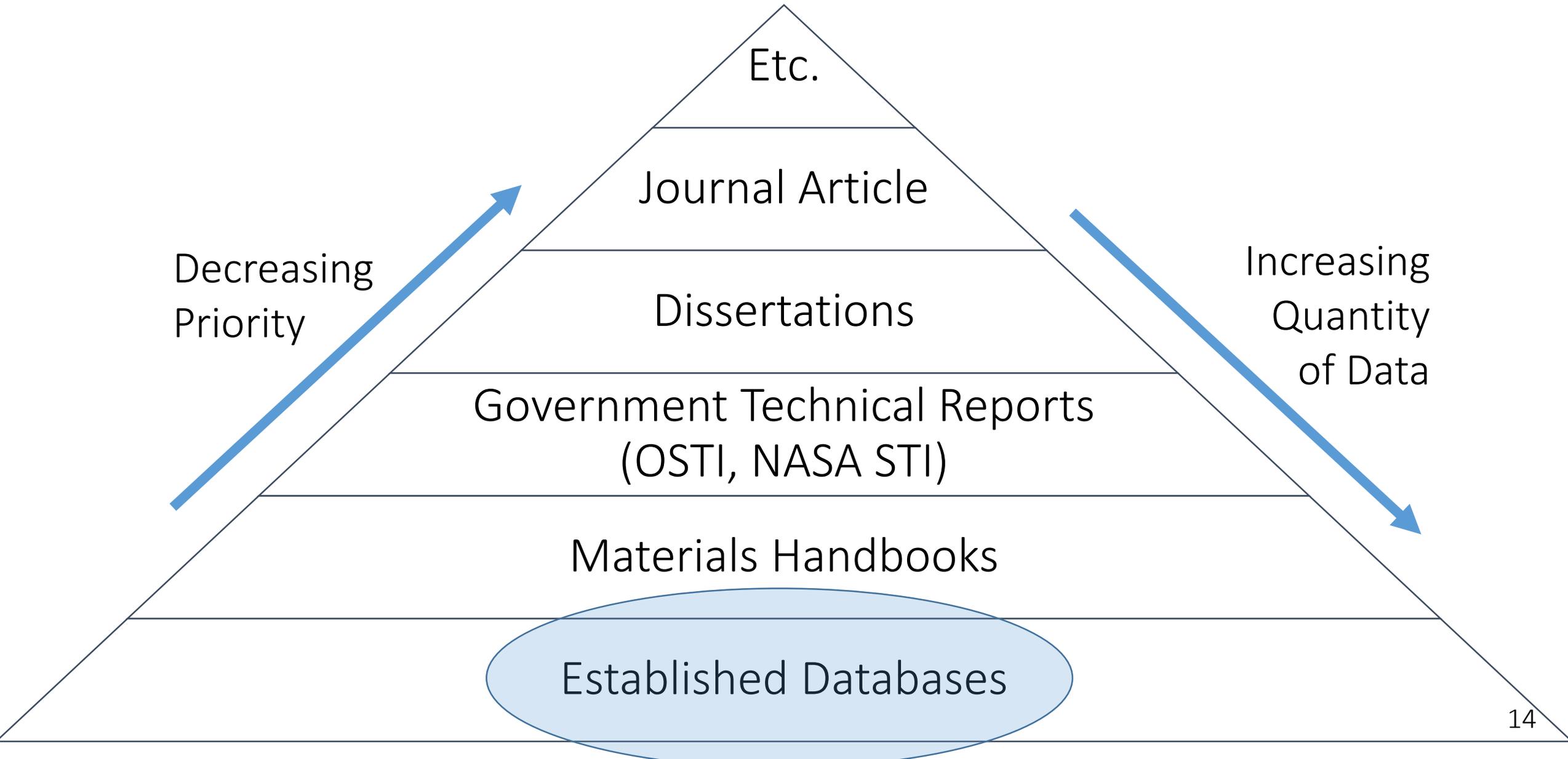
Established Data Sources



Need to Establish Connections



Locate, Digitize, Sort, and Store Data

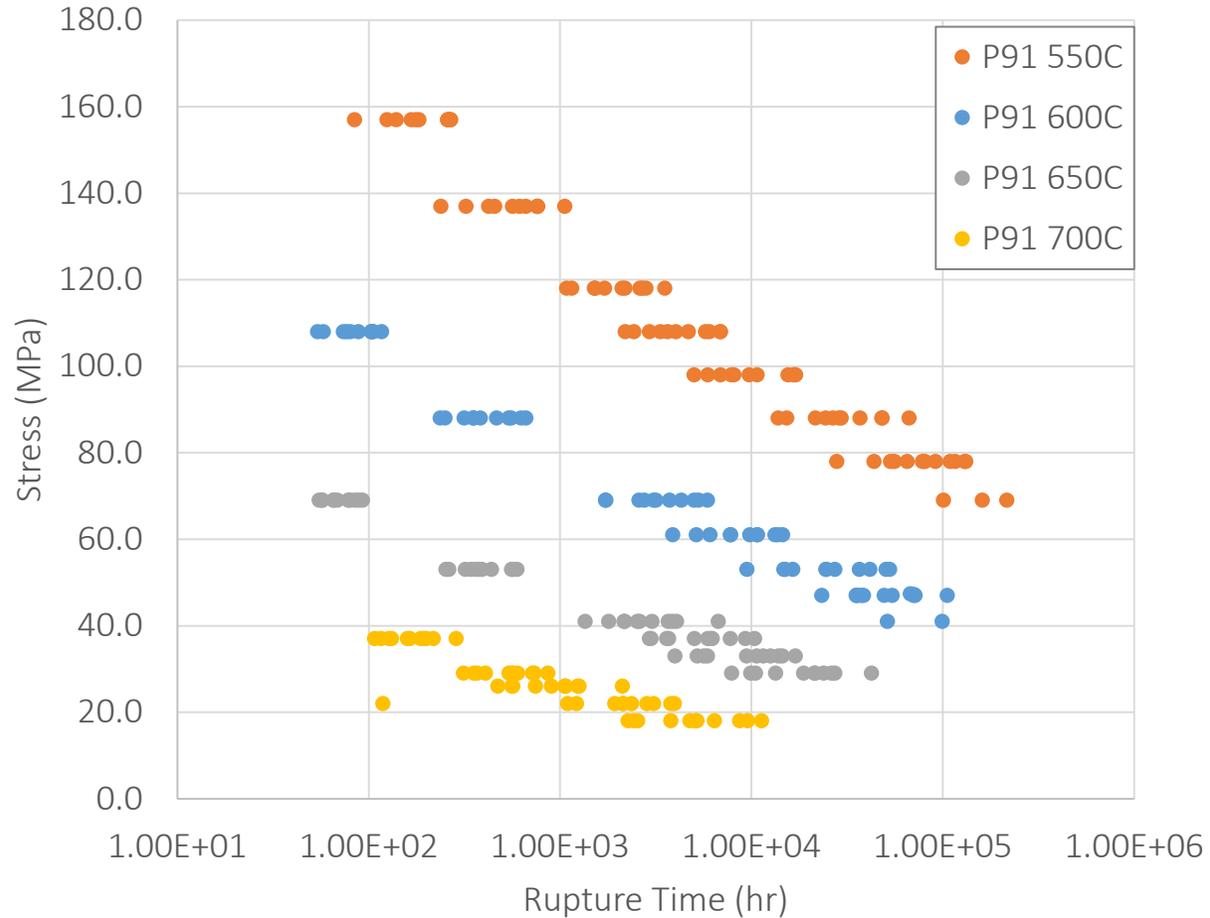


Current & High Priority Data Sources

Organization	Database(s)	Access	Available Metrics
National Institute of Materials Science (NIMS)	MatNavi	Granted	Material properties, monotonic, creep rupture
Materials and Processes Technical Information System (MAPTIS)	<ul style="list-style-type: none">• NASA Databases• ASM International Databases• Commercial Data	Granted	Material properties, monotonic, creep deformation & rupture, fatigue curves
Oak Ridge National Laboratory (ORNL)	Gen IV Materials Handbook	Pending	Material properties, monotonic, creep, statistical properties

