



Predicting Microstructure-Creep Resistance Correlation in High Temperature Alloy over Multiple Time Scales

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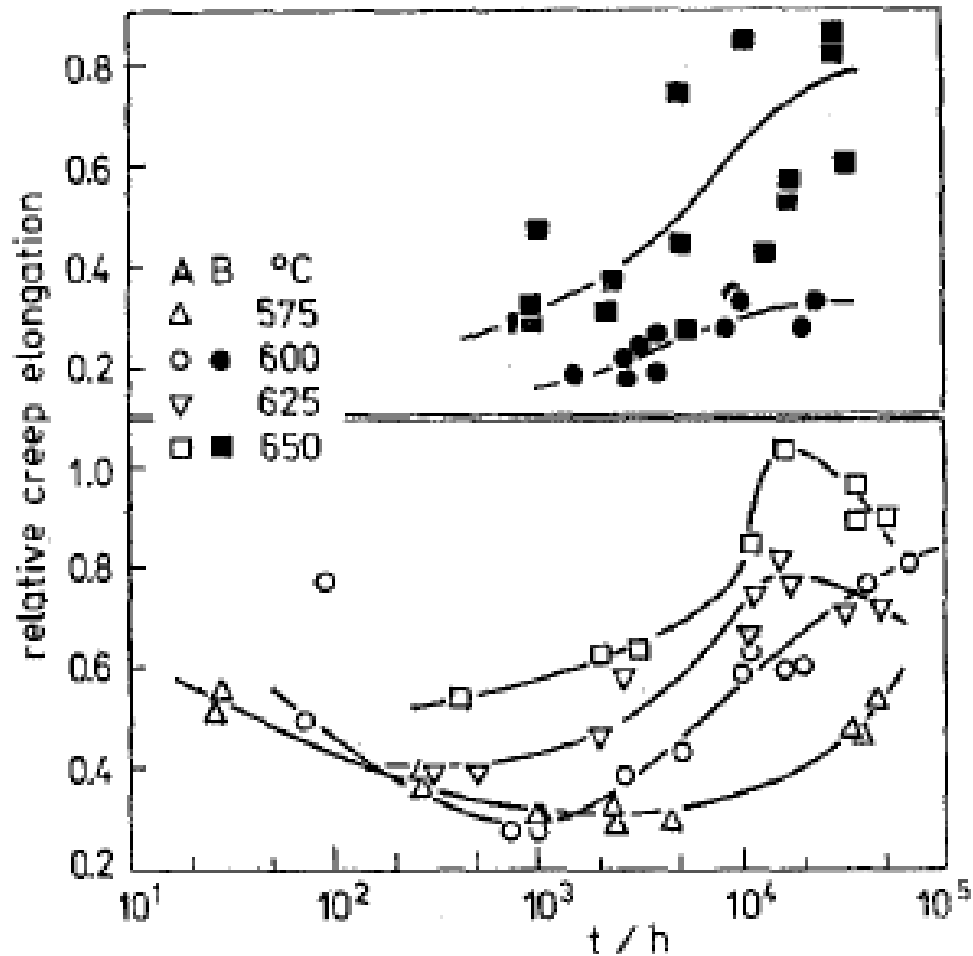
University of California, San Diego & Clemson University

Program Manager: Dr. Jason Hissam

Grant No. : DEFE0011291



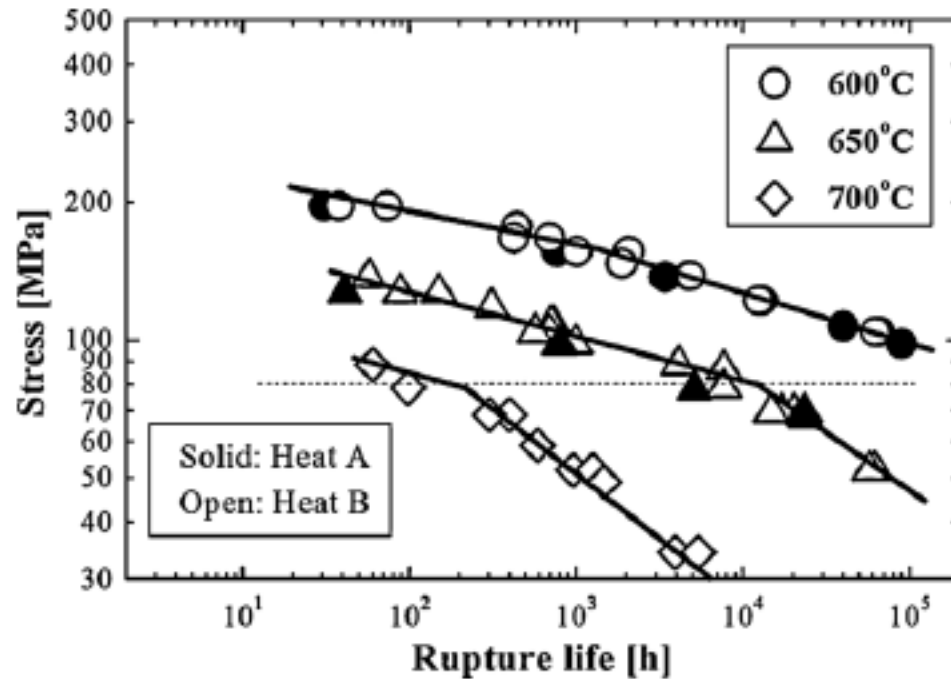
Long Term Creep in Microstructures



Sobotka, 1985, AISI 316 LN Steel

A detailed analysis of microstructure and fractures showed that the developing intergranular precipitation and the following coarsening of grain boundary particles of $M_{23}C_6$, Cr_2N and especially of the sigma phase are responsible for the significant changes of both creep and impact fractures from the point of view of their plasticity.

Long Term Creep in Microstructures



Igarashi, 2011

Fig. 1. Stress and temperature dependence of creep rupture life in Gr.91 steel.

The cause of the breakdown of creep strength has been studied in Gr.91 steel. The results show that the contribution of the static recovery of subgrains to creep deformation causes the breakdown of creep strength. The subgrain boundaries are mainly stabilized by $M_{23}C_6$ and MX precipitates. MX precipitates are thermally stable even in the time range when coarsening of subgrains takes place. Whereas $M_{23}C_6$ precipitates are not thermally stable and the aggregation of $M_{23}C_6$ precipitates takes place in the time range when coarsening of subgrains happens. Therefore, loss of pinning force from $M_{23}C_6$ precipitates is responsible for the static recovery of subgrains. MX has nothing to do with the static recovery. The

Proposal Research Workflow



Task-3

**Theoretical Framework to
Characterize GB Segregation**

Task-1

**Nanocrystalline Ni and Bulk W
Based Alloy Control Sample
Preparation**

Task-4

**Microstructure Level Multiscale
Modeling to Predict Effect of GBs on
Embrittlement, Creep, and rupture**

Task-2

**In-Situ Microstructural Testing of GB
Evolution and Strength**



U.S. DEPARTMENT OF
ENERGY

Task 1:

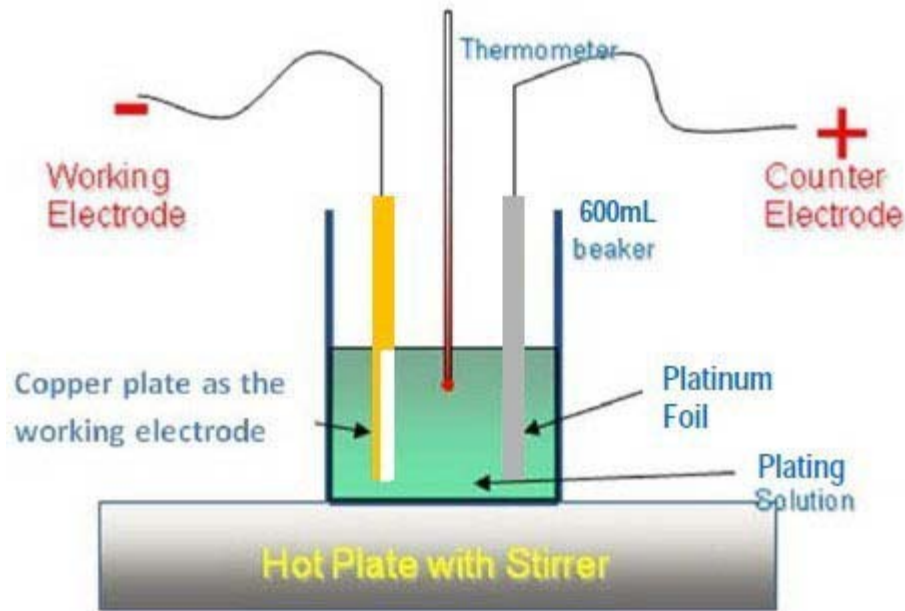
Fabrication and Characterization of Control Samples

UC San Diego

- **Task 1, Part A:** Nanocrystalline Ni and Ni-W Foils (Synthesized by Electrodeposition)
- **Task 1, Part B:** Bulk W based Alloys (Synthesized by Ball Milling + SPS)

1 Task 1: Fabrication and Characterization of Control Samples – Part A

Preparing Nanocrystalline Ni and Ni-W Specimens for Mechanical Test



Temperature: 65 °C

Deposition time:
30 min to 2h

Chemicals	Weight(g/L)
NiSO ₄ .6H ₂ O	300
NiCl ₂ .6H ₂ O	45
H ₃ BO ₃	45
Saccharine	5
Sodium Lauryl Sulfonate (CH ₃ (CH ₂) ₁₁ OSO ₂ Na)	0.25

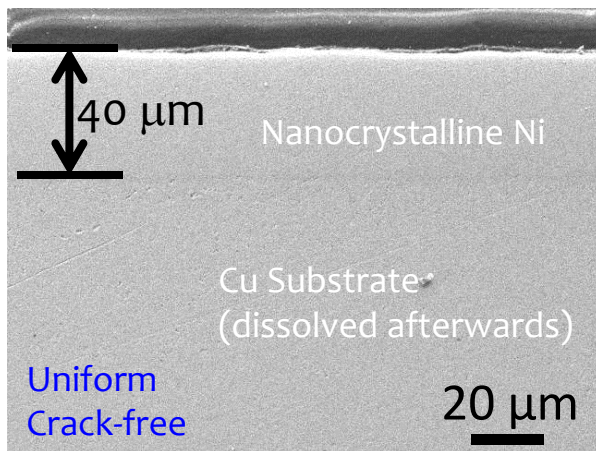
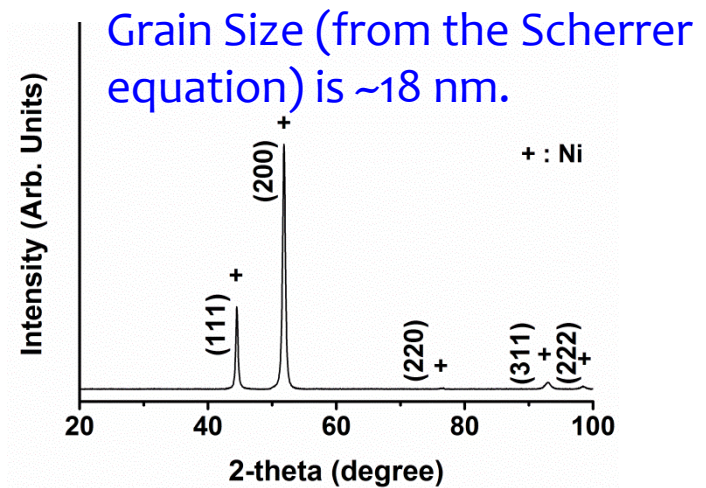


	Current	Time (ms)	Peak (A/cm ²)
Forwards	On	5	0.4
	off	15	

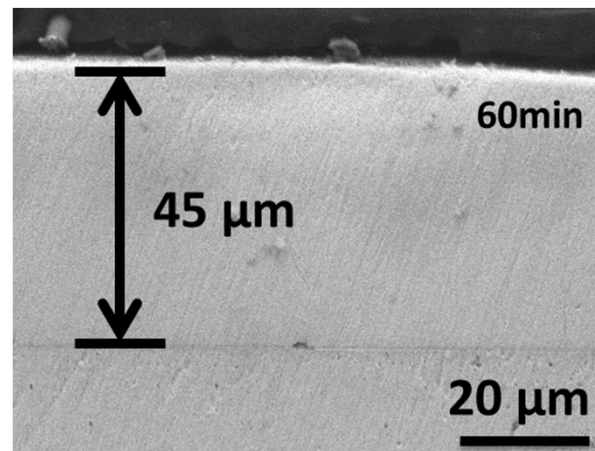
El-Sherik, et al., J of Materials Science 30, 5743 (1995)

Free-Standing Nanocrystalline Ni Specimens

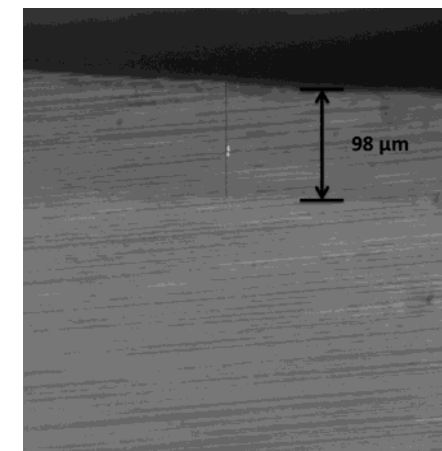
Sent to Purdue for Creep Testing...



