

# Phase field modeling of microstructure and conductivity evolution in SOFC electrodes

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## Introduction

- Purpose of this research:**
- Simulate microstructure evolution and coarsening in SOFC electrodes;
  - Predict property evolution associated with electrode coarsening.
- Phase field model of SOFC electrodes:**
- Capable of simulating long term microstructure evolution [1].
  - Properties of electrode can be extracted directly from simulated microstructures.
  - Need wide range of tunability with respect to various interfacial energies in the electrodes.

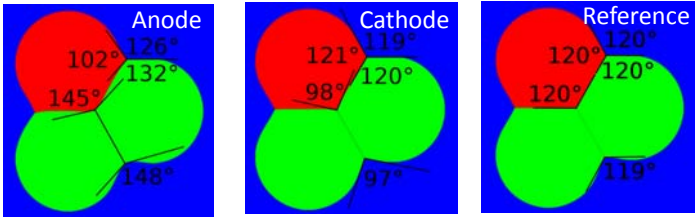
## Phase field modeling

- Phase-field parameters:
  - Phase fraction  $C_i$  (conserved)
  - Order parameter  $\eta_j^i$  (non-conserved)
- Free energy
 
$$F = \int \left\{ f_{bulk}(C_i, \eta_j^i) + \sum_{i,k} \frac{\kappa_{\eta}^{ik}}{2} (\nabla \eta_k^i)^2 + \sum_i \frac{\kappa_c^{ii}}{2} (\nabla C_i)^2 + \sum_{j>i} \frac{\kappa_c^{ij}}{2} (\nabla C_i \cdot \nabla C_j) \right\} d^3r$$
- Bulk free energy density  $f_{bulk}$  keeps  $(C_i, \eta_j^i)$  around (0,0) or (1,1).
- Crossing terms of parameter gradients improves the tunability of interfacial energies.
- Evolution of  $C_i$  (representing electrolyte and electrode phases): Cahn-Hilliard equation.
 
$$\frac{\partial C_i}{\partial t} = \nabla \cdot \left[ M_c \nabla \left( \frac{\delta F}{\delta C_i} \right) \right]$$
- Evolution of  $\eta_j^i$  (representing different polycrystalline grains): Allen-Cahn equation
 
$$\frac{\partial \eta_j^i}{\partial t} = -M_{\eta} \left( \frac{\delta f}{\delta \eta_j^i} \right)$$

## References

[1] Liang et al, *J. Appl. Phys.*, **117** (2015) 065105. [2] Nahor et al, *J. Mater. Sci.*, **49** (2013) 3949-3950. [3] Helmick, PhD thesis, CMU 2010. [4] Cheng and Wen, *Phys. Rev. E*, **91** (2015) 053307.

## Contact angles

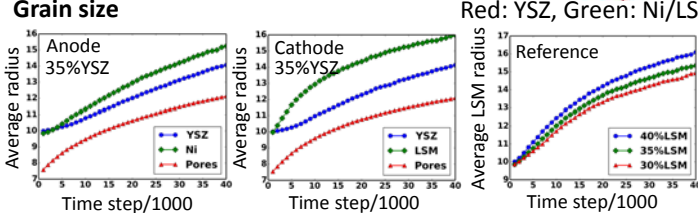
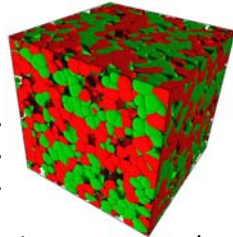


Red: YSZ, Green: Ni/LSM, Blue: Pore

**High energy interfaces**  
 Anode: Ni surface & Ni-YSZ interphase boundary [2].  
 Cathode: LSM grain boundary [3].  
 Reference: All interfaces are the same.

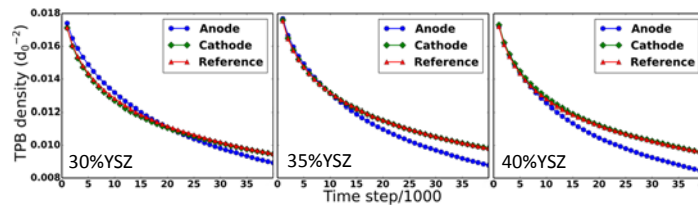
## Microstructure evolutions

- 3D model, 128 × 128 × 128 points.
- Three compositions:
  - 30%YSZ-40%Ni/LSM-30%Pore,
  - 35%YSZ-35%Ni/LSM-30%Pore,
  - 40%YSZ-30%Ni/LSM-30%Pore.
- Initial structure: ~2000 grains.



- Ni/LSM coarsened faster than YSZ.
- Coarsening rate depends on the volume fraction of each phase.

## Triple phase boundary



- The degradation of TPB in anode is the fastest one.
- The degradation of TPB is insensitive to grain boundary energy.

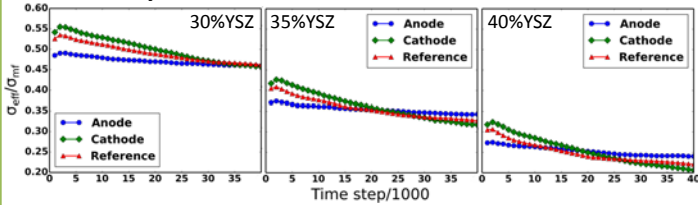
## Conductivity calculations

Solving Poisson's equation

$$\nabla \cdot (\sigma(\vec{r}) \vec{E}) = -\frac{\partial \rho}{\partial t} = 0$$

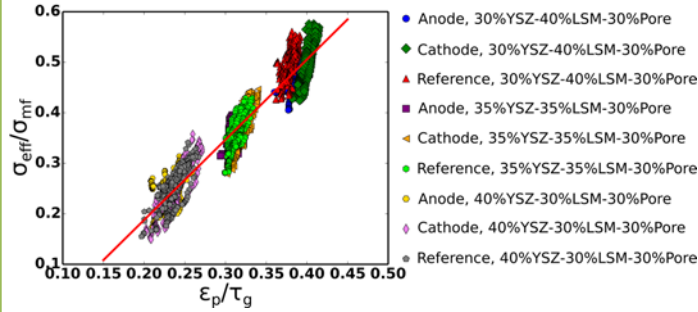
using Bound Charge Successive Approximation algorithm [4].

## Conductivity evolution



- $\sigma_{mf} = \sigma_{YSZ} C_{YSZ} + \sigma_{Ni/LSM} C_{Ni/LSM}$
- $\sigma_{eff}$  is greater with more Ni/LSM in the electrode.
- Conductivity degradation is slowest in anode.

## Correlation between conductivity and geometric properties



$\epsilon_p$ : percolated volume fraction of Ni/LSM  
 $\tau_g$ : geometric tortuosity of Ni/LSM  
 Positive correlation between the conductivity and the ratio between the percolated fraction and the tortuosity of Ni/LSM.

## Conclusions

- The new phase-field model can simulate microstructure evolution in real SOFC electrodes and extracting the "real-time" effective conductivity during coarsening.
- Coarsening rate and TPB density depend on the electrode composition and ratio of interfacial energies.

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