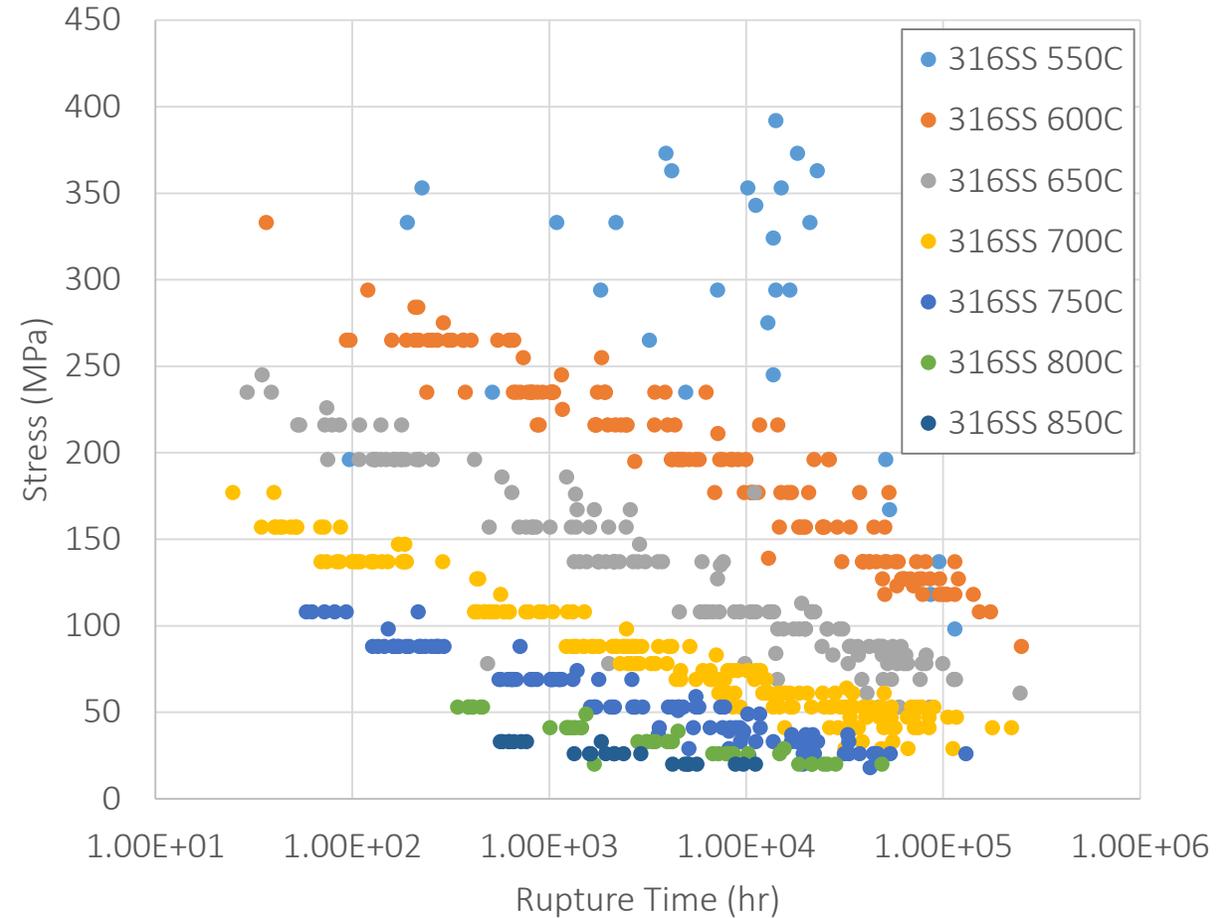
Creep Rupture Data (NIMS Database)

P91 Creep Rupture



Data points: 272

316SS Creep Rupture



Data points: 696

Locate, Digitize, Sort, and Store Data

- **MetaData** – A set of data that describes the characteristic of a dataset.
- MetaData can be used to identify **sources of uncertainty** in our data.



Locate, Digitize, Sort, and Store Data



```
<?xml version="1.0" encoding="US-ASCII"?>
```

```
<!-- Possible XML format for various test data -->
```

```
<database>
```

```
<!-- here is a possible creep test data. Go to http://xmlgrid.net/ to validate the data -->
```

```
<experiment material="inconel 718" country="USA" laboratory="ORNL" reference="the big creep database" type="creep deformation" name="stewart101">
```

```
<data name="chemical composition" format="ascii" dtype="float" units="hours" rank="1"> 52.50 1.00 19.00 3.05 17.00 0.35  
0.35 0.08 0.60 0.90 0.30 0.015 0.006 0.015 5.125</data>
```

```
<data name="time" format="ascii" dtype="float" units="hours" rank="1"> 0.0 1.0 2.0 3.0 4.0 5.0 </data>
```

```
<data name="strain" format="ascii" dtype="float" units="mm/mm" rank="1"> .000 .001 .002 .005 .010 .020 </data>
```

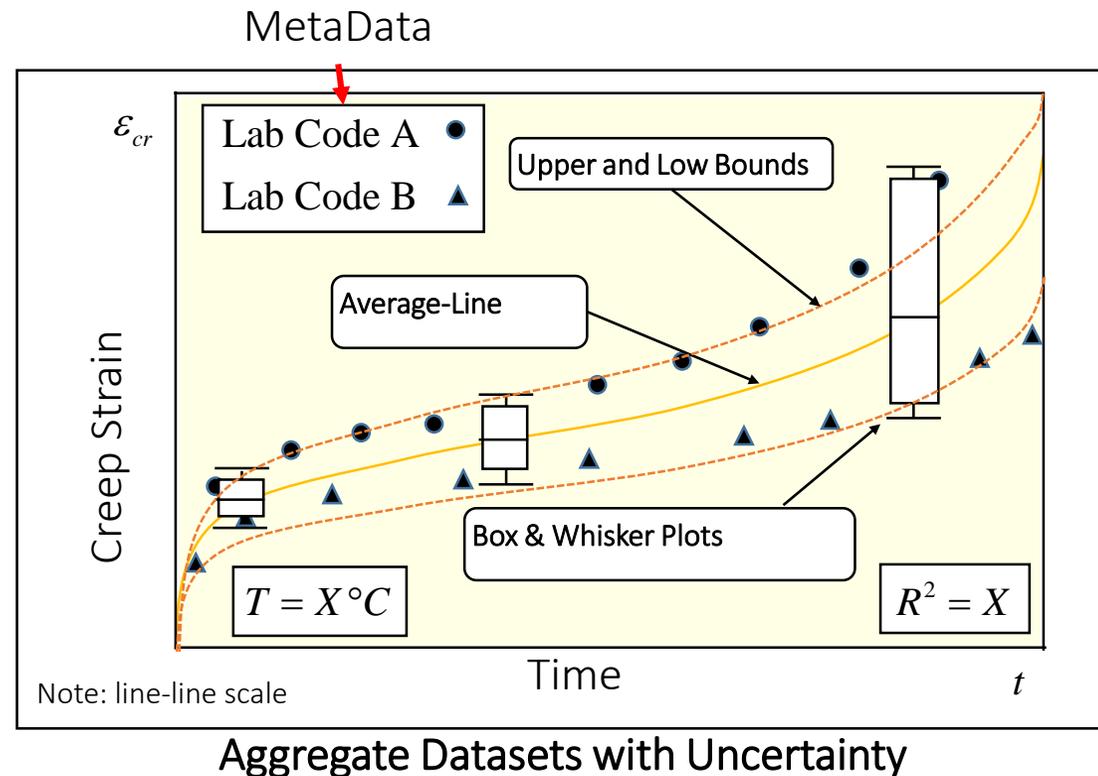
```
<data name="description" dtype="string"> "This is a basic creep test conducted by Dr. Calvin Stewart" </data>
```

```
<data name="stress" dtype="float" units="MPa" rank="0"> 2000.0 </data><data name="tbd"/></experiment>
```

```
</experiment></database>
```

Uncertainty and Integrity of Experimental Data

- Integrity Check
 - average line
 - upper and low bounds
 - standard deviations
 - coefficient of variation
 - box and whisker plots
 - factor of 2 bands
 - confidence intervals
 - coefficient of determination



- A parametric evaluation of the full database and individual datasets with regards to metadata will be performed to quantify the impact of experimental uncertainty on the material response.

Mathematical Analysis and FEA of the Models

Generate
Model
Database

Taxonomy of
Models

Material
Constant
Determination

Model Database

- Model Name (Year)
- Authors
- Primary Source
- Taxonomy
- Equations
 - Count
 - Functional form
- Material Constants
 - Count
 - Physical representation
 - Functional form

- Notes
 - Advantages
 - Disadvantages
 - Special remarks
- Analytical form of the Material Jacobian matrix (pseudo-Jacobian if necessary)

$$\mathbf{C}_{TOT} = \frac{\partial \sigma_i}{\partial \epsilon_j}$$

- USER MATerial (USERMAT) subroutine



Unification of Master Curve Models

$$P_{unified} = \frac{\log(t_r) - \alpha_0 - \alpha_3 T^r}{(T^r - \alpha_2^r)^q}$$

Model	Year	Parametric equation	Condition	Attribute
Larson-Miller	1952	$P_{LMP} = T(\log(t_r) + t_a)$	$r = -1, q = 1$ $\alpha_2 = \alpha_3 = 0$	Linear
Manson-Haferd	1953	$P_{MH} = \frac{\log(t_r) - \log(t_a)}{T - T_a}$	$r = q = 1,$ $\alpha_3 = 0$	Linear
Manson-Succop	1953	$P_{MS} = \log(t_r) - BT$	$r = 1, q = 0,$ $\alpha_0 = 0$	Linear
Orr-Sherby-Dorn	1954	$P_{OSD} = \log(t_r) - Q / RT$	$r = -1, q = 0$ $\alpha_0 = 0$	Linear
Goldhoff-Sherby	1968	$P_{GS} = \frac{\log(t_r) - \log(t_a)}{1/T - 1/T_a}$	$r = -1, q = 1$ $\alpha_3 = 0$	Linear
Modified Manson-Haferd	2016	$P_{MMH} = \frac{\log(t_r) - \log(t_a)}{T}$	$r = 1, q = 1,$ $\alpha_2 = \alpha_3 = 0$	Linear
Manson-Brown	1953	$P_{MB} = \frac{\log(t_r) - \log(t_a)}{(T - T_a)^n}$	$r = 1, \alpha_3 = 0$	Non-Linear
Graham-Walles	1955	$P_{GW} = \frac{\log(t_r)}{T - T_a}$	$r = q = 1,$ $\alpha_0 = \alpha_3 = 0$	Linear
Chitty-Duval	1963	$L_{CD} = T - m \log(tr)$	$r = q = 1$ $\alpha_0 = 0,$ $T = \alpha_2 - \alpha_3$	Linear
White le may	1978	$P_{WM} = \frac{1/T - 1/T_a}{\log(t_r) - \log(t_a)}$	Inverse of Goldhoff-Sherby	Linear
Mendelson-Roberts-Manson	1965	$P_{MRM} = \frac{\log(t_r) / \sigma^q - \log(t_a)}{(T - T_a)^n}$	Special Manson-Brown	Non-Linear