30min



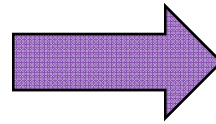
60min



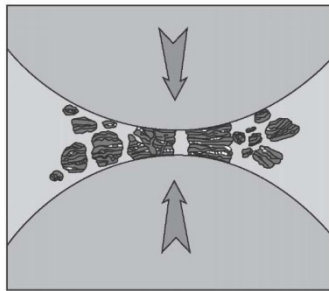
120min

Two-step to Prepare Bulk Nanocrystalline W Alloys

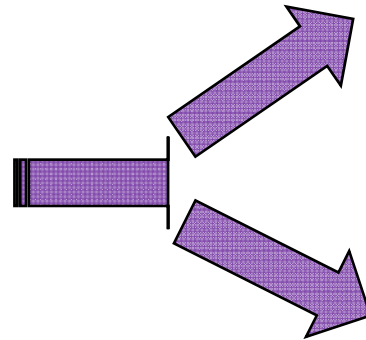
Nanocrystalline
Powders



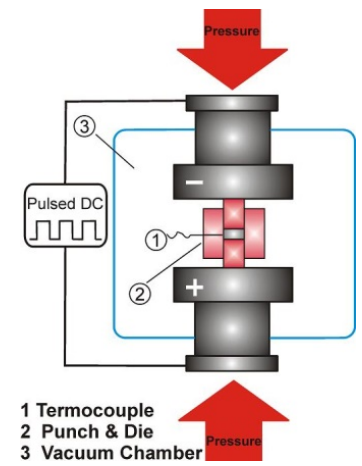
Bulk Nanocrystalline
Material



High Energy Ball Milling



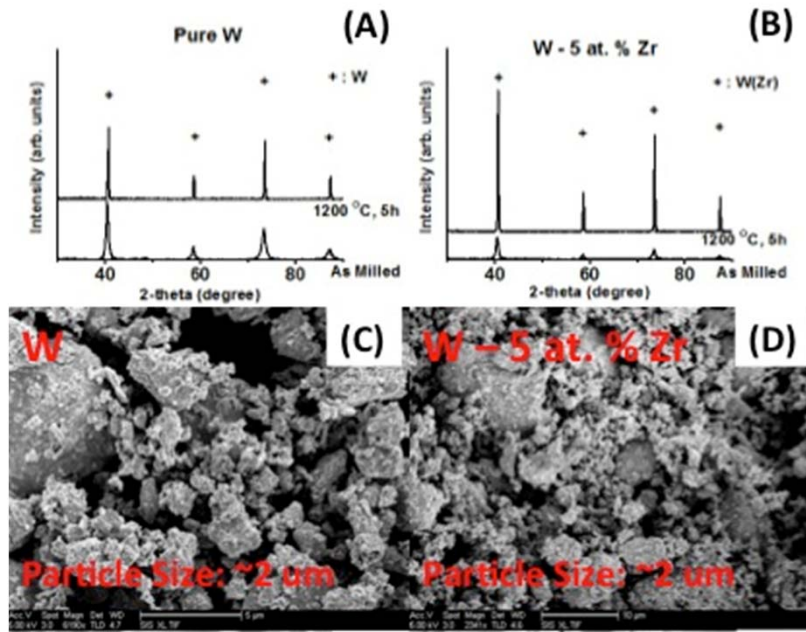
Pressureless Sintering



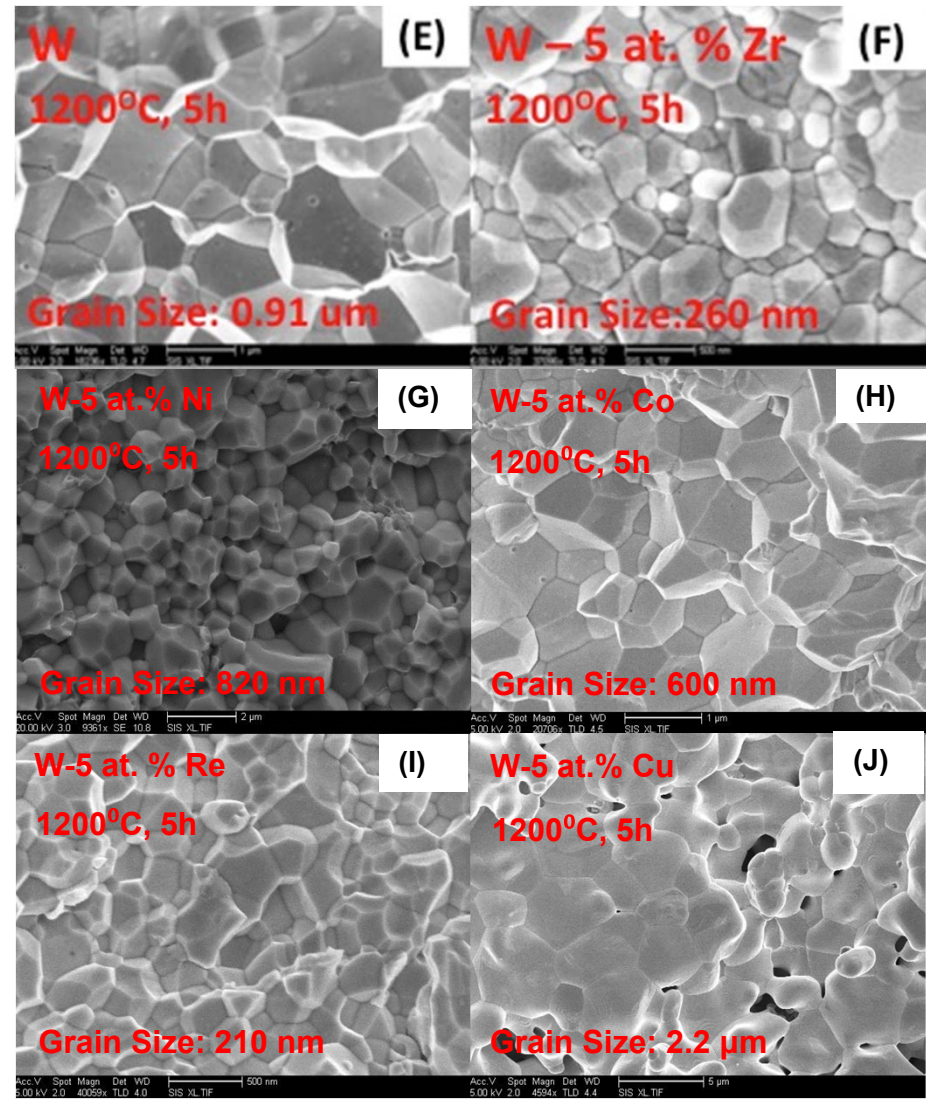
Spark Plasma Sintering

Task 1: Fabrication and Characterization of Control Samples – Part B

Bulk Nanocrystalline W Alloys



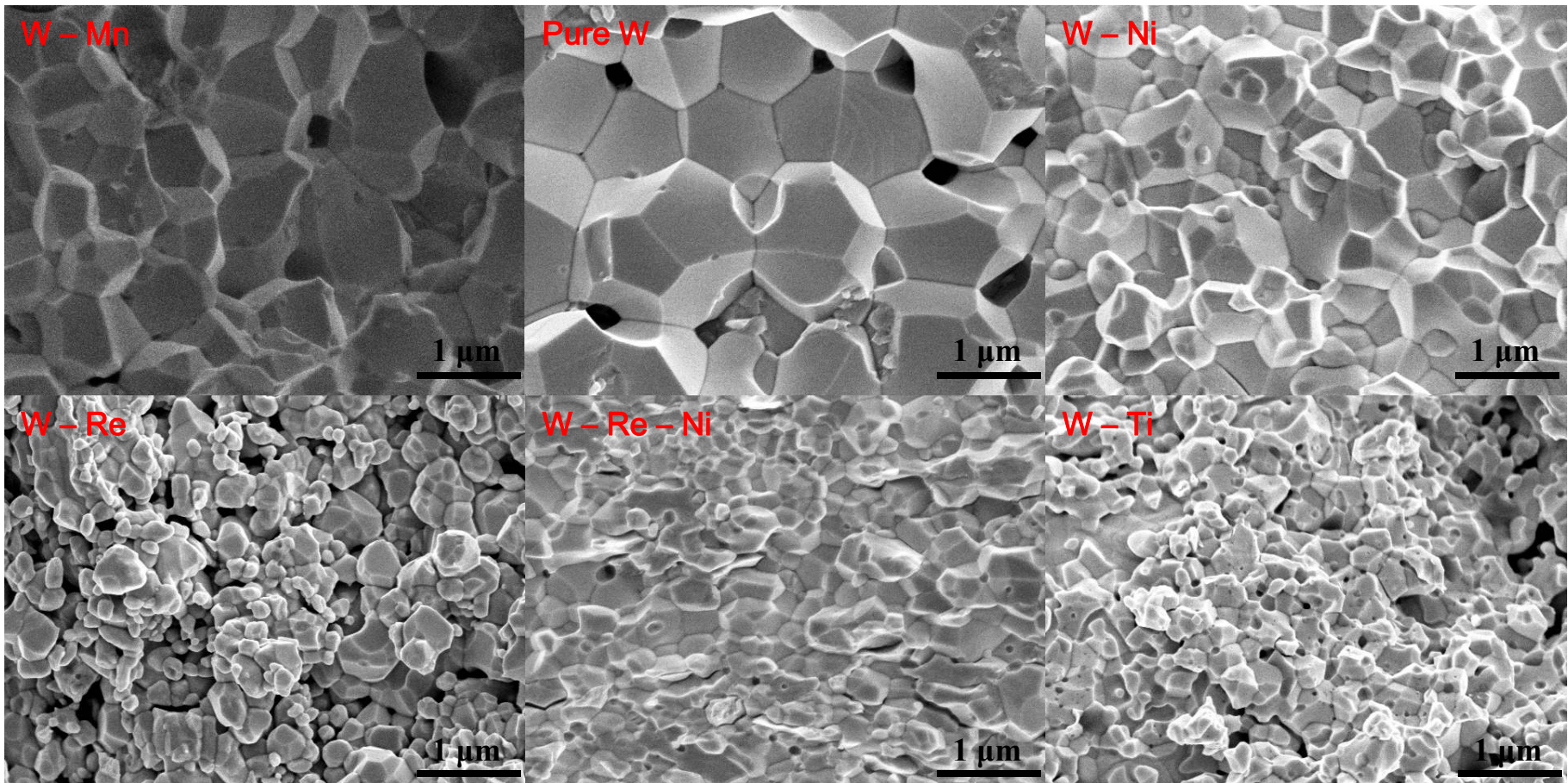
Ball Milled Powder



Pressureless Sintered Samples

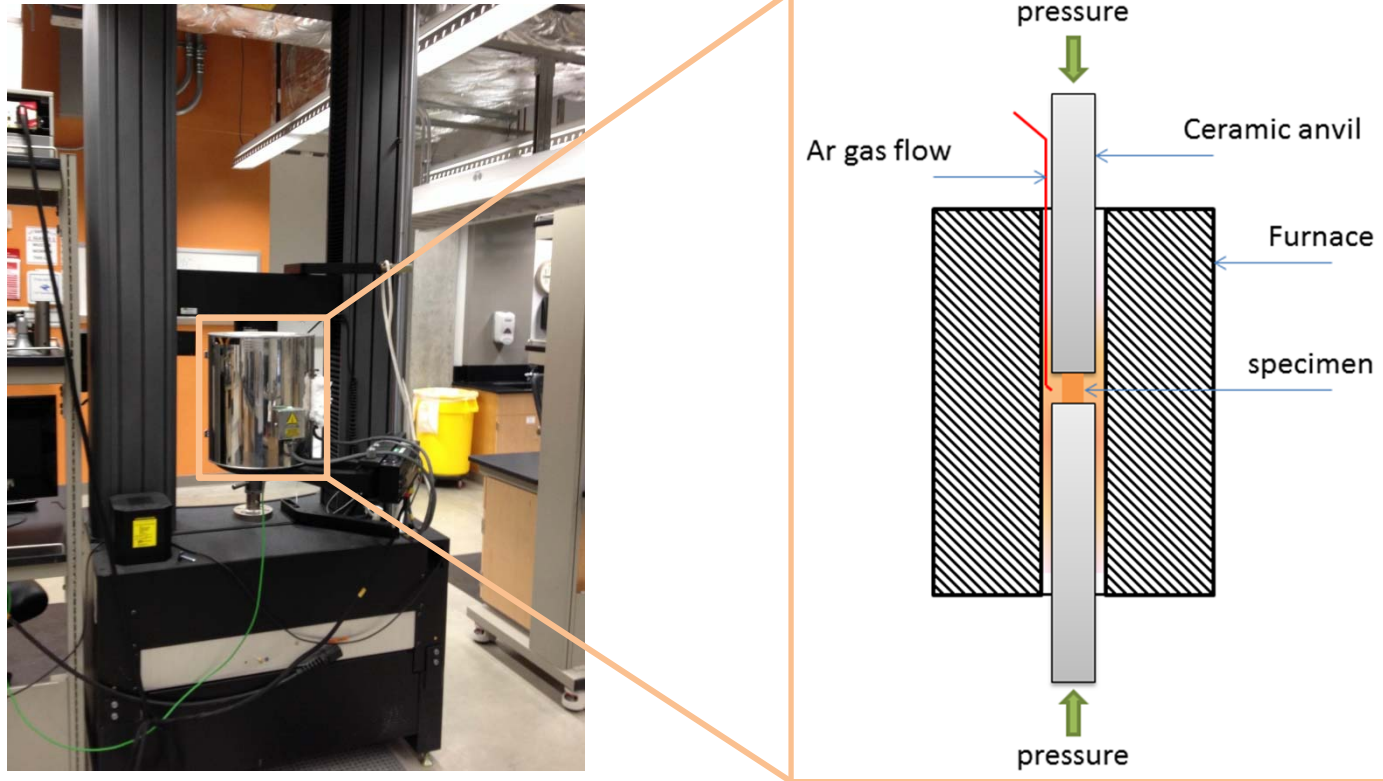
Task 1: Fabrication and Characterization of Control Samples – Part B

Bulk Nanocrystalline W Alloys



Spark Plasma Sintered Samples

Creep Test Setup

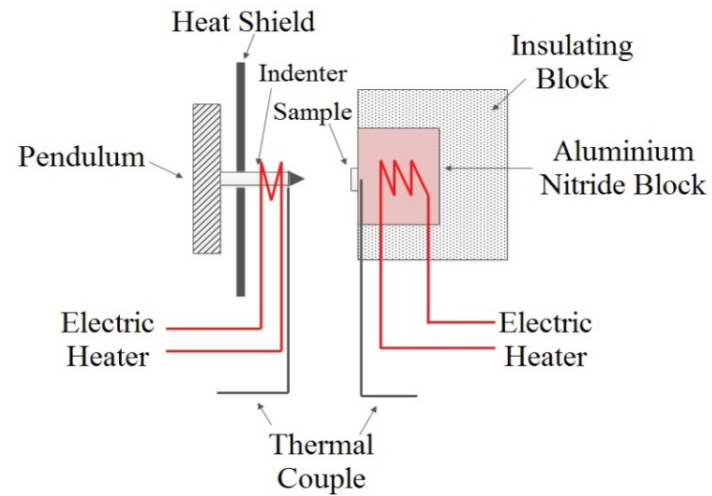
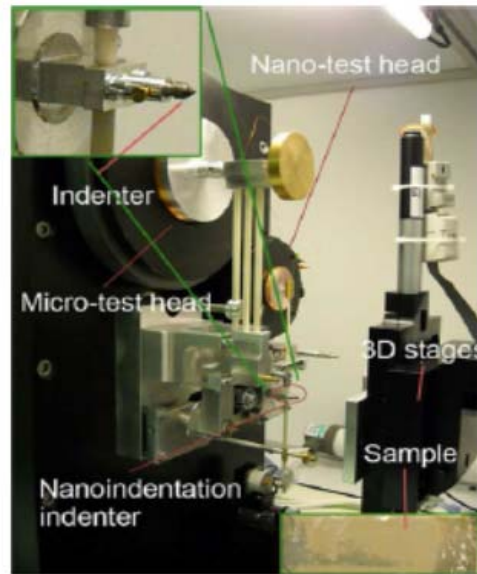


INSTRON Instrument Equipped with Heating Furnace

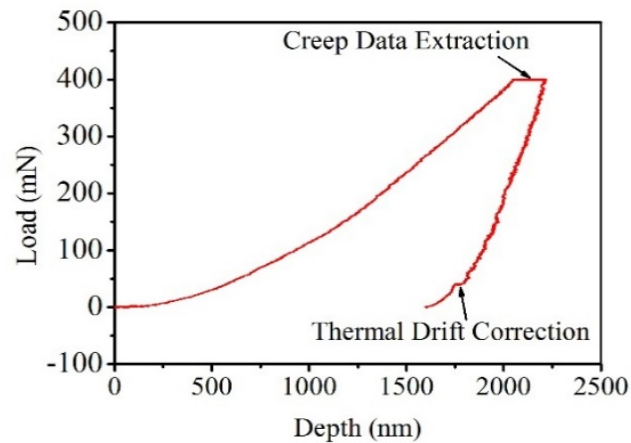
Planned Experiments:

- The creep tests for the specimens pure W, W-5%Ni, W-5%Ti, W-5%Co, W-5%Re and W-5%Cu will be performed at elevated temperature 400°C and/or 750°C.
- Creep data will be collected to evaluate the mechanical properties of the W alloys with different doping elements.
- Moreover, the microstructure evolution of creep tested W alloys specimens will be characterized by SEM and TEM.

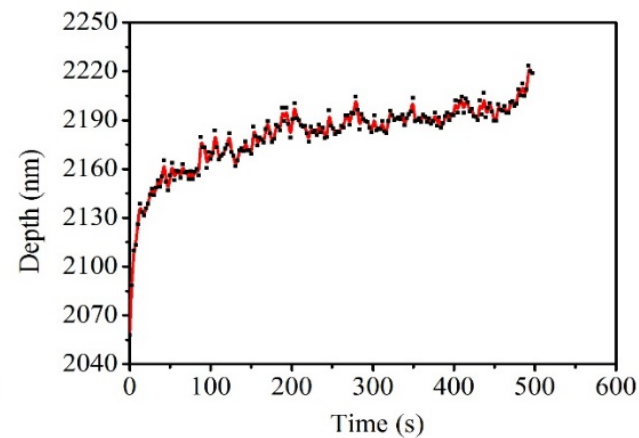
Task 2-High Temperature Nanoindentation Tests



(a.)



(b.)



(c.)

Task 3:

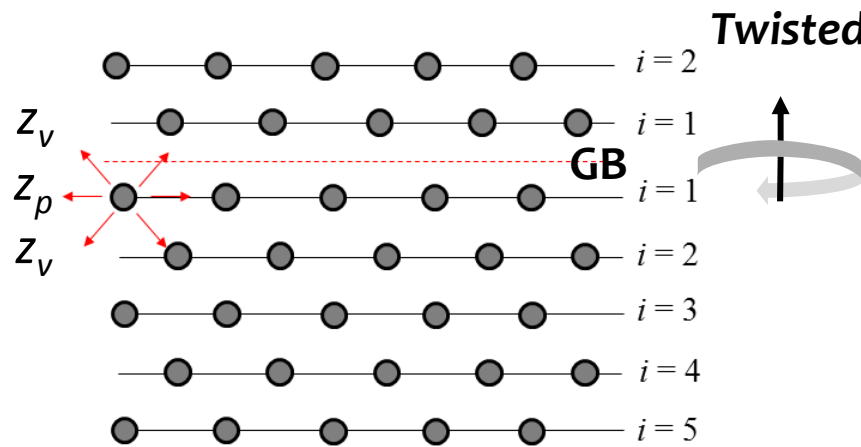
A New Theoretical Framework to Characterize GB Segregation

UC San Diego

- **Task 3, Part A:** The Classical GB Segregation Model (Assessments of W alloys with the Wynbaltt-Chatain Model)
- **Task 3, Part B:** Non-Classical High-*T* GB Segregation (Coupled with GB Premelting/Interfacial Disordering)

Task 3, Part A: Classical GB Segregation Model

Assessment of W based Alloys by the Wynblatt-Chatain Model



A Mclean type segregation equation

$$\frac{X_i}{1 - X_i} = \frac{X_\infty}{1 - X_\infty} \exp\left(-\frac{\Delta H_i^{seg}}{kT}\right)$$

i th layer composition

Bulk composition

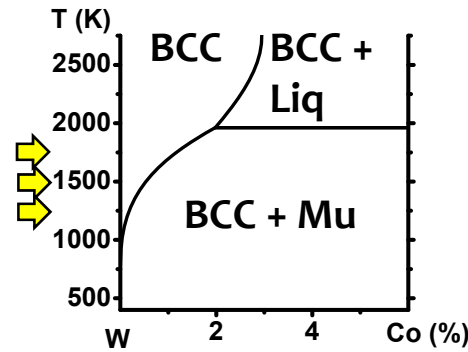
GB absorption $\Gamma_{GB} = 2 \sum_i (X_i - X_\infty)$

Segregation Enthalpy

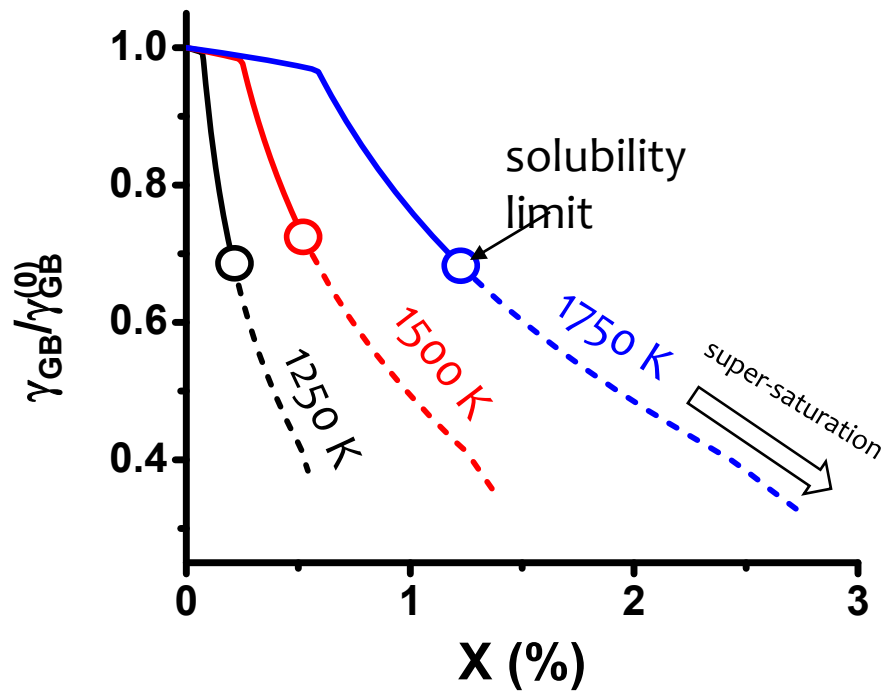
$$\Delta H_i^{seg} = \begin{cases} \underbrace{-0.5Q(e_{BB} - e_{AA})z_v}_{\text{bonding energy difference}} \underbrace{\Delta E_{el}^1}_{\text{strain energy}} + \underbrace{2\omega_S}_{\text{Solute-dopant interactions}} \left[\begin{array}{l} zX_\infty - z_p X_1 - z_v X_2 \\ -(1-Q)z_v X_1 - \frac{1}{2}Qz_v \end{array} \right] & i = 1 \\ \underbrace{-\Delta E_{el}^i}_{\text{strain energy}} + \underbrace{2\omega_S}_{\text{Solute-dopant interactions}} (zX_\infty - z_p X_i - z_v X_{i+1} - z_v X_{i-1}) & i > 1 \end{cases}$$