Name: Larson-Miller	Authors: Larson and Miller	Year: 1952
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Model Equations: $P_{LMP} = T(\log(t_r) + t_a)$	Attribute: <ul style="list-style-type: none"> • Creep-Rupture • Master curve • Time-Temperature Parameter • Linear iso-stress line
Number of constants: 2	

Constant terms, definition, unit:
 P_{LMP}, t_a : Larson-Miller parameter, Point of convergence respectively, both are unitless

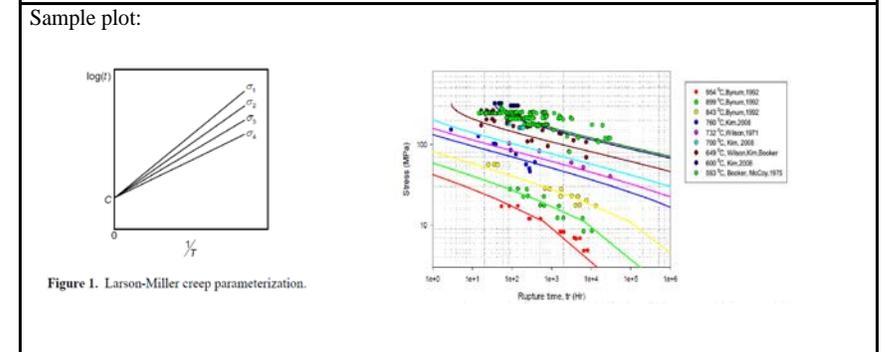


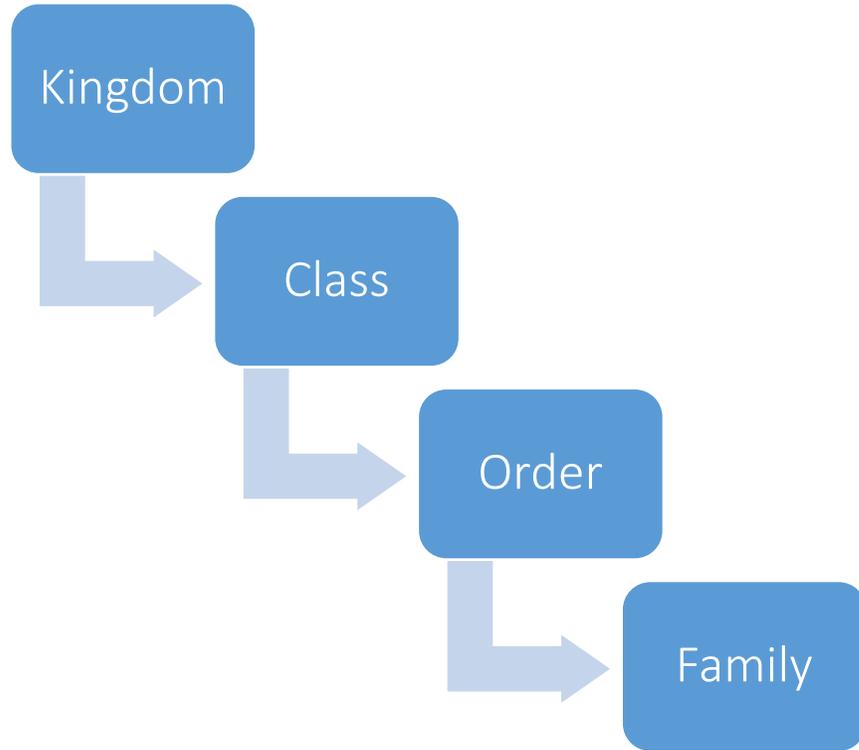
Figure 1. Larson-Miller creep parameterization.

Note: (advantages/limitations/special remarks)
 Linear iso-stress line.
 For wide range of data exhibits inflection point.

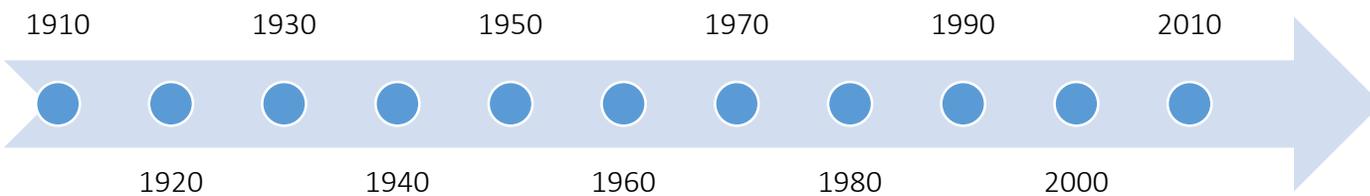
References:
 1. F.R. Larson, J. Miller Trans. ASME, 74 (1952), p. 765

Taxonomy of Models

Taxonomy



Development Timeline



KINGDOM: Phenomenological, Mechanistic, Multiscale

CLASS:

Deformation

ORDER

Minimum creep strain rate

FAMILY: Originating Model/Author

Primary creep

Secondary creep

Tertiary creep

Mixed

Creep Viscoplasticity

Viscoplasticity

Unified Viscoplasticity

Zero-Yield Unified Viscoplasticity

Damage & Rupture

ORDER

Classic damage mechanics / Ratios

Continuum damage mechanics

Microstructural damage mechanics

Combined

Material Constant Determination

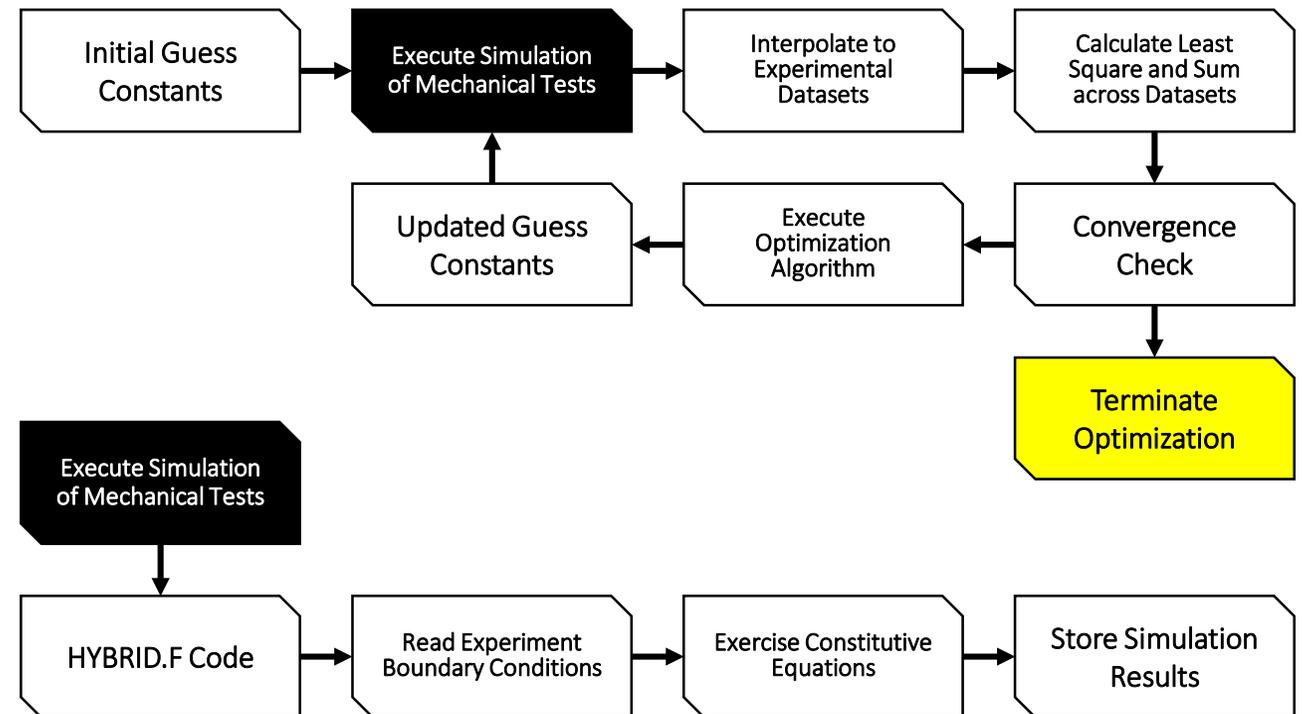
- Analytical Optimization for Simple Models
- Numerical Optimization for Complex Models (# of Matl Constants >> Variables)

MACHO

MAterial Constant Heuristic Optimization

Features

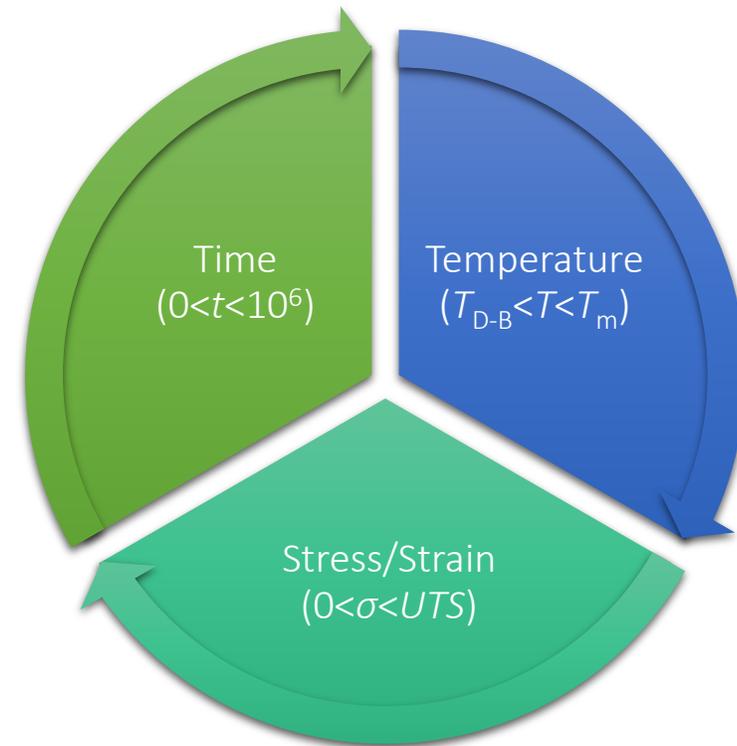
- Global Optimization Routine (uphill and downhill moves)
- Suitable for a high number of variables (tens of thousands)
- Internal FEM Code
- 64-bit, multi-core, multi-CPU
- scalable memory allocation



Calibration and Validation

- The calibrated models will be parametrically simulated across a full range of temperature, stress, and time to testing for **fit, interpolation, and extrapolation ability** of the models.
- Evaluate the credibility of **characteristic curves** produced by the models.
- Ideally, the best models will be able to predict **extreme conditions** and pass **physical realism requirements**

Parametrically explore the
Time-Temperature- σ/ϵ Map
and
Time-Temperature- $\Delta\sigma/\Delta\epsilon$ Map



Calibration and Validation

Extreme Conditions for Creep

Condition	Creep Rupture	Deformation
$\sigma < 0$	$t_r \approx \infty$	$\dot{\epsilon}_{cr} \approx 0$
$\sigma = 0$	$t_r = \infty$	$\dot{\epsilon}_{cr} = 0$
$0 < \sigma < UTS$	$t_r \propto f(\sigma, T)$	$\dot{\epsilon}_{cr} \propto f(\sigma, T)$
$\sigma = UTS$	$t_r \approx 0$	$\dot{\epsilon}_{cr} \gg 1$
$T \Rightarrow T_{D-to-B}$	$t_r \approx \infty$	$\dot{\epsilon}_{cr} \approx 0$
$0.3T_m < T < T_m$	$t_r \propto f(\sigma, T)$	$\dot{\epsilon}_{cr} \propto f(\sigma, T)$
T_m	$t_r = 0$	$\dot{\epsilon}_{cr} \gg 1$