W-Co (Co-doped W) Alloy

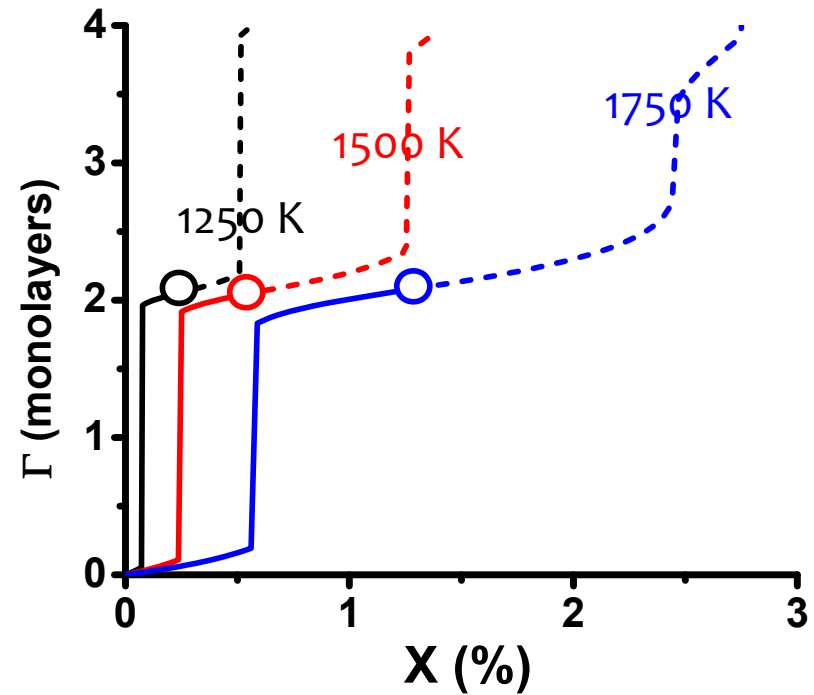
Phase diagram



GB energy

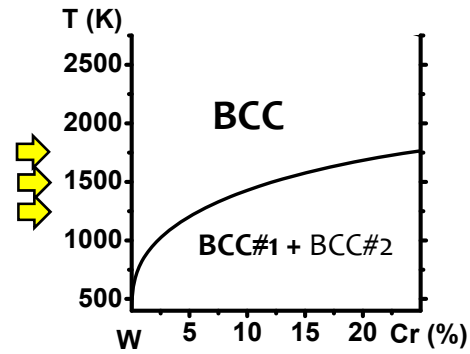


GB absorption

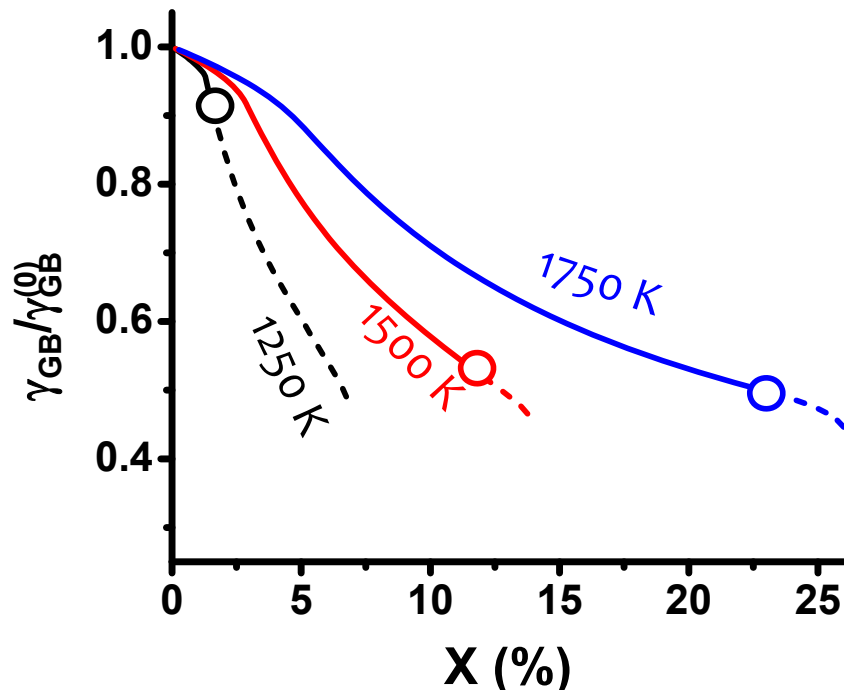


W-Cr Alloy

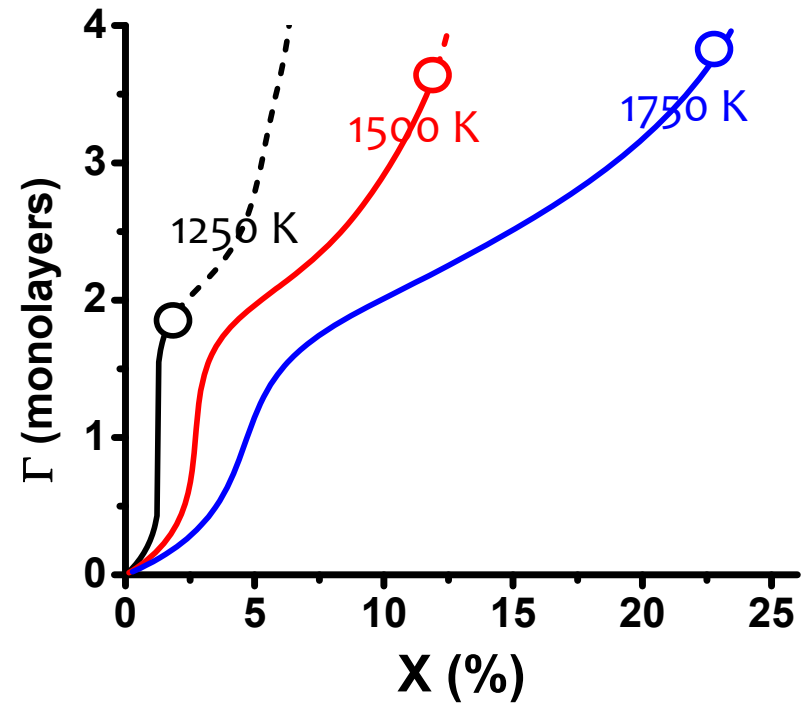
Phase diagram



GB energy

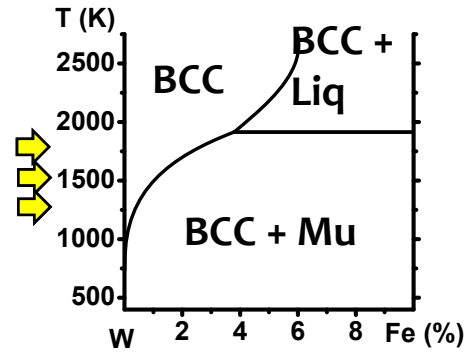


GB absorption

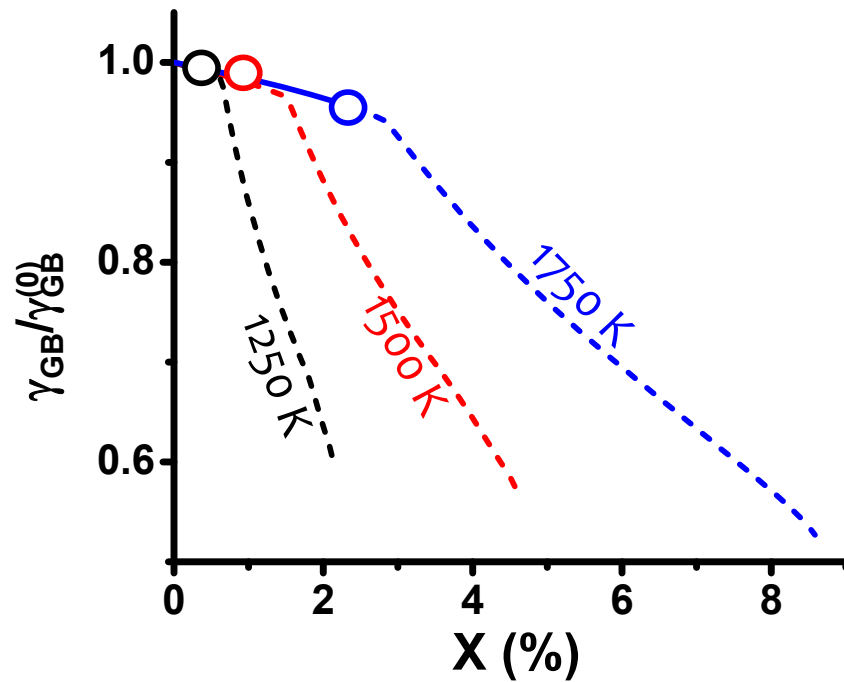


W-Fe Alloy

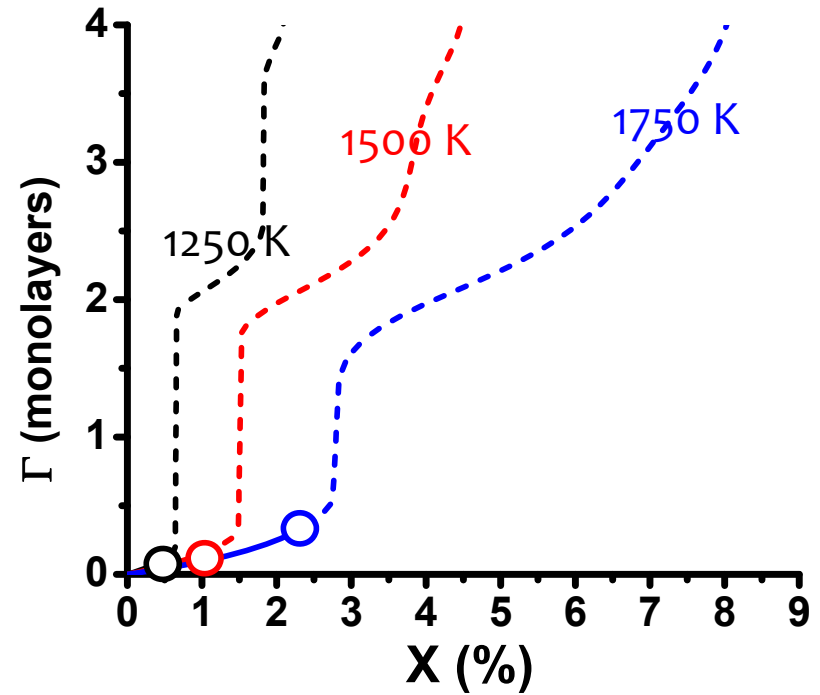
Phase diagram



GB energy

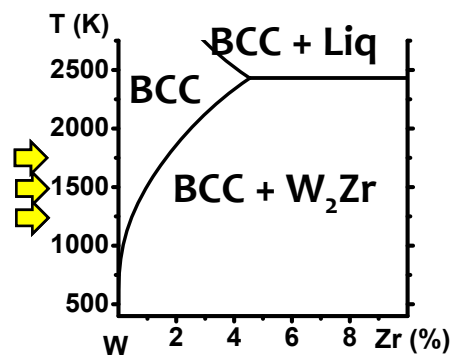


GB absorption

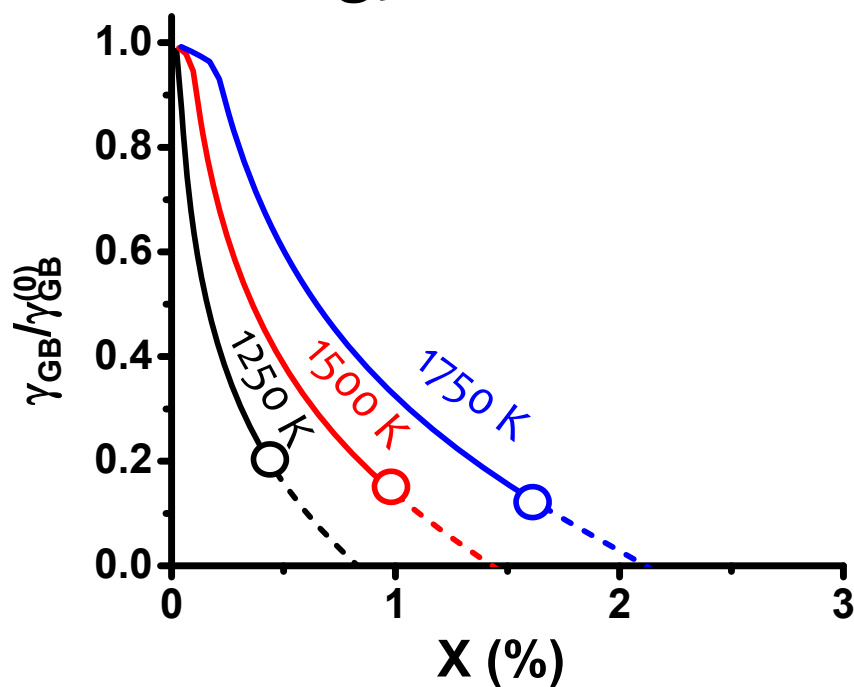


W-Zr Alloy

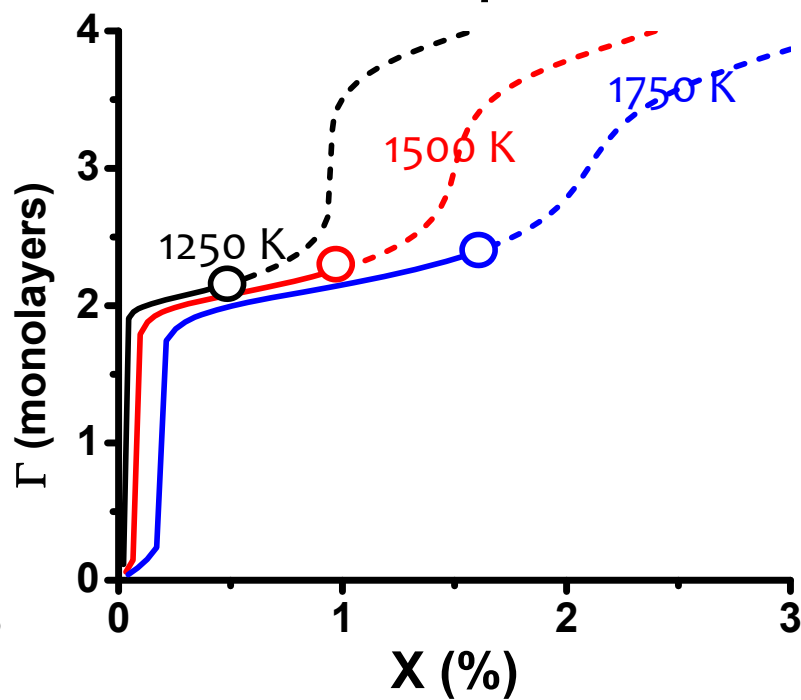
Phase diagram



GB energy



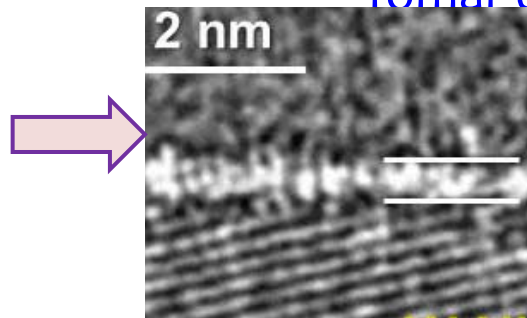
GB absorption



Task 3, Part B: High-T Segregation + GB Disordering

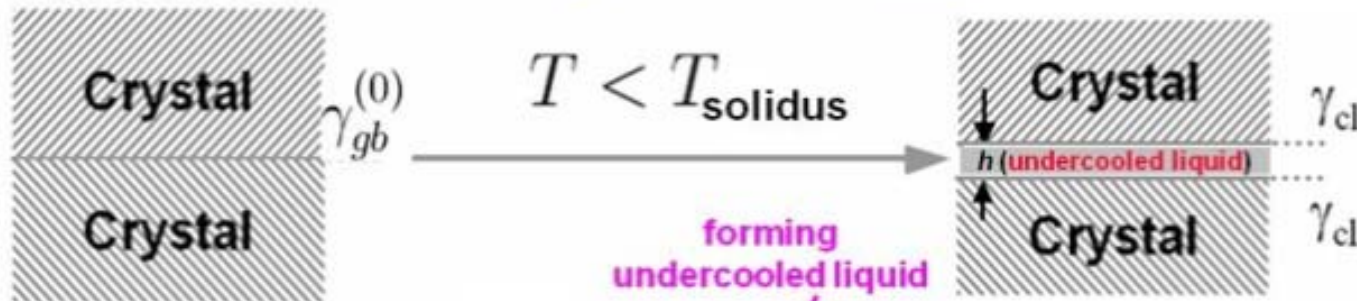
Develop a thermodynamic framework to predict a “new” type of high-T (premelting-like) GB segregation
 Luo *et al.* at Clemson/UCSD

Multiscale modeling to characterize microstructure-dependent creep
 Tomar *et al.* at Purdue



Discovered by the Luo group
Appl. Phys. Lett. 2005
Acta Mater. 2007

Thermodynamic Principle



A subsolidus quasi-liquid film is thermodynamically stable if:

$$\Delta G_{vol.} \cdot h < -\Delta\gamma \equiv \gamma_{gb}^{(0)} - 2\gamma_{cl}$$

Prior Relevant Studies

Thermodynamic Model for High- T GB Disordering

A Thermodynamic Variable: λ

Luo & Shi, *Appl. Phys. Lett.* 92:101901 (2008)

Thermodynamically stable if:

$$\Delta G_{\text{amorph.}} \cdot h < -\Delta\gamma$$

Define & quantify:

$$\lambda \equiv \text{Max}_{(0 < X_M < 1)} \left\{ \frac{-\Delta\gamma}{\Delta G_{\text{vol}}} \right\}$$

Representing the thermodynamic tendency to stabilize a quasi-liquid film

λ scales the film thickness

Continuum approx. for metals:

$$f(h) \approx 1 - e^{-h/\xi} \quad \text{Coherent length}$$

$$h_{EQ} \approx \xi \cdot \ln(\lambda/\xi)$$

$$\Delta\gamma \equiv -(\gamma_{gb}^{(0)} - 2\gamma_{cl})$$

Miedema type "macroscopic atom" model (Benedictus-Böttger-Mittemeijer Model)

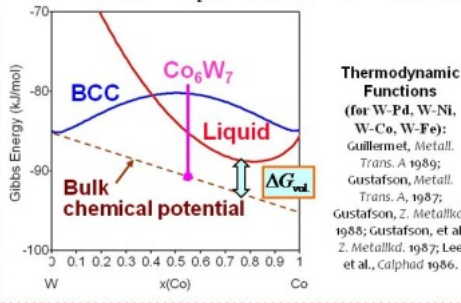
$$\gamma_{cl} = F_M^W(X_M) \cdot \frac{\Delta H_{\text{W in M}}^{\text{interface}}}{C_0 V_W^{2/3}} + \frac{H_W^{\text{fasc}}}{C_0 V_W^{2/3}} + \frac{1.9RT}{C_0 V_{\text{WM}}^{2/3}}$$

Benedictus, Böttger, Mittemeijer, *Phys. Rev.* 54: 9109 (1996)

A recent review: Jeurgens, Wang, Mittemeijer, *Int. J. Mat. Res.* 100:128 (2009)

CalPhad

$$\Delta G_{\text{vol}} = G_{\text{liquid}}^f - [X_M \mu_M + (1 - X_M) \mu_W]$$



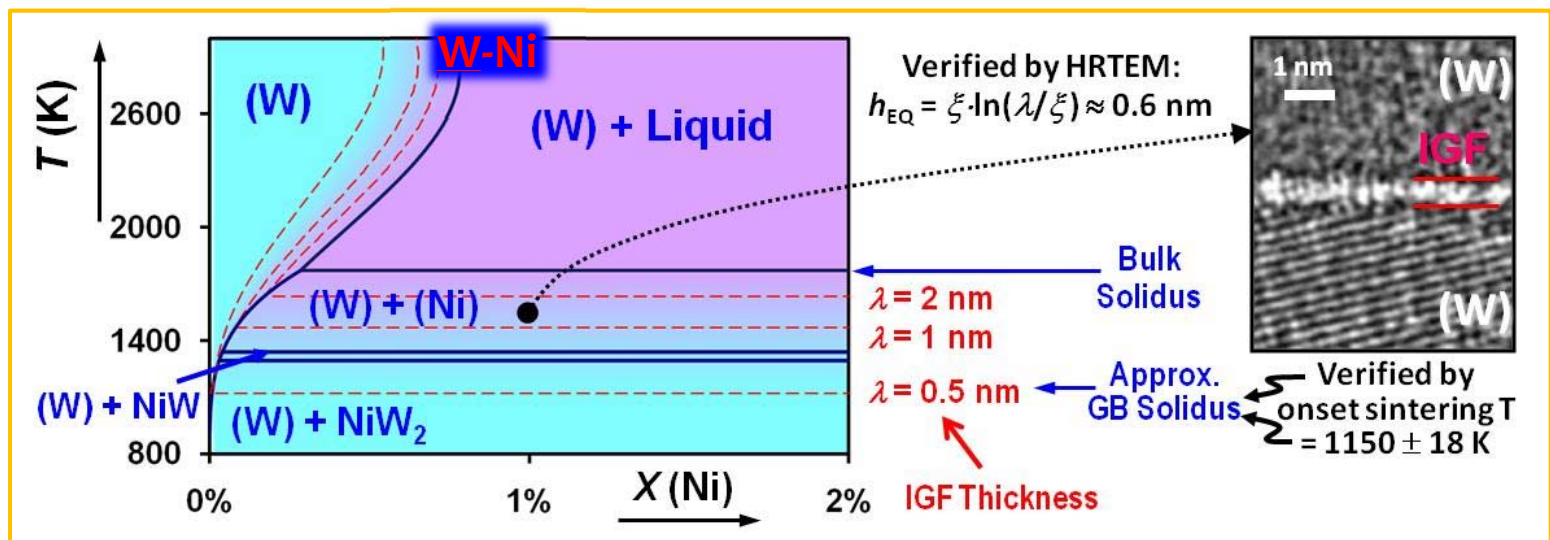
See: related review article

"Developing Interfacial Phase Diagrams for Applications in Activated Sintering and Beyond: Current Status and Future Directions"

Journal of the American Ceramic Society

95: 2358 (2012)

Computed GB λ Diagrams to Represent Levels of GB Disorder



The Model for Ternary Alloys

Interfacial energies

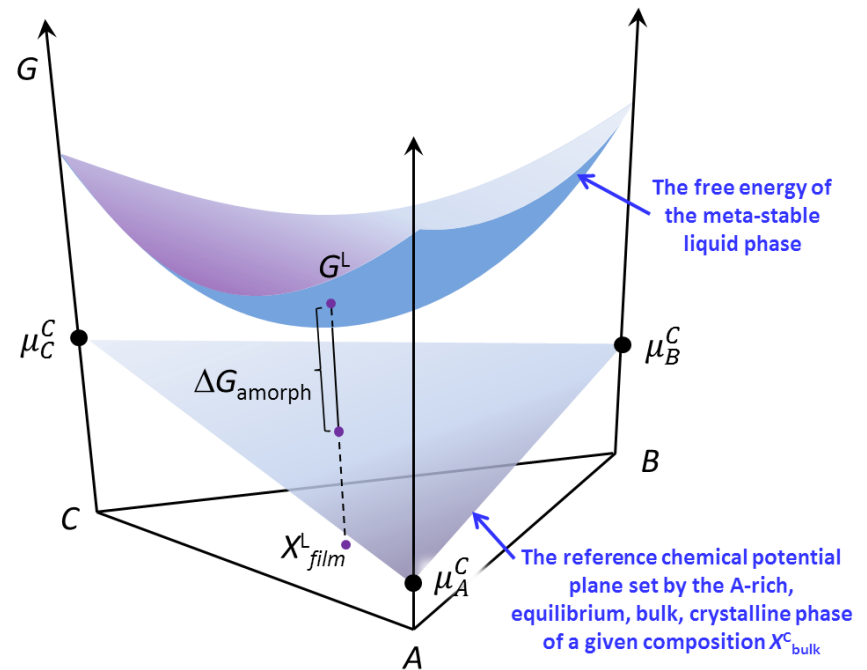
$$\Delta\gamma = 2\gamma_{cl} - \gamma_{GB}^{(0)} \left\{ \begin{array}{l} \gamma_{GB}^{(0)} \approx \sum_i X_i^C \gamma_{GB,i}^{(0)} + \overbrace{\frac{Q}{C_0 V^{2/3}} \sum_{i \neq j} X_i^C X_j^C \Omega_{i-j}^C}^{\text{excessive interaction energy}} \\ \gamma_{cl} \approx \gamma_{cl}^{(0)} = \frac{1}{C_0 V^{2/3}} \left[\underbrace{\sum_i X_i^C \left(\Delta H_i^{fuse} + \sum_{i \neq j} X_j^L \Omega_{i-j}^L \right)}_{i-j \text{ interfacial energy}} - \frac{1}{2} \left(\underbrace{\sum_{i \neq j} X_i^L X_j^L \Omega_{i-j}^L + \sum_{i \neq j} X_i^C X_j^C \Omega_{i-j}^C}_{\text{reference energy}} \right) + \underbrace{1.9RT}_{\text{entropy due to near interface ordering}} \right] \end{array} \right.$$

Miedema type model modified to use CALPHAD parameters

Bulk free energy of undercooled liquid

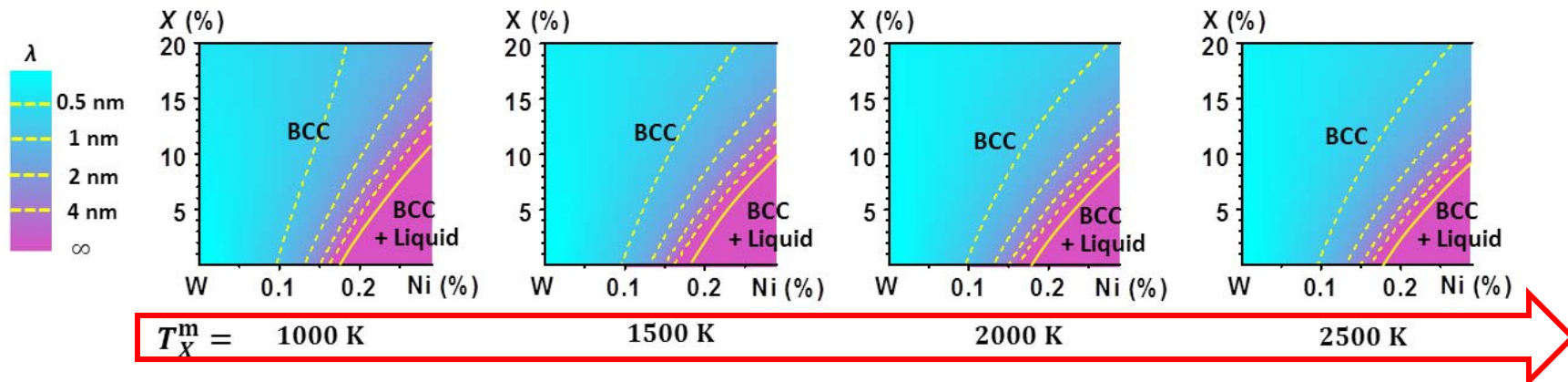
$$\Delta G_{\text{amorph}}^{(\text{mol})} = G^L(\mathbf{X}_{\text{film}}^L) - \sum_i \mu_i^C X_i^L$$

Multicomponent free energy function built based on binary CALPHAD database



The Effects of Co-Doping on Enhancing or Suppressing GB Disorder

The effects of adding a co-alloying element X to W-Ni



Change the melting point of the co-alloying element X

Assumptions:

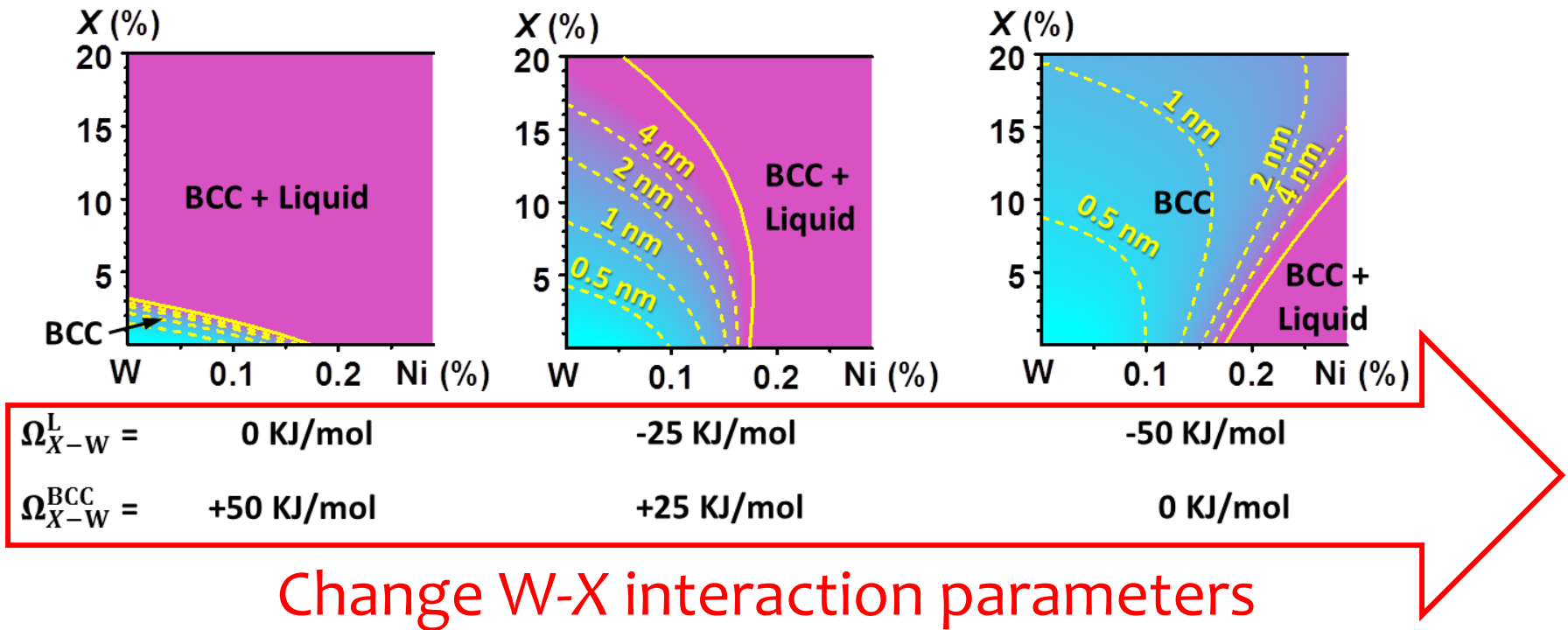
X mix ideally with W and Ni

X mix ideally with Ni and ($-\Omega_{W,X}^{BCC} = 95.0 \text{ kJ/mol}$)