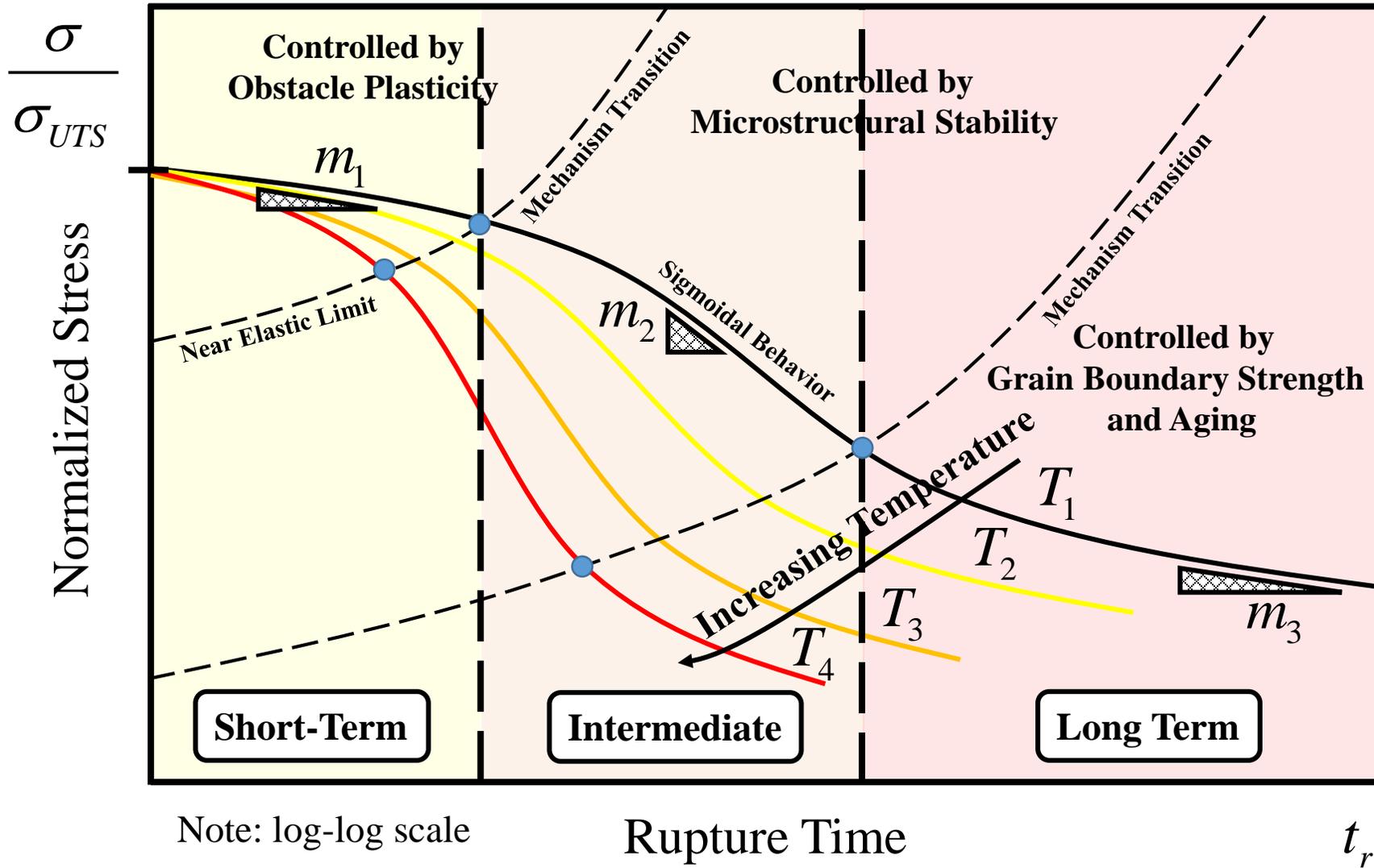
Note: σ is equivalent stress

Calibration and Validation

Physical Realism Requirements

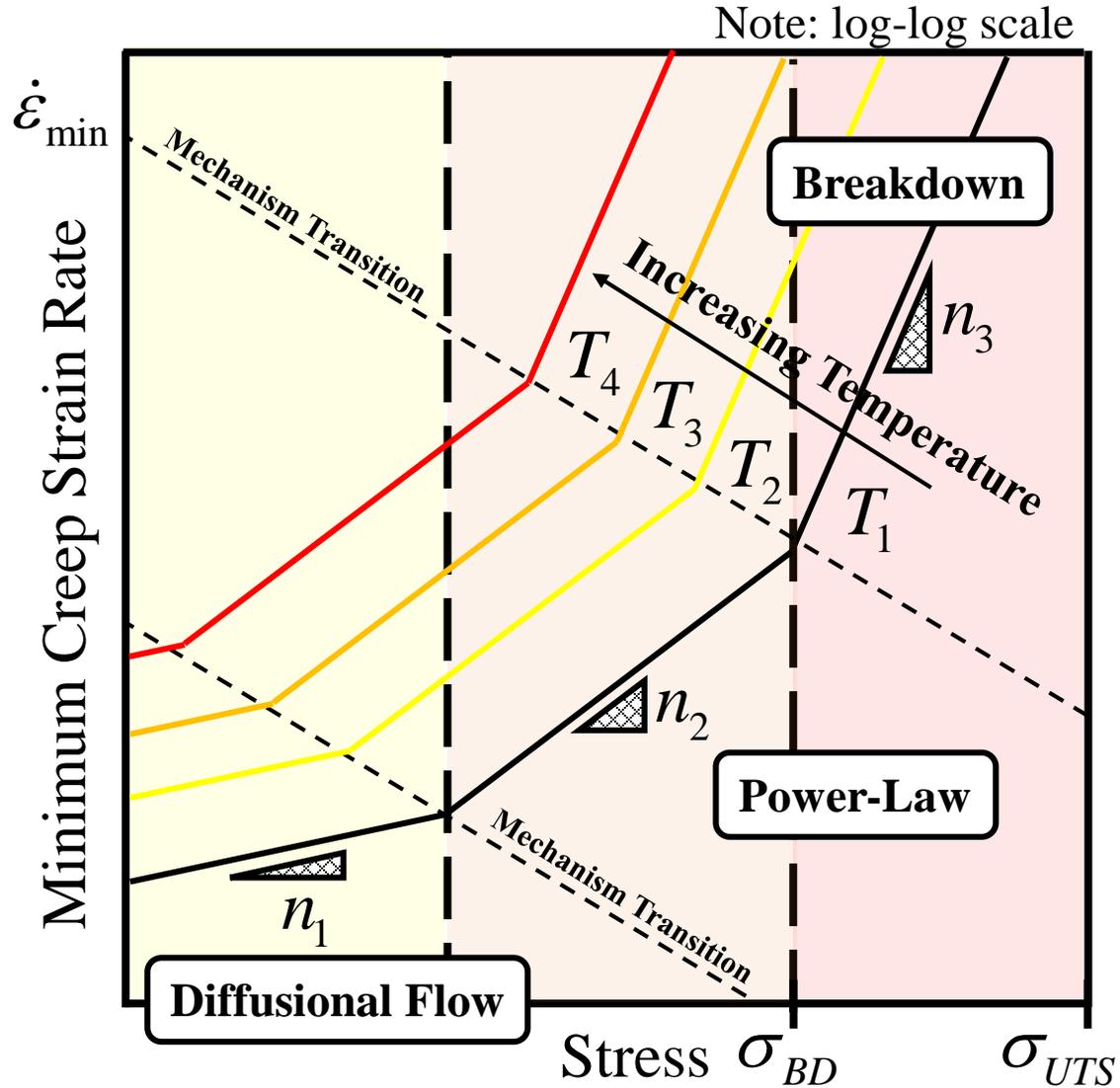
<i>Creep Rupture Requirements</i>	<i>Creep Deformation Requirements</i>
<ul style="list-style-type: none">• The isotherms do not cross-over, come-together, or turn back;• The extrapolated isotherms produce a sigmoidal behavior if a sigmoidal response is expected in material;• Both mechanism transition stresses decrease with temperature;• $T_{D-to-B} < T < 0.3T_m$, the isotherms for creep-rupture are tightly bunched together;• $0.3T_m < T < T_m$, the isotherms become more dispersed.	<ul style="list-style-type: none">• Minimum creep strain rate isotherms<ul style="list-style-type: none">○ do not cross-over, come-together, or turn back;○ transitions from power-law creep to breakdown;• Creep deformation<ul style="list-style-type: none">○ grows with σ and T; isostress lines do not cross-over, come-together, or turn back;○ regime dominance (primary at low stress and temperature, secondary at intermediate stress and temperature, tertiary at high stress and temperature) depends σ and T;○ Increasing σ and T coincidences with increased rupture strain as the creep deformation mechanisms change.

Calibration and Validation



$$\sigma \Rightarrow \sigma_{UTS} \quad t_r \Rightarrow 0 \quad m_3 \Rightarrow 0 \quad \sigma \Rightarrow 0 \quad t_r \Rightarrow \infty$$

Calibration and Validation

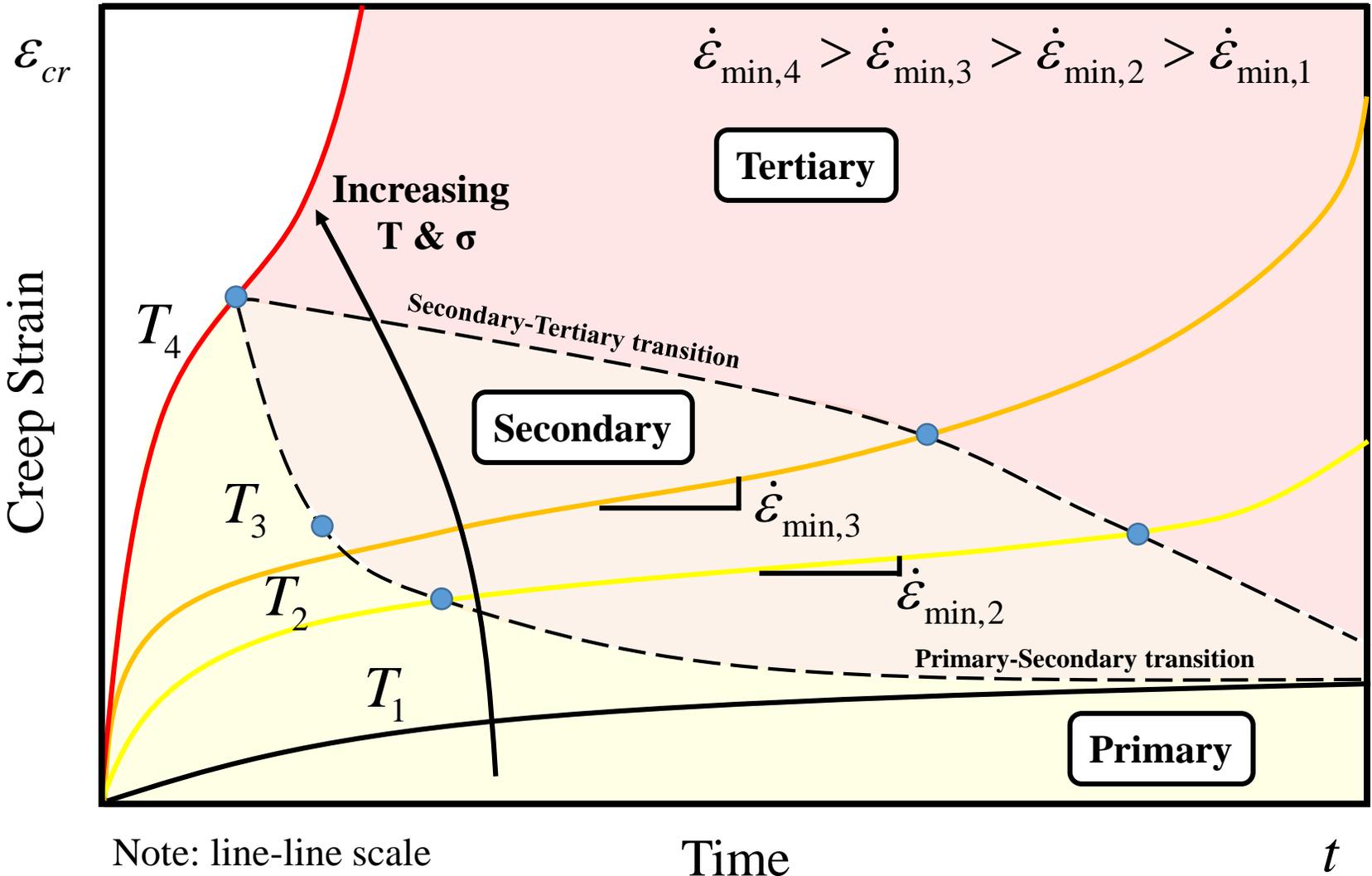


Diffusional Flow / Harper Dorn
Controversy

Kassner, Kumar, and Blum 2007

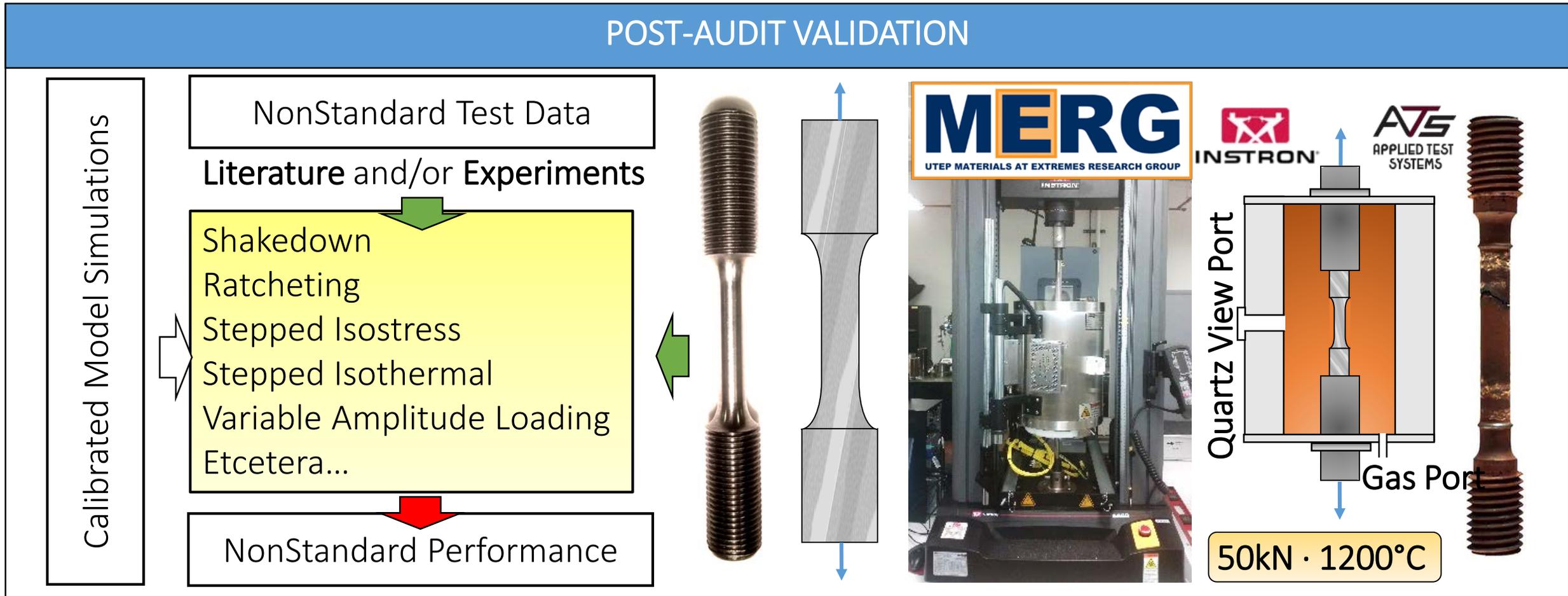
Blum and Maier 1999

Calibration and Validation



Post-Audit Validation

- Post-audit validation will provide insight into the ability of the constitutive models to reproduce various **non-standard** test responses.



Experimental Capabilities



Team MERGe



100 kN



50 kN



50 kN



5 kN



200 N

-150 to
Gas Env.

Rm to
Gas Env.

BioReactor
Liquid/Gas

Challenger-Columbia Structures and Materials Research Facility

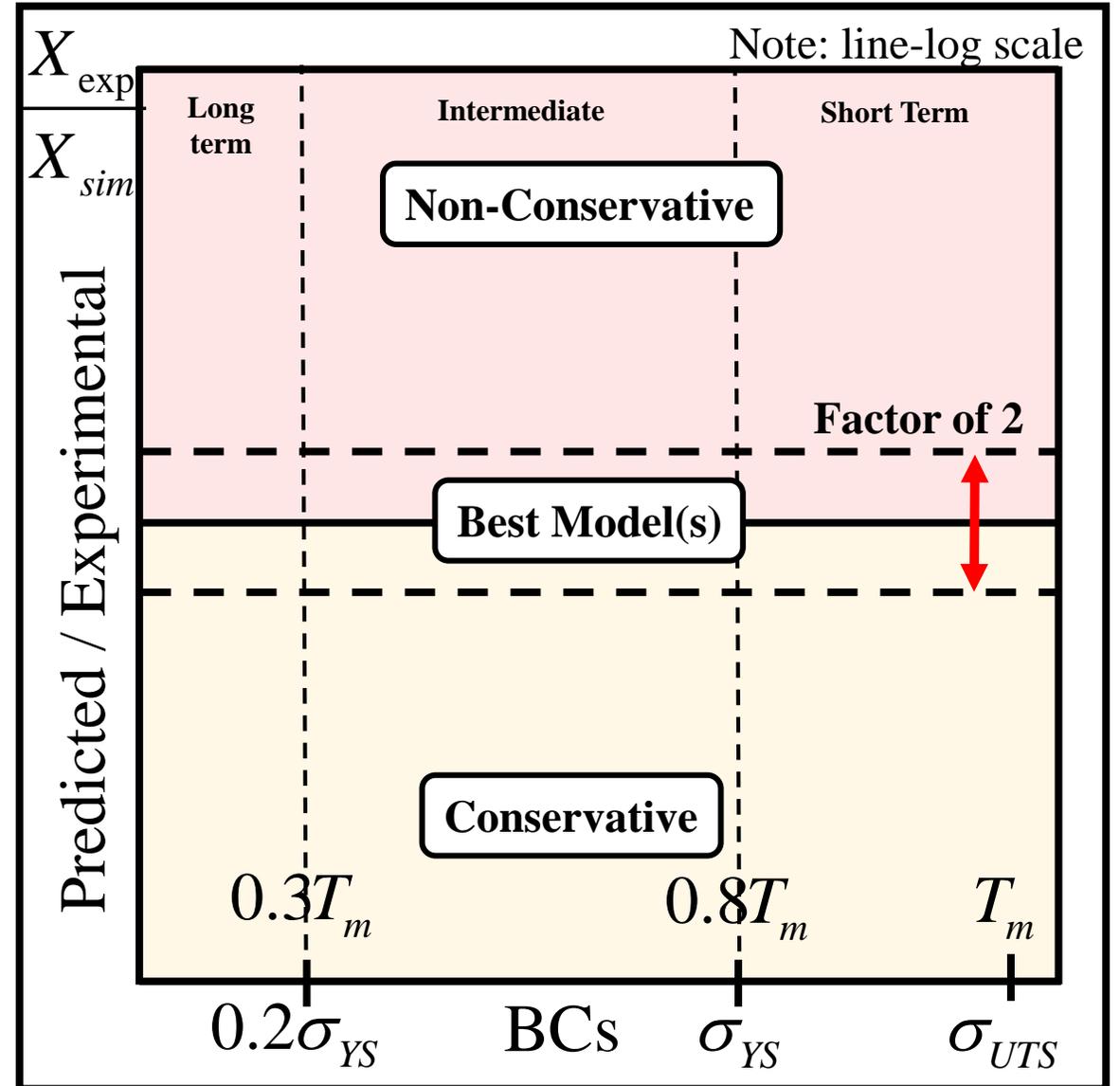
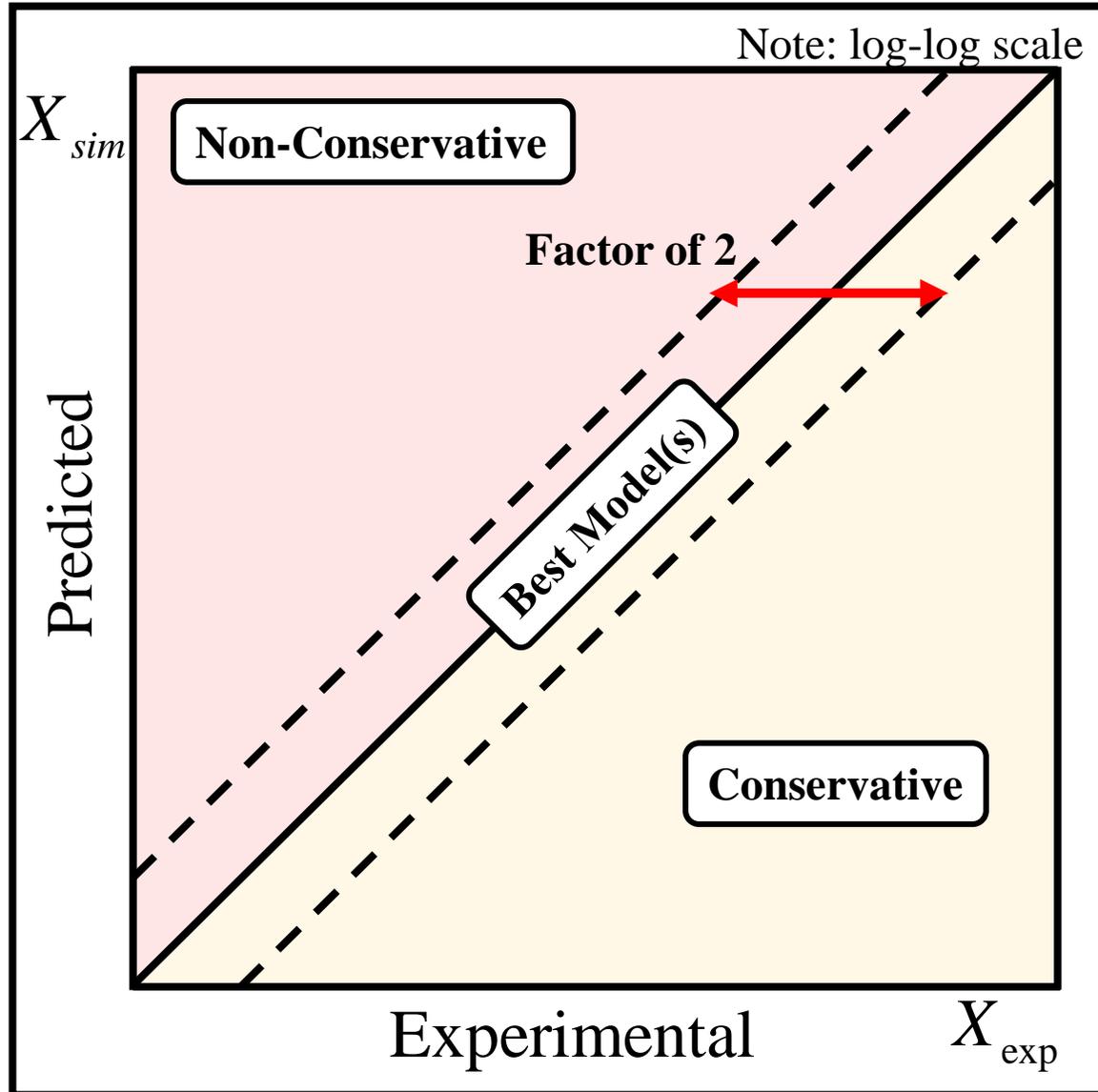
This 5,500 ft² facility houses state of the art materials synthesis, processing, and testing equipment for developing advanced materials research for next generation energy and aerospace systems. Dr. Stewart's Materials at Extreme Research Group (MERGe) is housed in this facility and he maintains the equipment above.