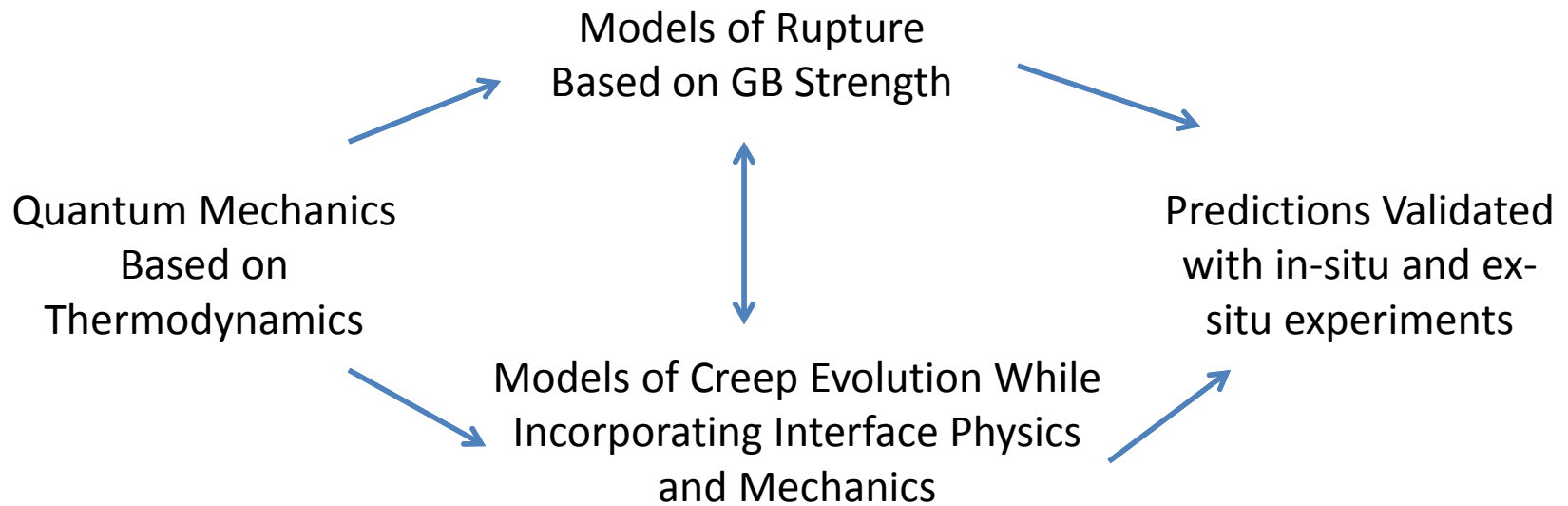
Zhou & Luo,
Acta Materialia 2015

The Effects of Co-Doping on Enhancing or Suppressing GB Disorder

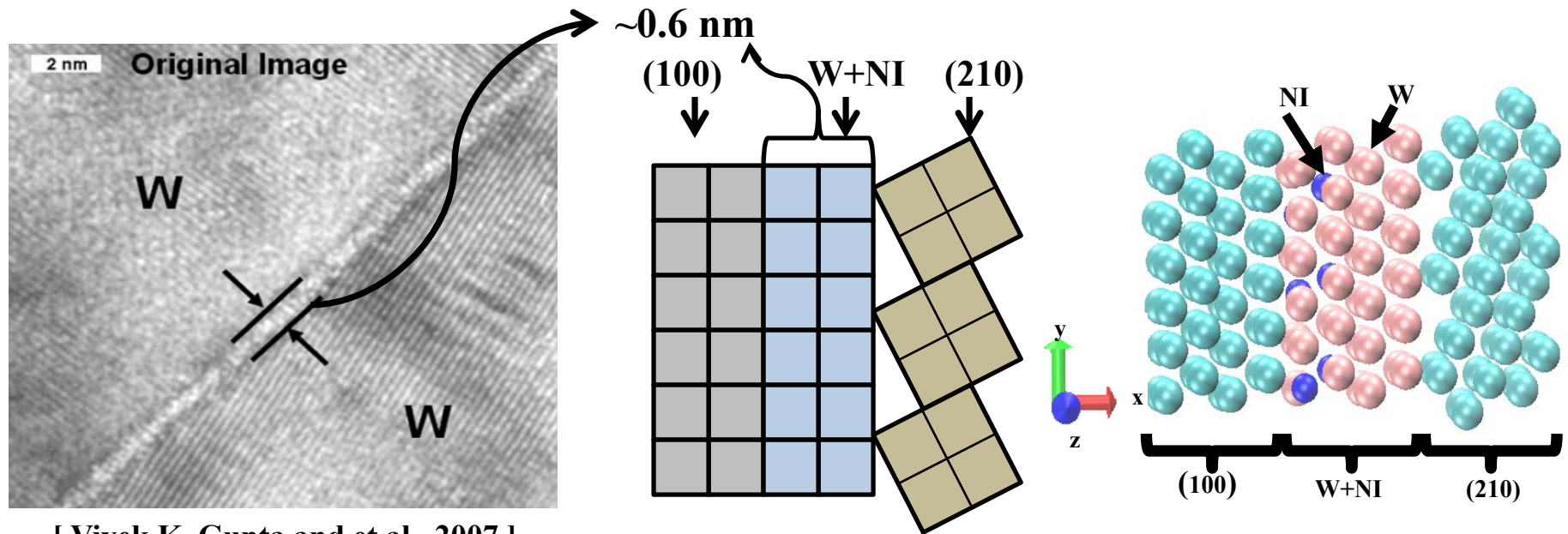
The effects of adding a co-alloying element X to W-Ni



Task 4: Multiscale Models for Rupture Strength and Long Term Creep



➤ Quantum mechanical calculation of GB Strength

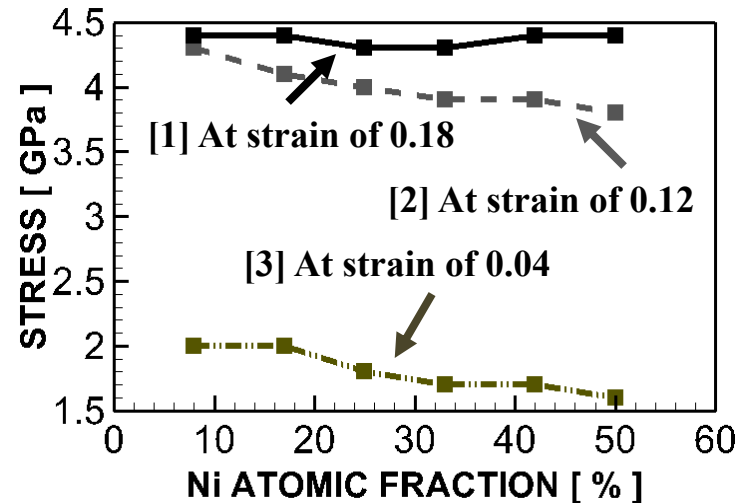
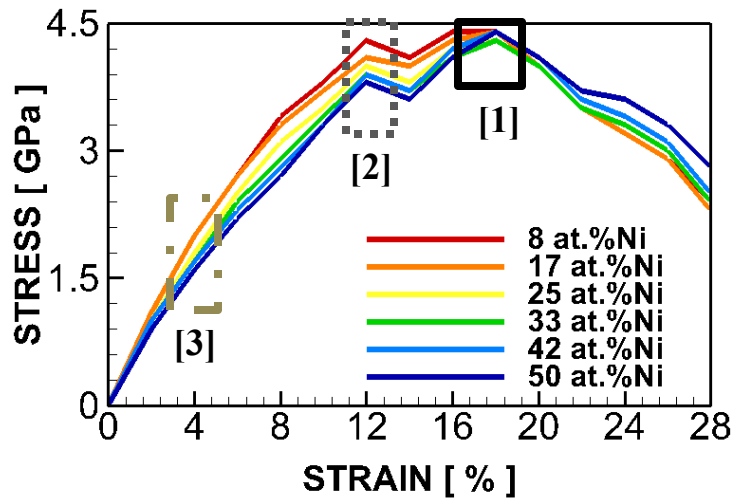


[Vivek K. Gupta and et al., 2007]

- ❖ time step: 5 a.u. , total 2000 steps Becquart and et al., 2006
- ❖ cutoff energy for wavefunction : 350 eV Nose and Shuichi, 1984
- ❖ Nose-Hoover thermostat : 300K, 400K, 500K, 600K Hoover and William, 1985
- ❖ electronic fake mass for CPMD : 400 a.u. Perdew and et al., 1996 Vanderbilt and David, 1990
- ❖ number of k-points for integration over Brillouin zone : 32x32x32 Monkhorst and Pack., 1996

➤ Stress – strain relation

(1) Unsaturated Ni - W



Yield strength: at strain 4%,

First peak: at strain 12%

Yield strength and first peak's values have dependent on the Ni volume fraction.

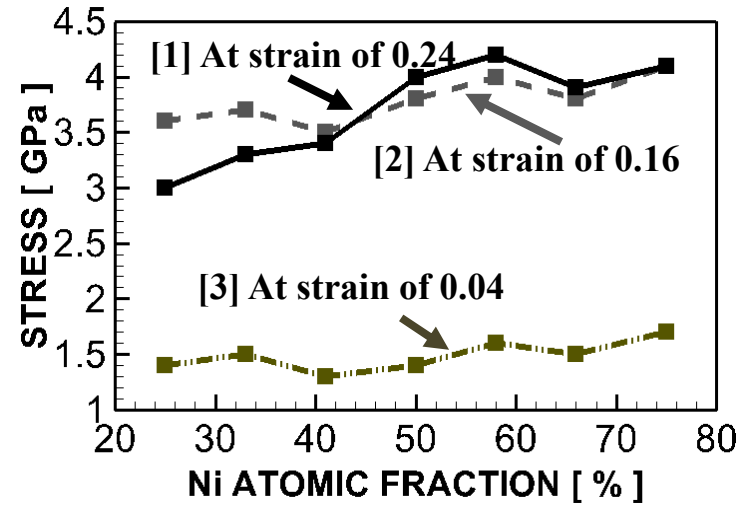
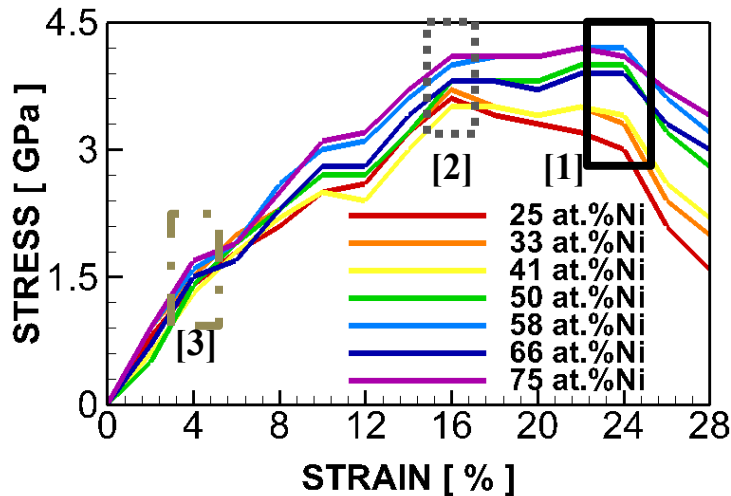
Second peak: at strain 18%

The second peak's values are not depend on the Ni volume fraction.

Ultimate tensile strength : strain of 12~18%

The maximum tensile strength is not affected by Ni volume fraction for the unsaturated W-Ni.

(2) Saturated Ni - W



Yield strength: at strain 4%,

First peak: at strain 16%

Yield strength and first peak's values have dependent on the Ni volume fraction.

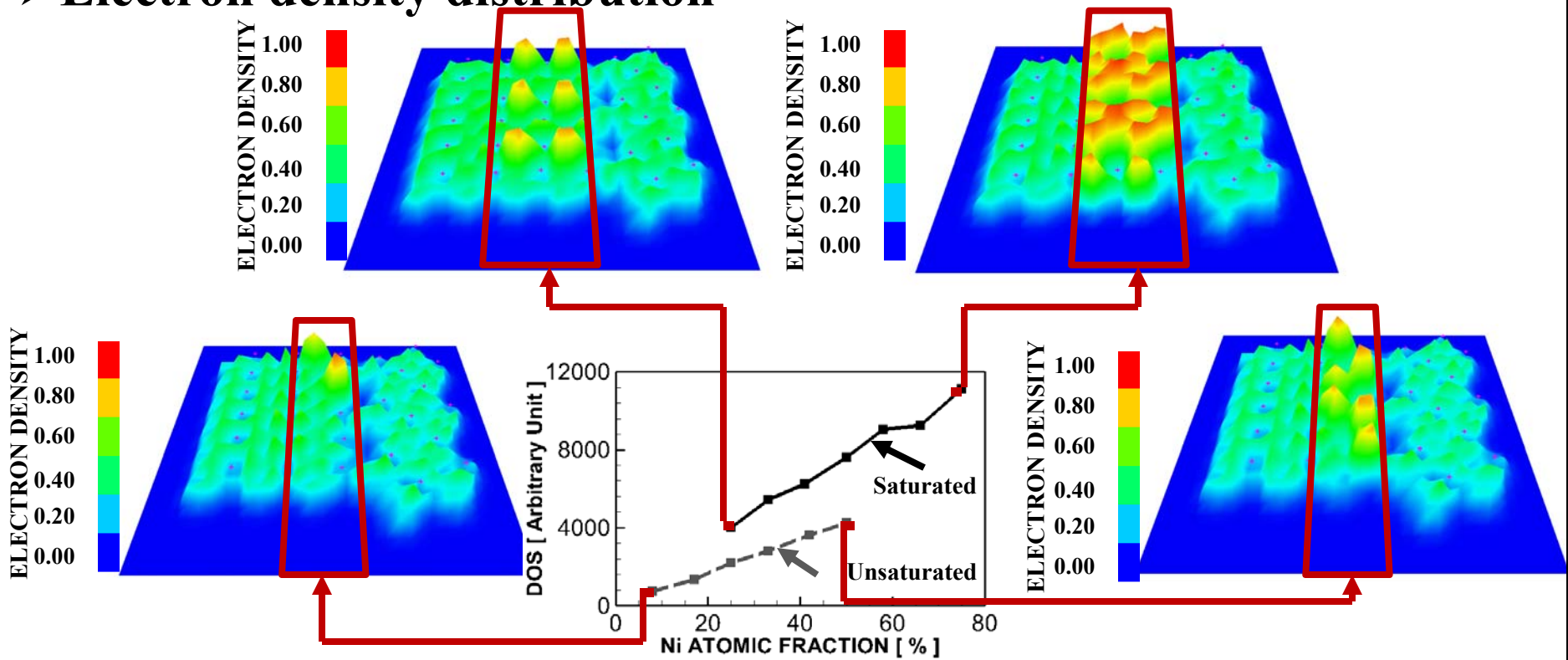
Second peak: at strain 24%

The second peak's values have the largest dependence on the Ni volume fraction.

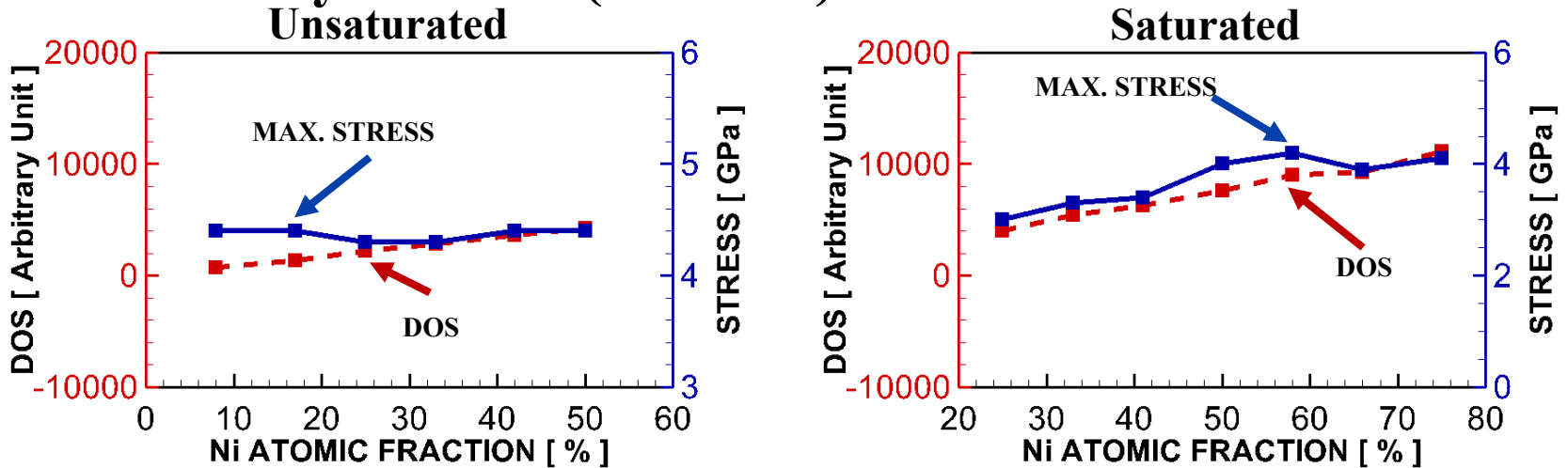
Ultimate tensile strength : strain of 16~24%

The maximum tensile strength is not affected by Ni volume fraction for the saturated W-Ni.

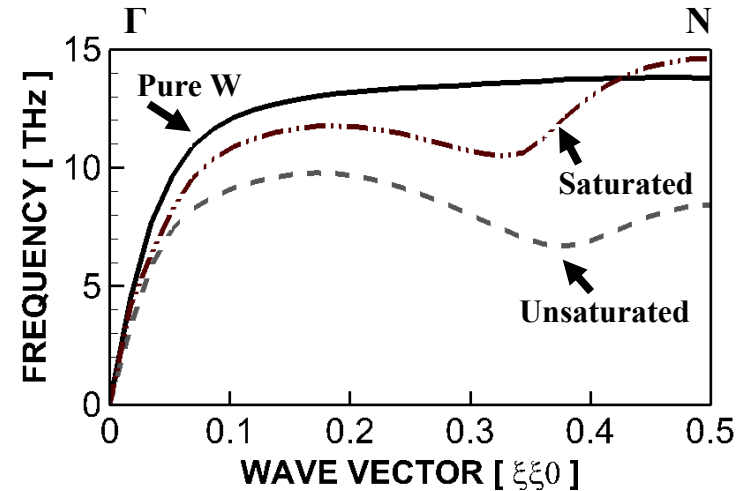
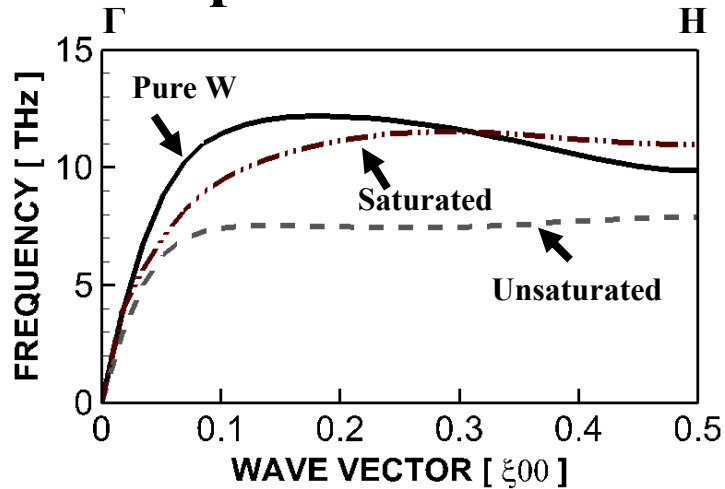
➤ Electron density distribution



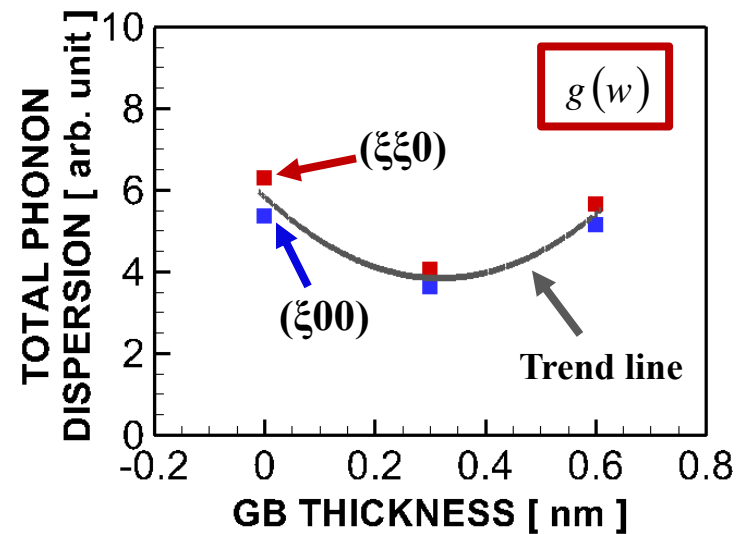
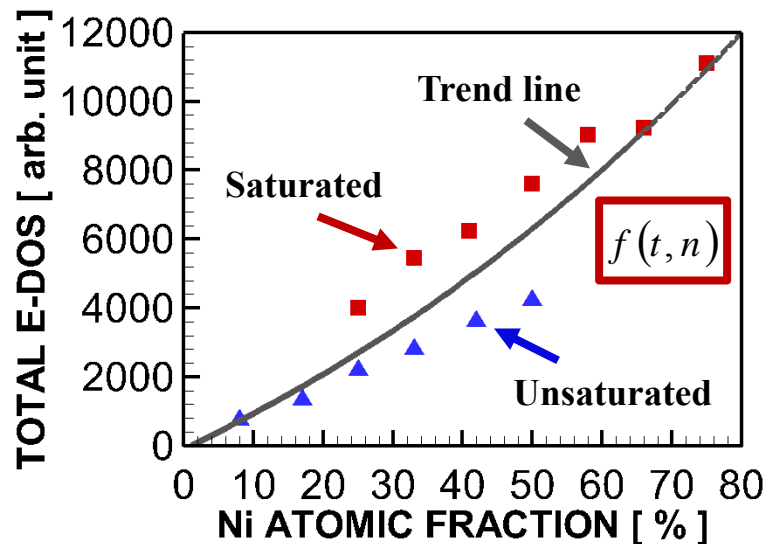
➤ Electron density of states (f-orbital)



➤ Phonon dispersion



➤ Prediction of peak tensile strength



$$\frac{T_{\max}}{T_{\text{ideal}}} = \frac{CE}{CD} \cdot \frac{1}{\Phi} \cdot f(t, n) \cdot g(w)$$

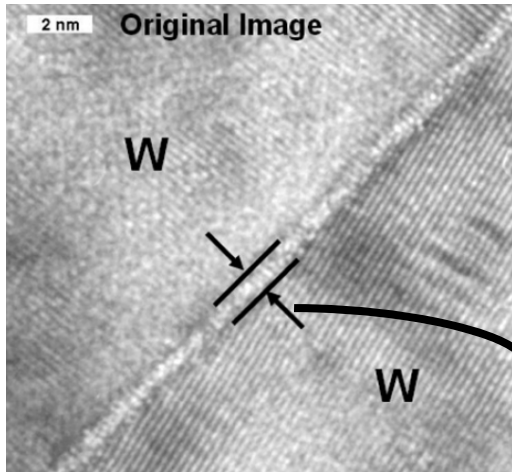
- T_{\max} : Maximum tensile strength of W-Ni alloy
- T_{ideal} : Idealistic maximum tensile strength of W
- Φ : Surface energy of W
- CE : Atomic level cohesive energy of W

How does this prediction apply to continuum scale fracture?

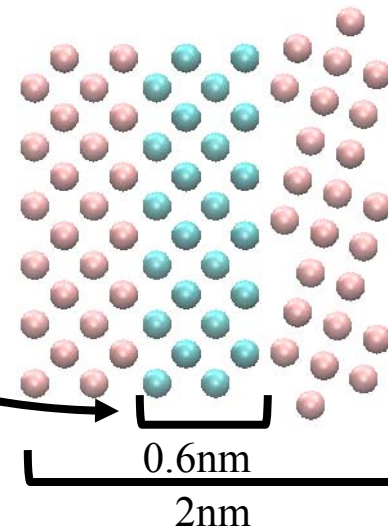


➤ Continuum scale model

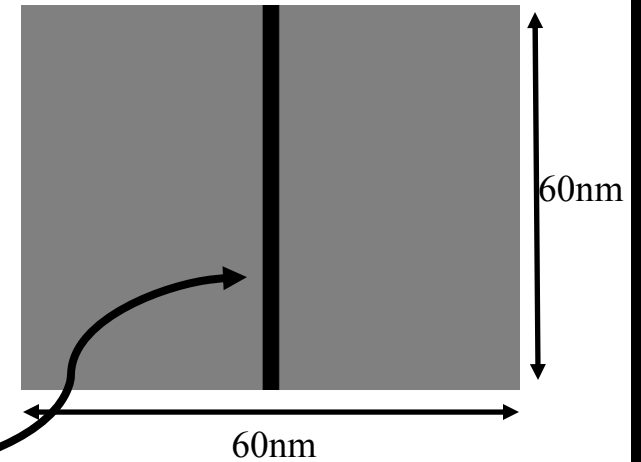
(1) Nano-scale model



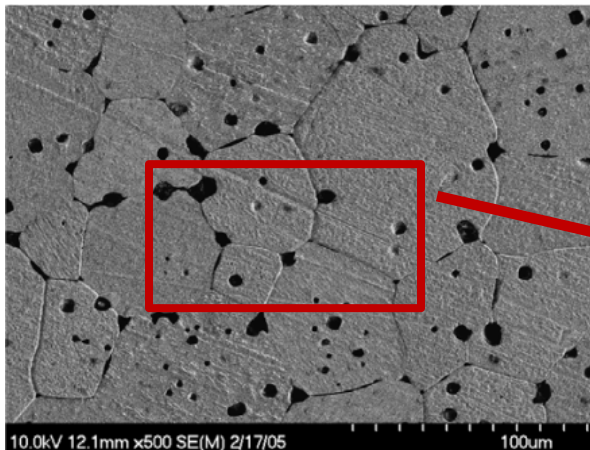
[V. Gupta et al, 2007]



Bi-granular model

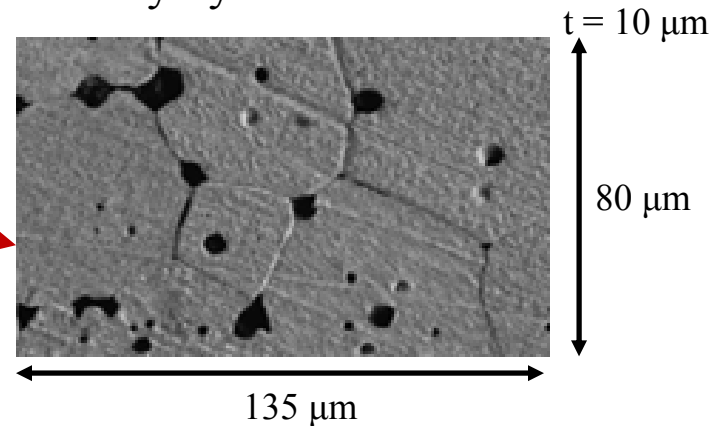


(2) Micro-scale model



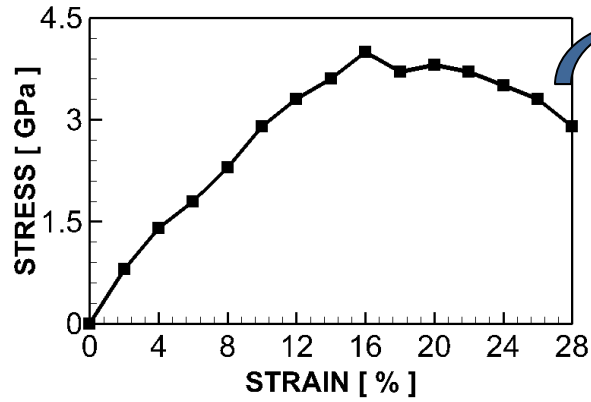
[V. Gupta et al, 2007]

Polycrystalline model

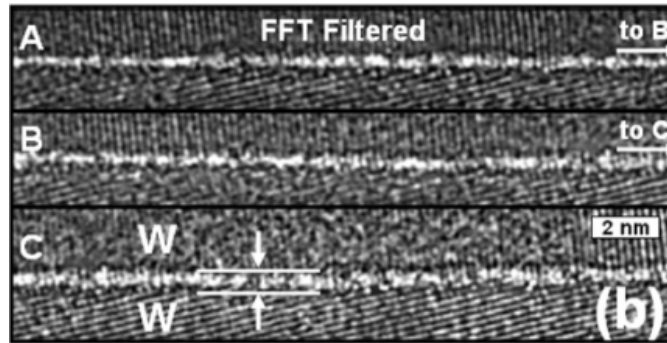
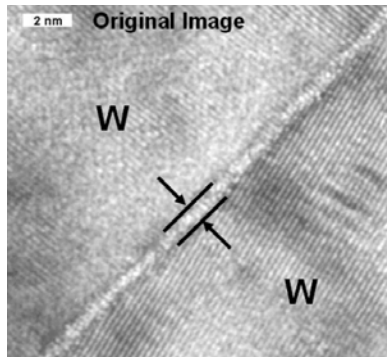
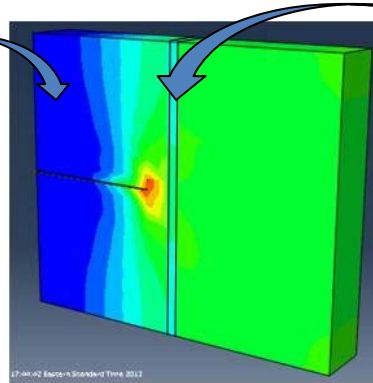
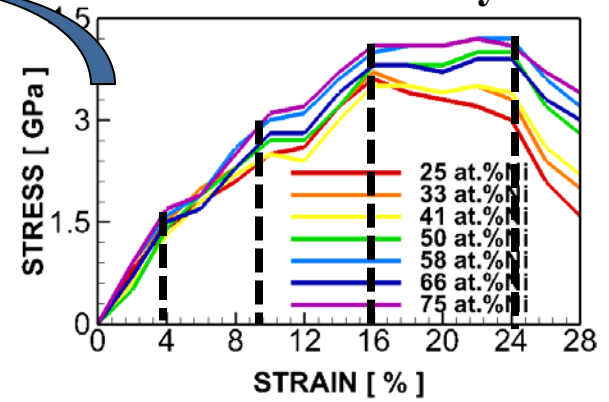


➤ Material model of grains and GBs

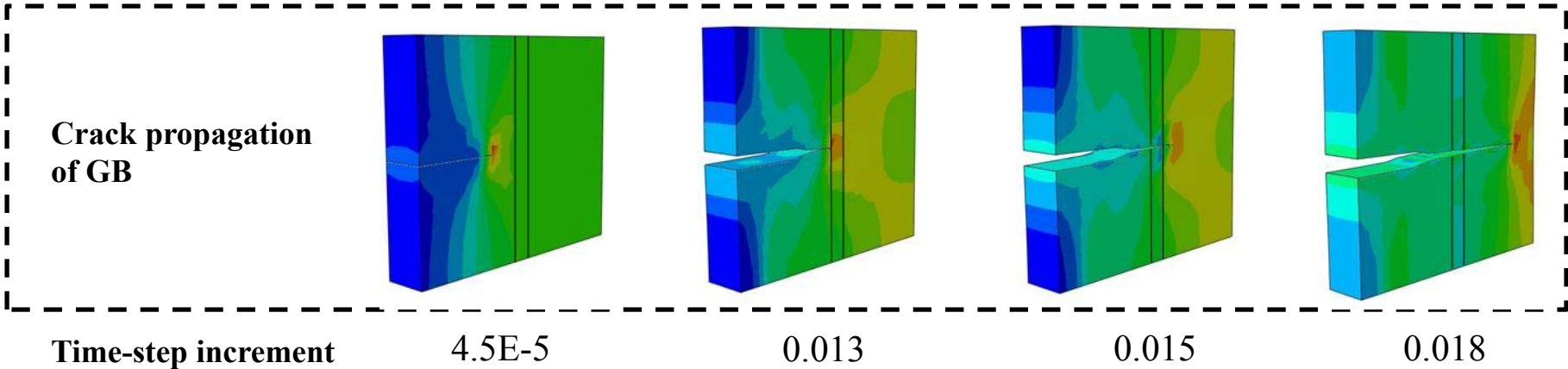
Grain



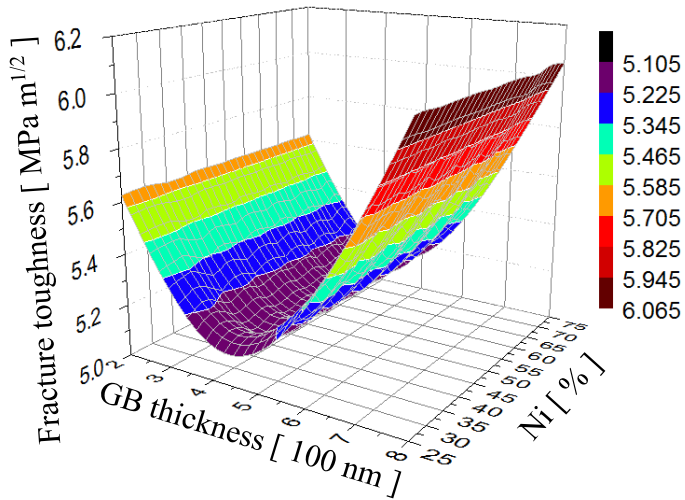
Grain boundary



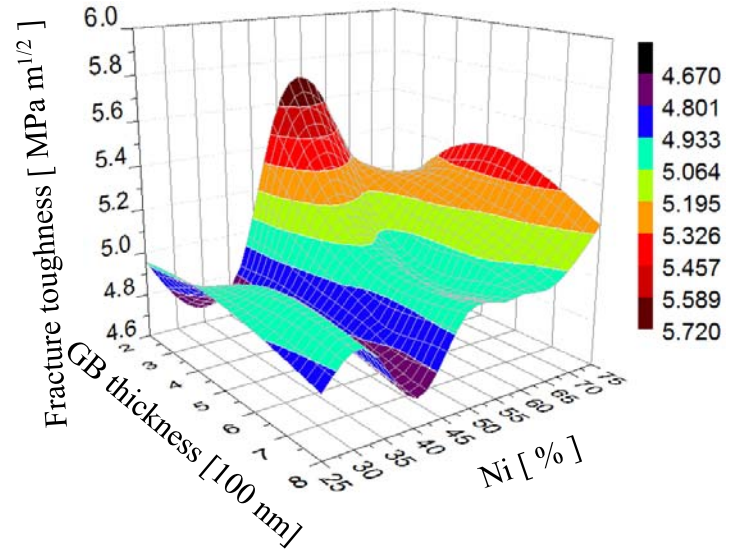
[V. Gupta et al, 2007]