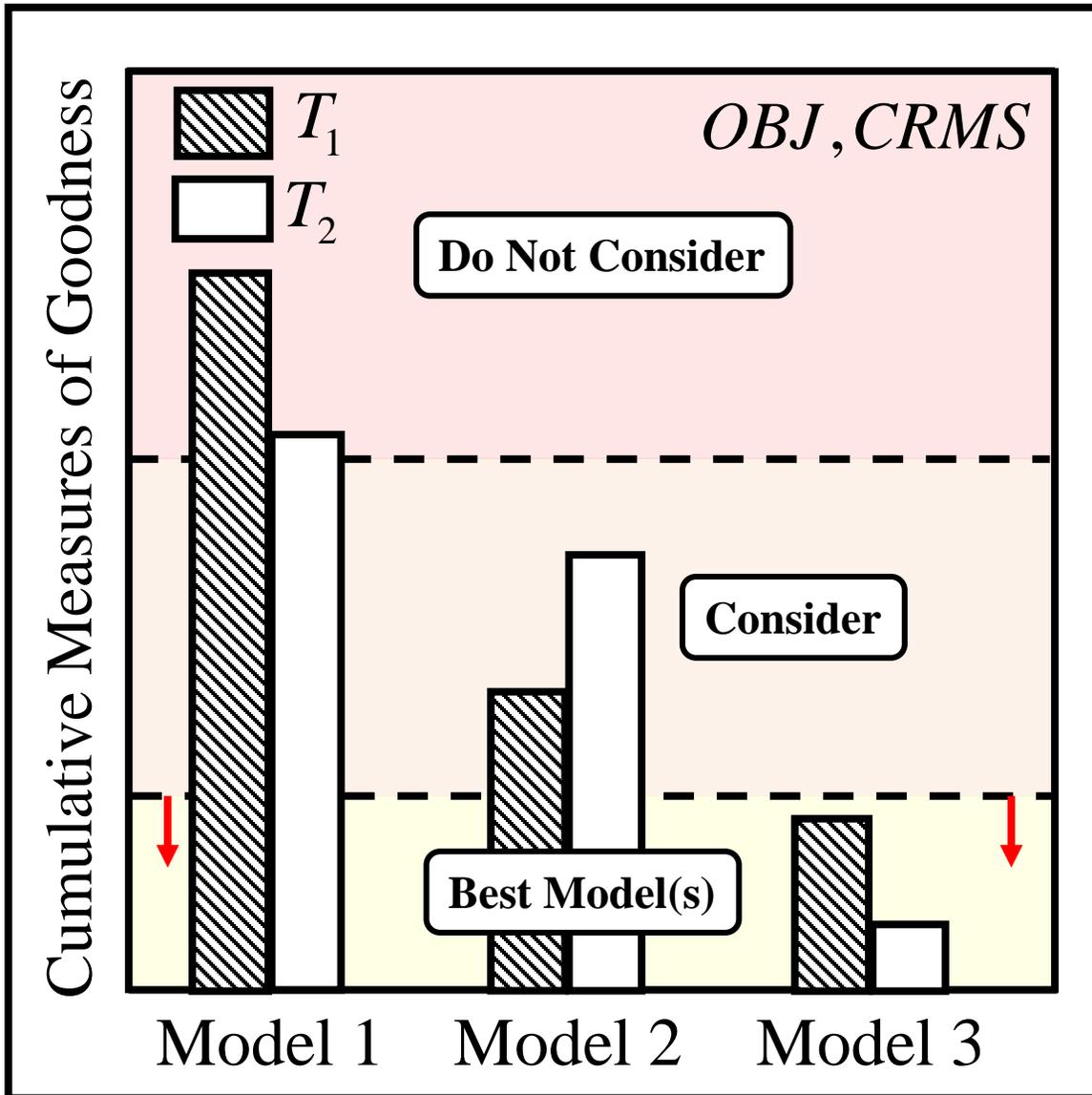
Uncertainty Analysis of the Models

- The model performance will be evaluated with respect to experiment uncertainty.
- The repeatability and stability of extrapolations using the models will be tested across boundary conditions regimes (short term creep, long term creep, low cycle fatigue, high cycle low frequency fatigue, creep-fatigue interaction, etc.) and when the database is culled by 50% overall and 10% in the long term creep and creep-fatigue interaction regime.
- By breaking the data and model performance into categories and executing this uncertainty matrix, the bias in the experimental data can be separated from model performance.

Uncertainty Analysis of the Models



Uncertainty Analysis of the Models



Creep Deformation / Hysteresis Loops

$$NMSE = \frac{1}{n} \sum_{i=1}^n \left[\frac{(X_{sim,i} - X_i)}{X_{max}} \right]^2, \quad OBJ = \sum_i NMSE_i;$$

Rupture and/or Cycles to Failure

$$Z_{CRMS} = 10^{2.5CRMS}, \quad CRMS = \sqrt{\frac{\sum [\log(t_r) - \log(t_{r,sim})]^2}{n-1}};$$

Final Assessment

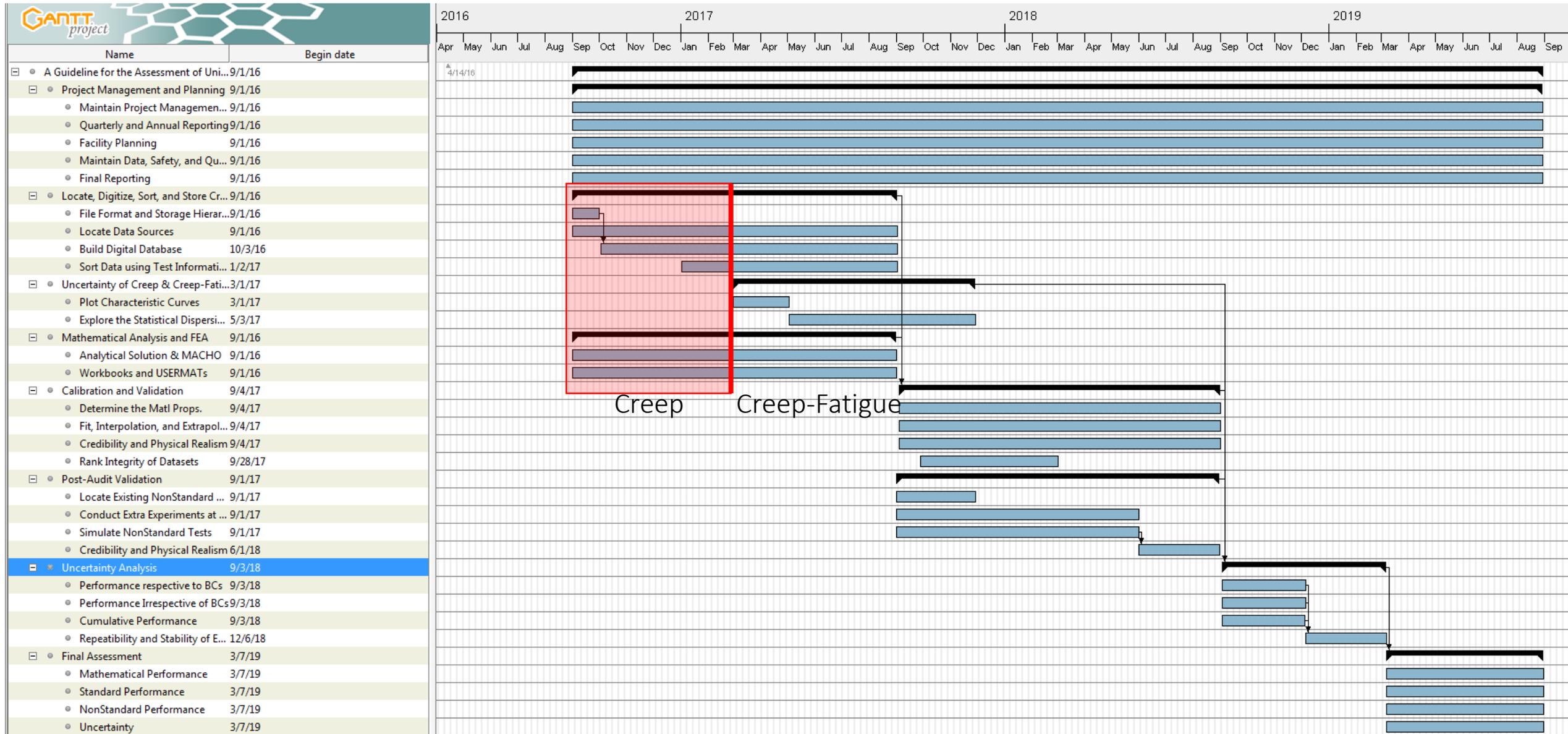
- The results of the mathematical/FEA, standard, nonstandard, and uncertainty analysis will be used to assign performance letter grades (A, B, C, D, or F) to each model for each loading condition, phenomena, and regime of interest.