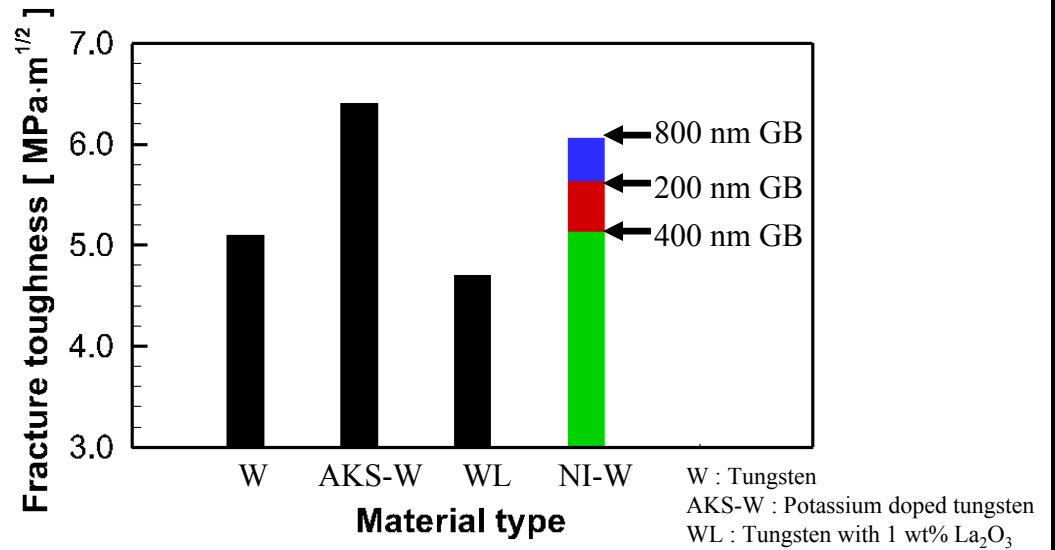
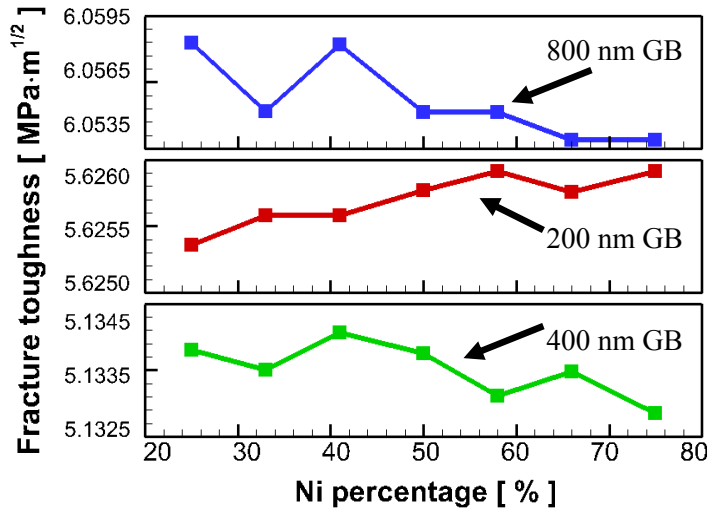
➤ Fracture toughness analysis



Fracture toughness in crack initiation

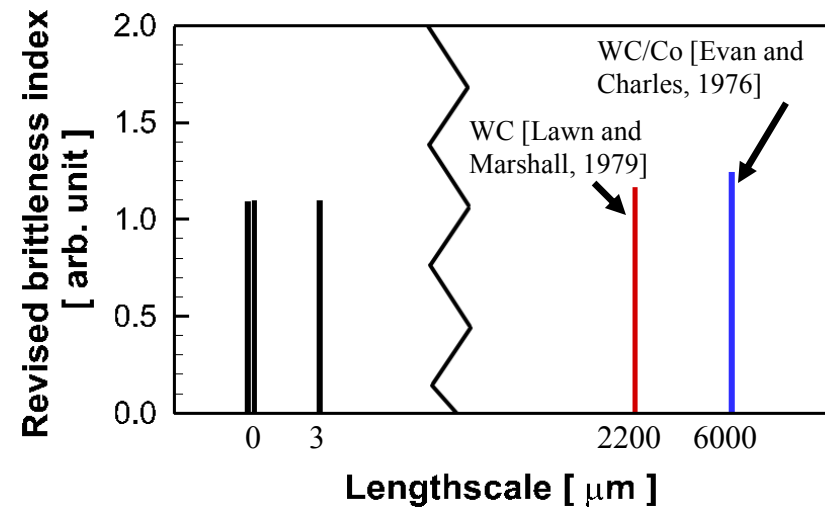
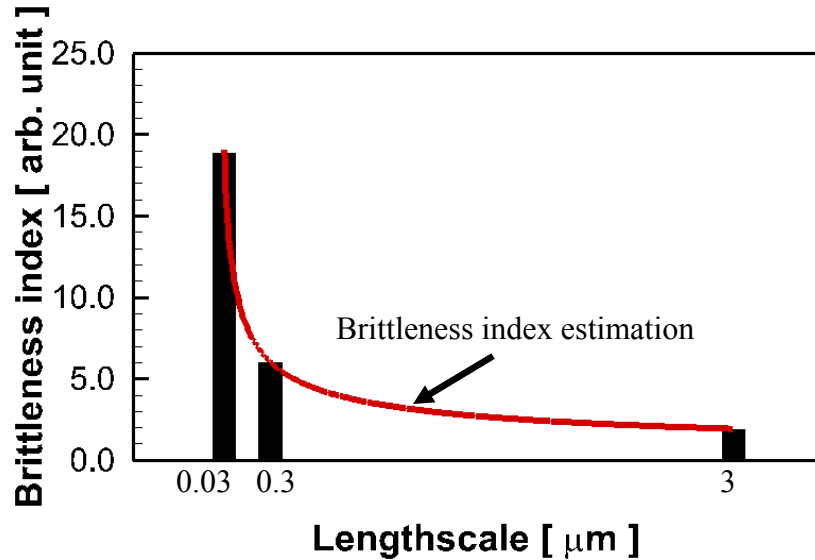


Fracture toughness inside the GB

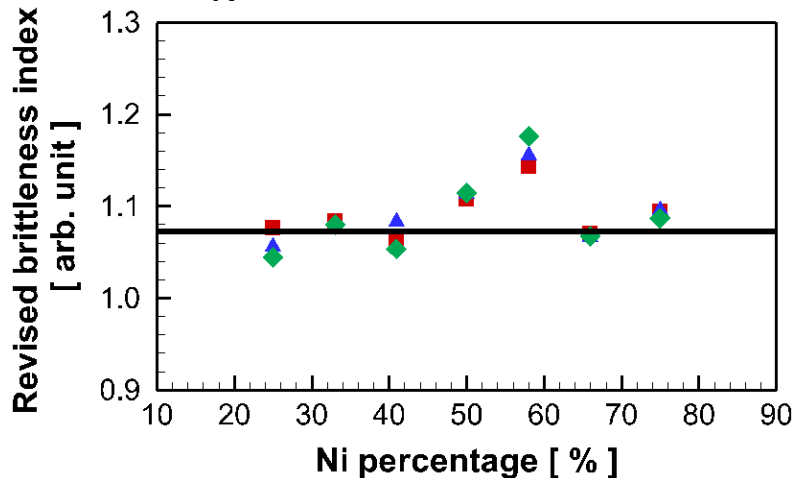


[B. Gludovatz and et al., 2010]

➤ Brittleness index of GBs



Effect of length-scale : $B = 3.3L^{-1/2}$



$$B^* = \frac{H}{K_c} \cdot \frac{1}{\alpha} \sqrt{L}$$

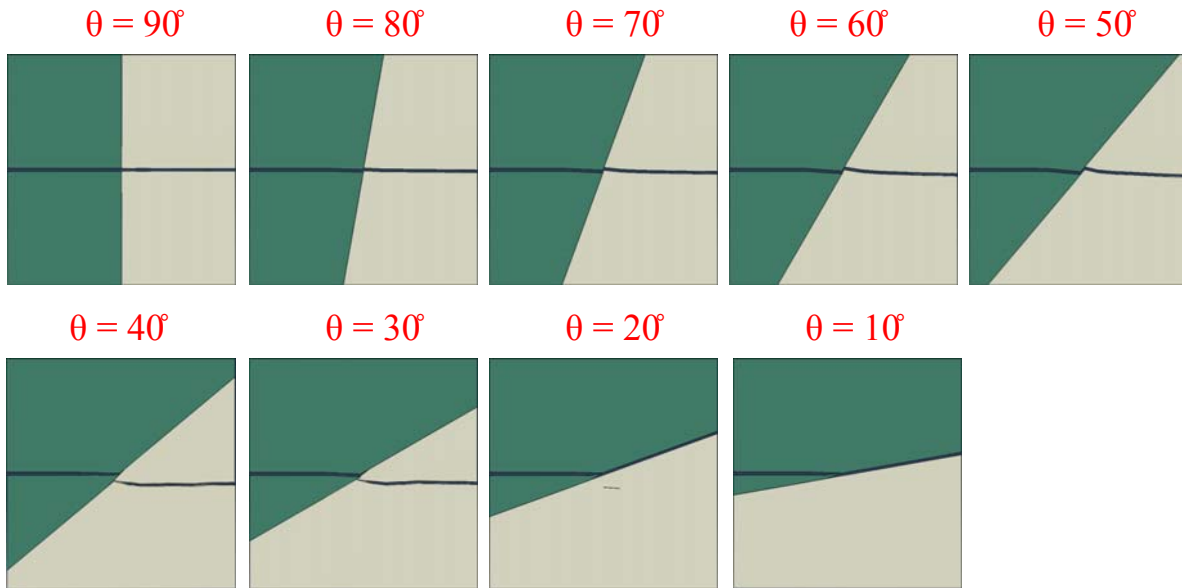
$\alpha = 3.3$ for W-Ni

Nomenclature

B^*	brittleness index (no unit)
L	lengthscale (μm)
T	max. tensile strength (fracture strength)
H	hardness (GPa)
K_c	fracture toughness ($\text{MPa m}^{1/2}$)
t	GB thickness (μm)
p	Ni fraction (no unit)

- Measurement of GB embrittlement has been obtained using the revised brittleness index.
- This provides an absolute range of qualitative measurement to describe the brittleness without considering the length scale limitations.

➤ Crack propagation in different angled GBs



- Inter-granular failure is represented as 1
- Trans-granular failure is represented as -1

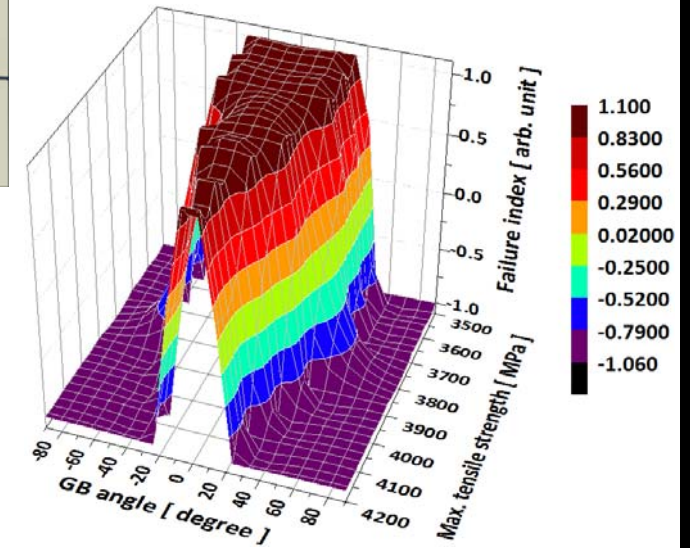
❖ **Failure index** : An index (between -1 and 1) to describe failure type, which can be either inter-granular failure or trans-granular failure.

$$FI = a + b \frac{T_{GB}}{T_{Grain}} + c \theta^2$$

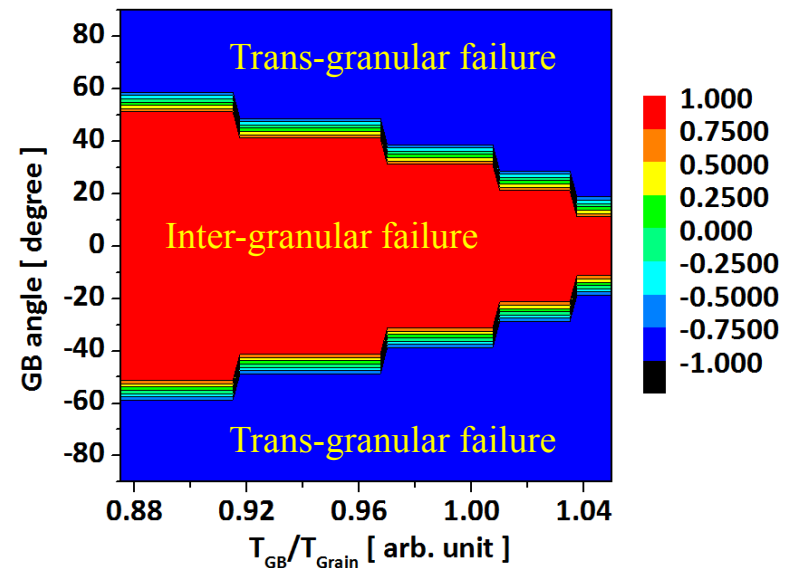
$a = 4.45$
 $b = -4.2$
 $c = -0.00024$

Using the Heaviside function

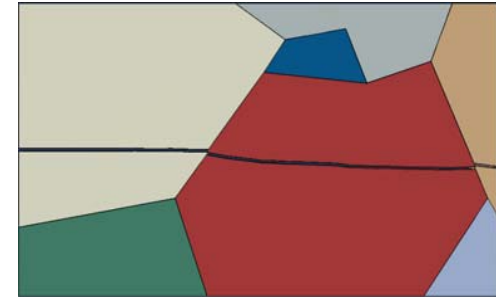
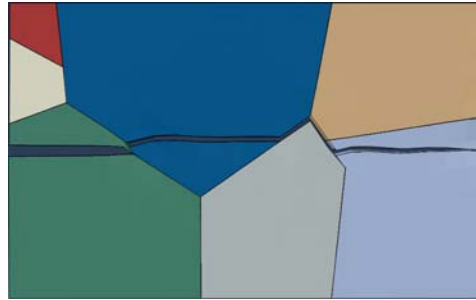
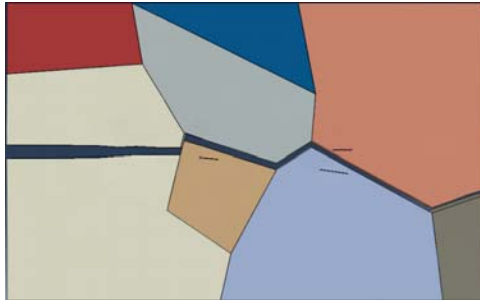
$$H[FI] = \begin{cases} 1, & FI \geq 0 \\ -1, & FI < 0 \end{cases}$$



GB angle from -90 to 90 degree



➤ Validation and Conclusion

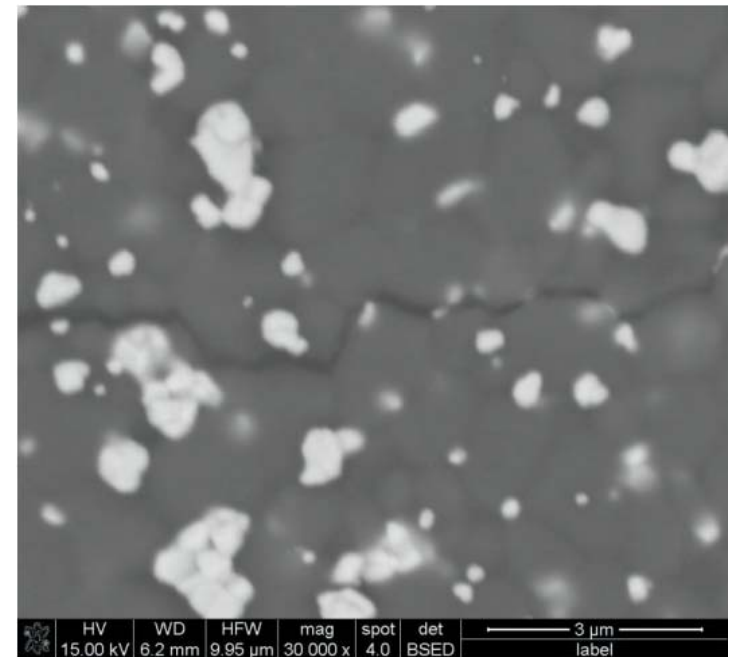


- Perfect inter-granular failure has occurred.
- Contains crack path with maximum GB angle of 67° .
- GB strength property can be predicted.

$$FI = a + b \frac{T_{GB}}{T_{Grain}} + c \theta^2$$

- According to the failure index prediction, given microstructure has max. tensile strength ratio between GB and grain as $T_{GB} \leq (0.803) \cdot T_{Grain}$.