Primary Categories

Sub Category

Mathematical/FEA	A	B	C	D	F							
Standard Performance	A	B	C	D	F	→	Creep	A	B	C	D	F
NonStandard Performance	A	B	C	D	F		Fatigue	A	B	C	D	F
Physical Realism	A	B	C	D	F		Tensile Hold	A	B	C	D	F
Uncertainty	A	B	C	D	F							
Overall	A	B	C	D	F							

Gantt Chart



Milestones

Mile-stone	Title	Description	Success Metrics	Reporting	Qtr	Date	Done?
Phase 1							
M1	P91 and 316SS Database Compiled	An exhaustive database of high integrity data.	Sorted excel workbooks	Summarized in Quarterly Report	Y1-Q4	9/1/2017	NO
M2	Uncertainty Analysis of Databases	The databases are analyzed according to material and equipment/test related uncertainties	Separation of systematic and random variables	Summarize results in Quarterly Report	Y2-Q2	3/1/2018	NO
M3	Topical Report	“A Guideline for the Assessment of Creep and Creep-Fatigue Data”	Submission	Emailed to Program Manager	Y2-Q2	3/1/2018	NO
Phase 2							
M4	Mathematical Analysis Report	Document describing the mathematical form and material constant determination procedure of all models	Completed Document	Summarize results in Quarterly Report	Y1-Q4	9/1/2017	NO
M5	Calibration and Validation	Fit, Interpolation, and Extrapolation of Models	Material constants and characteristic creep curves	Summarize results in Quarterly Report	Y2-Q4	9/1/2018	NO
M6	Post-Audit Validation	Simulations and Experiments under complex loading conditions	Blind Simulations compared to the experimental data	Summarize results in Quarterly Report	Y2-Q4	9/1/2018	NO
M7	Model Uncertainty	Parametric exercise of models against creep data uncertainty	characteristic creep curves for different datasets	Summarize results in Quarterly Report	Y3-Q2	3/1/2019	NO
M8	Final Assessment	Letter Grade score of models for mathematical/FEA, calibration validation, and post-audit validation	A table listing the performance of each model under different boundary conditions and regimes of interest	Summarize results in Quarterly Report	Y3-Q4	9/1/2019	NO
M9	Topical Report	“A Guideline for the Assessment of Creep and Creep-Fatigue Models” & “Recommendations for Improved Creep-Fatigue Models”	Submission	Emailed to Program Manager	Y3-Q4	9/1/2019	NO
Outside Budget Periods							
M10	Final Report	Summary of experimentation, findings and data	Final	Report	Y4-Q1	12/31/2019	NO

In Preparation. The Next 6 months...

- ASME PVP 2017
 - Time-Stress Parameters in Continuum Damage Mechanics
 - A Guideline to Representative Stress Model Selection for Multiaxial Creep
 - Development of a Stepped Iso-Stress Method Accelerated Creep Test for Metallics
- Nuclear Material Design
 - Model Transformations of Theta Projection, MPC Omega, and Sin-Hyperbolic Creep Deformation, Damage, and Life Prediction Models
- ASME Journal of Pressure Vessel Technology (Special Issue)
 - A Review of Master Curve Models for Creep-Rupture

Questions?



Calvin M. Stewart

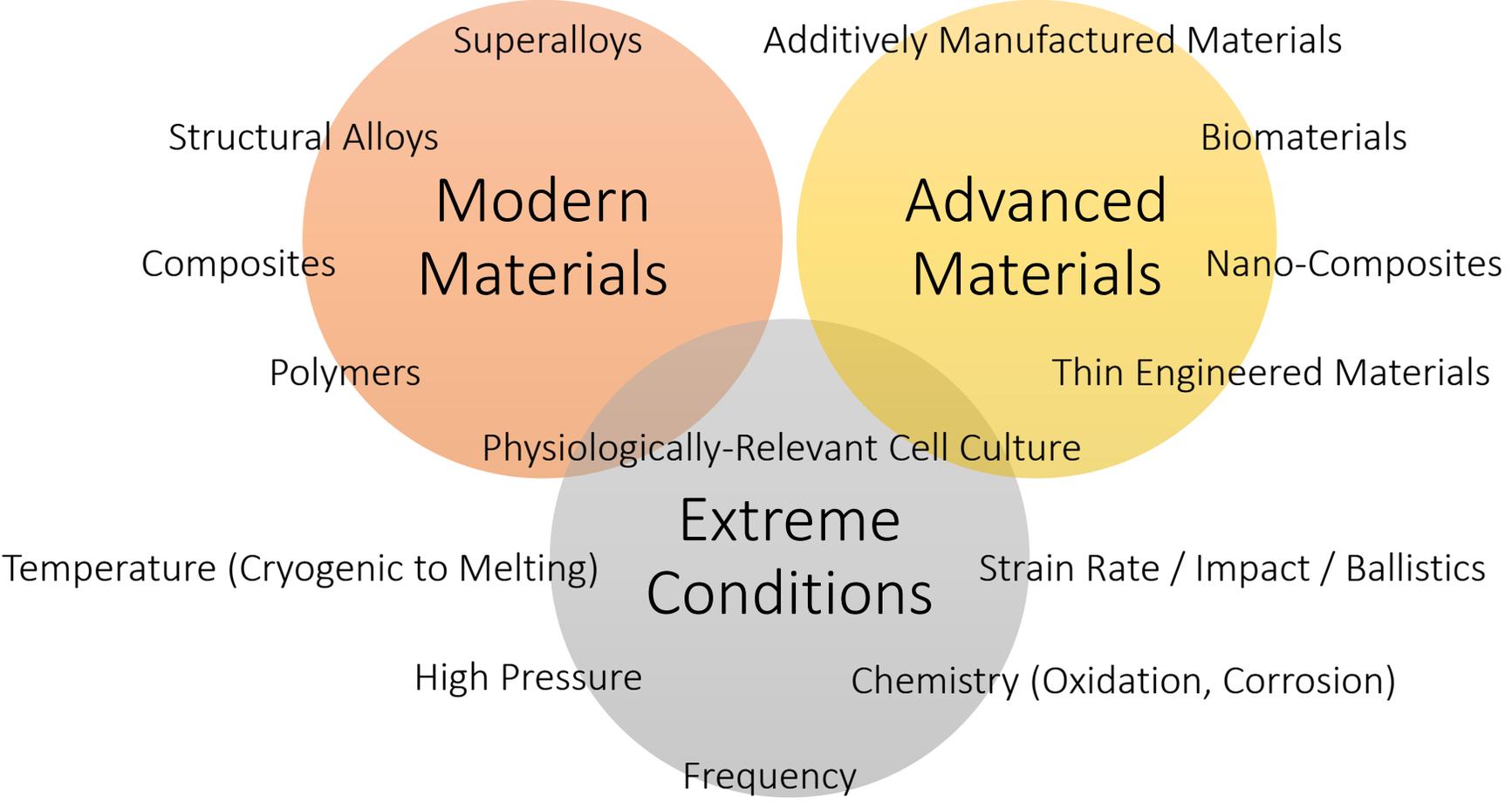
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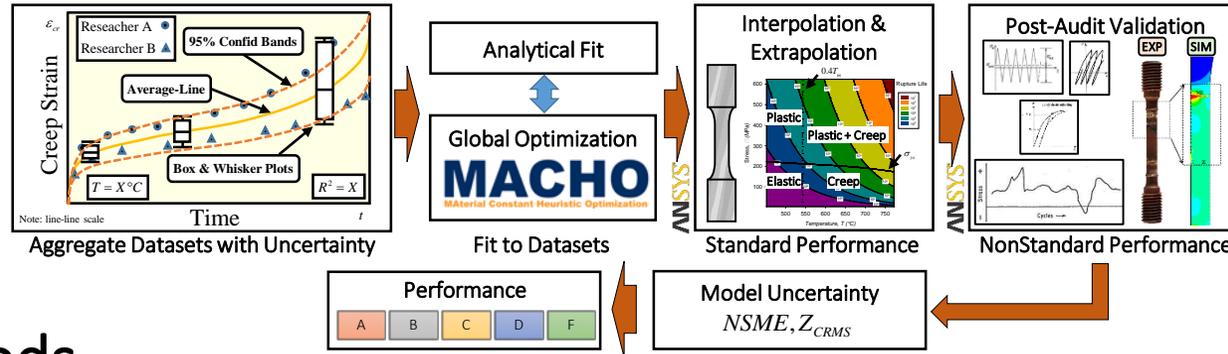




The goals of MERG are to:

- Expand the UTEP's capability to conduct **experimental research** that replicate the extreme boundary conditions experienced by modern and advanced materials.
- Develop **theoretical models** that capture the key phenomena (at appropriate time- and length-scales) that enable the prediction of constitutive response, damage evolution, and component life at a high fidelity.
- Design **numerical tools** to facilitate the rapid implementation of theory into academia, government, and industry.

From Materials to Models



Experimental Methods

- Subjecting small samples to mechanical test conditions bearing similarity to larger structures

Theory Development

- Applying of theories of elasticity, plasticity, viscoplasticity, etc.
- Developing constitutive models and life prediction equations from the experimentally observed behavior

Numerical Modeling

- Using appropriate continuum and/or non-continuum mechanics based numerical codes to simulate the materials response

Post-Audit Validation

- Evaluate the physical-realism of simulations through parametric simulations compared to blind experimental data.

Design

Outcomes

- Experimental Database of Standard and NonStandard Data
- Library of Validated Creep and Creep-Fatigue Models
- Topical Report – A guideline to the assessment of creep and creep-fatigue data
- Topical Report – A guideline to the assessment of creep and creep-fatigue models
- Final Report
- Conference papers
- Journal articles