✓ For various failed morphologies of polycrystalline W-Ni, GB's strength property can be predicted using the derived failure type criteria.

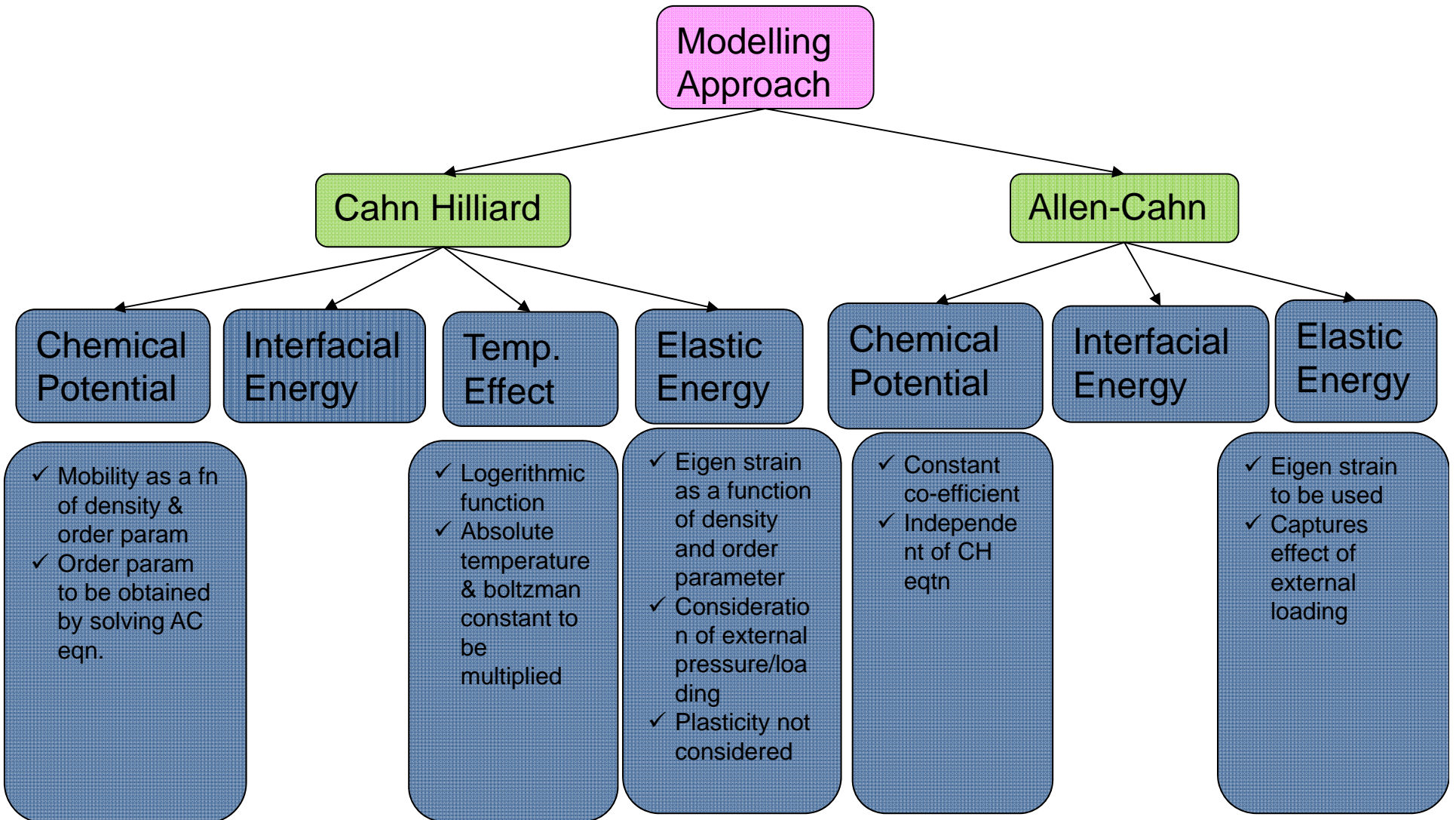


[Zbigniew Pedzich, 2012]

Evolution: Previous Works

- Microstructure evolution has been observed through experimental studies
Groza, 2000; Hong, 2003; Dahl, 2007
- Simulation developed replicating the whole sintering process
Maizza, 2007; Vanmeensel, 2005
- Kinetic Monte Carlo simulation applied to microstructural evolution: Probabilistic approach, depends on random sampling
Olevsky, 2004
- Phase field modeling has been done to identify sintering mechanisms, external loading not considered
Wang, 2006; Liu, 2011; Deng, 2012
- Consolidation kinetics has been captured experimentally
Bruson, 1984; Grigoryev, 2009; Tang, 2013

Modeling Approach



Moose Simulation

Mesh

- Rectangular grid will be created
- Corresponding Element types will assigned

Functions

- The phase field variables will be assigned
- Initial structure is created with assigned initial condition
- All the constants & their values can also be assigned in material section

Kernels

- Define the total free energy expressions, use in-built Allen-Cahn & Cahn-Hilliard equations
- Calculate derivatives & give them as input

Executioner

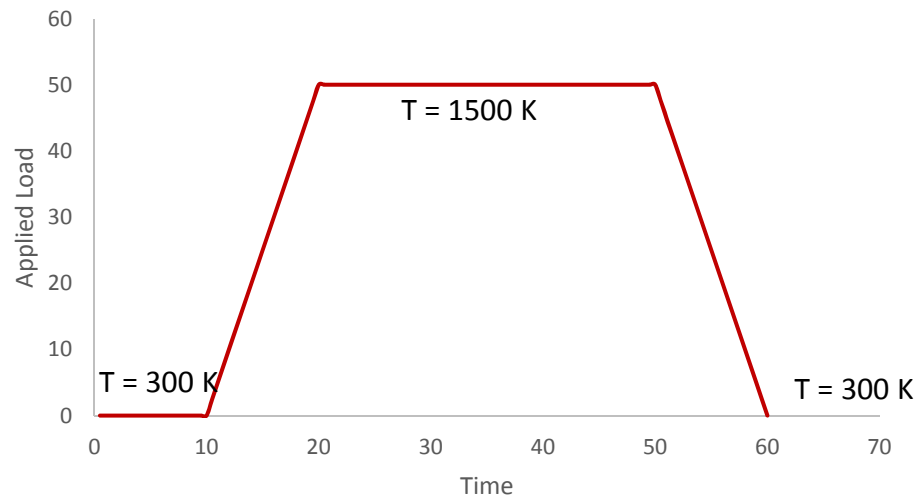
- Define solver type: Finite Difference Method
- Assign pre-conditioning if required

Post-process

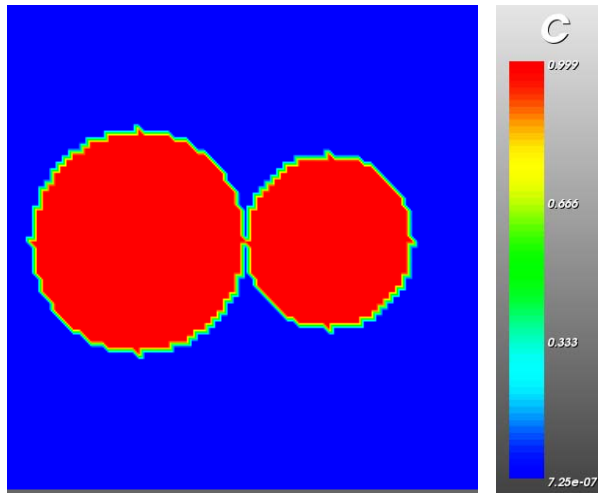
- Micro-structural images
- Plot for temporal evolution of phase field variable
- Calculate evolution of grain size

Simulation Details: Test Run

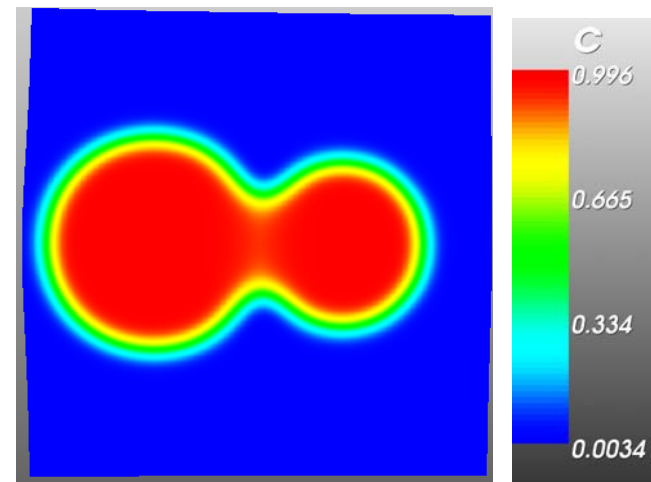
- ✓ Simulation block: 100X60; Particle Radius: 20 & 20;
- ✓ Grid Size: 0.5
- ✓ Total Time: 60 with Time Step: 1.0
- ✓ Maximum displacement applied 35 μm



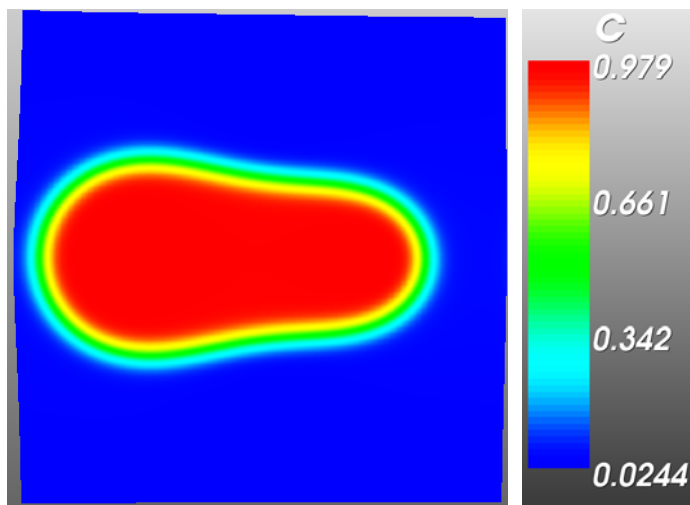
Test Results: DensityVariation w/o load



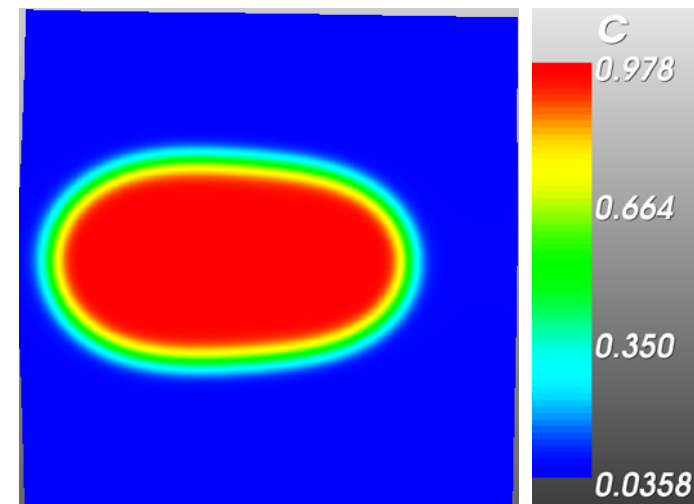
Initial Condition



Time = 0.5

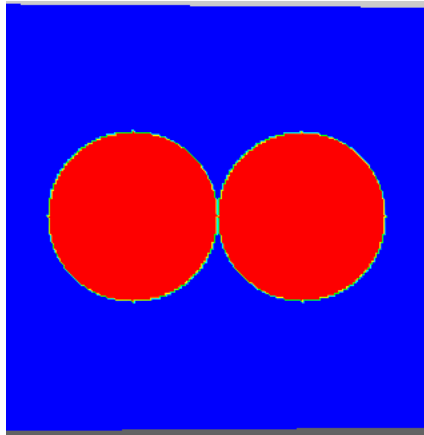


Time = 20.5

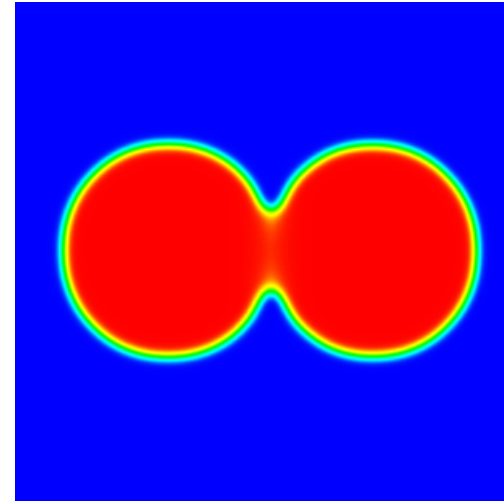


Time = 60.0

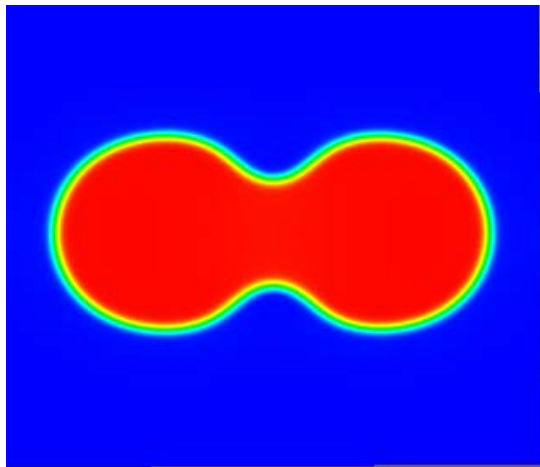
Test Results: DensityVariation w/ load



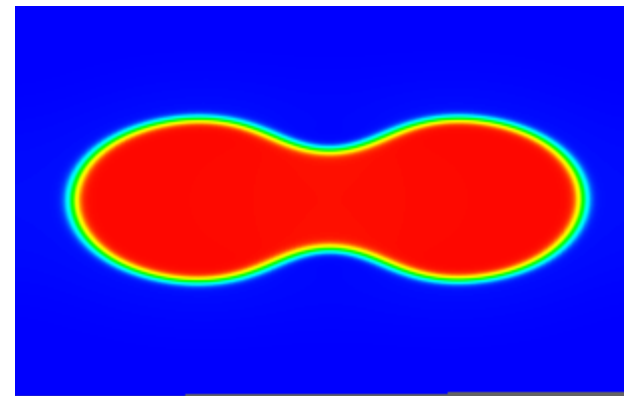
Initial Condition



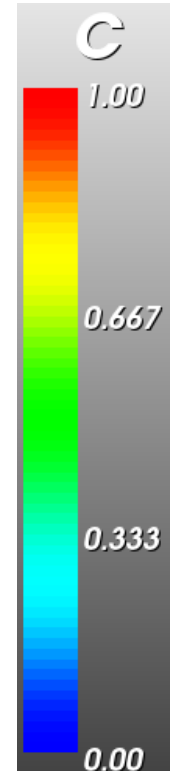
Time = 1.0



Time = 14



Time = 35.0



Summary

- All Tasks on Schedule
- A Grain Boundary Diagram Based Approach for long term GB evolution identified
- A Brittleness Index parameter identified to predict effect of GB on microstructural Strength
- Control sample manufacturing process established
- In-situ and ex-situ experimentation protocols established
- 4 international journal publications, 1 PhD graduate, 3 supported students with grant in second year