## Pulse Detonation Engine for Power Extraction from Oxy-Combustion of Coal-Based Fuels



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**Oregon State University** 

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**Collaborators:** Drs. Fred Schauer, John Hoke and team at Air Force Research Laboratory.



# Motivation

- Improvements in thermodynamic efficiency of power plants needed
- Pressure gain combustion using detonations can significantly improve efficiency



Richardson, Blunck et al., Combustion and Flame 2016

# Motivation



Advantages of detonation-fed MHD:  $P \propto \sigma imes V^2 imes B^2$ 

- High velocities (Ma > 2)
- High temperatures (T > 3000 K) increase electrical conductivity



# **Key Findings**

- 1) Particle seeder developed for unsteady detonations
- 2) Data collected for  $CH_4$ - $O_2$  detonations
- 3) Electrical conductivity measurements being collected, preliminary results indicate seeding needed
- 4) Ionization chemistry of seed particles reduces detonation speed
- 5) Detonation solver developed for oxygen-fuel combustion
- 6) Residual combustion products suppress detonations



# **Technical Objectives**

### **Overall Goal**

Develop and evaluate a pulse detonation engine system which can be coupled with a MHD system, and analyze MHD and detonation performance.

### **Specific Objectives:**

- 1) Design, build, and operate a pulse detonation engine that operates on gaseous or solid fuels with oxygen.
- 2) Evaluate the operational envelope and performance of the pulse detonation device with both seeded and unseeded flows.
- 3) Develop and use a numerical design tool to calculate the performance of pulse detonation and coupled detonation-MHD systems.



## **Progression of Research**



### **Experimental Effort**



- N<sub>2</sub>O and O<sub>2</sub> pulse detonation engines built
- Measured CH<sub>4</sub>/O<sub>2</sub> detonation speeds, added coal
- Method for injecting particles developed
- Preliminary electrical conductivity measurements
- Ongoing effort evaluating the influence of residual combustion products

Coupled MHD detonation calculations with coal particles



# Development of Pulse Detonation System



January 2018



November 2018



# CH<sub>4</sub> – O<sub>2</sub> Detonation Speeds



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# CH<sub>4</sub> – O<sub>2</sub> Detonation Speeds



### **Injection of Seed**



High speed video of particulate injection through seeder



# **Oxygen and Particle Delivery System**





High speed imaging of particle injection

# **Measuring Electrical Conductivity**

 $P \propto \sigma \times V^2 \times B^2$ 

- Detonation propagates through magnetic field
- Deflection measured by induced current in search coil
- Conductivity evaluated with relationship:



# Instrumentation to measure electrical conductivity





# **Electrical Conductivity Signal**

**Photodiode Signal** 



Oxy-methane  $\varphi \approx 1$  for all tests

## **Progression of Research**



- 2D simulations of detonation through H<sub>2</sub>-O<sub>2</sub>
- 1D simulations of hydrocarbon detonations
- 1D ionizing H<sub>2</sub>-O<sub>2</sub>-KOH model has developed and applied
- Riemann solvers initially updated to account for MHD in1D

Coupled MHD detonation calculations with coal particles



# **Detonation Solver**

 Godonov's finite volume with Conservation Laws Package (CLAWpack) 5.4.0 (Mandli et al, 2016)

$$Q_{i}^{n+1} = Q_{i}^{n} - \frac{\Delta t}{\Delta x} \left( F_{i+\frac{1}{2}}^{n} - F_{i-\frac{1}{2}}^{n} \right)$$

- Riemann approximation with Roe averaging and entropy inclusion
- Kinetics handled by Cantera 2.3.0

Cell Width = 3.2 [mm] Experimental = 2.02 [mm] (Denisov,1960)

CLAWPack DOI:10.5281/zenodo.262111,URL: <u>http://www.clawpack.org</u>

Cantera DOI:10.5281/zenodo.170284,URL: http://www.cantera.org



# **Governing Eq. for MHD/Detonation**

Mass conservation equation:

$$\frac{\partial}{\partial t} \iint_{S} \rho dS = -\int_{l} \rho \boldsymbol{u} \cdot \boldsymbol{n} dl$$

u: Gas Velocity  $\rho$ : Density p: Pressure

**B**: Magnetic Flux Density **J**: Electric Current Density

<u>Momentum conservation equation</u>: E: Total Energy  $\sigma$ : Electrical Conductivity

$$\frac{\partial}{\partial t} \iint_{S} \rho \boldsymbol{u} dS = -\int_{l} \{\rho \boldsymbol{u} (\boldsymbol{u} \cdot \boldsymbol{n}) + p\boldsymbol{n}\} dl + \int_{l} \bar{\tau} \cdot \boldsymbol{n} dl + \iint_{S} \boldsymbol{J} \times \boldsymbol{B} dS$$

Total energy conservation equation:

$$\frac{\partial}{\partial t} \iint_{S} \rho E dS = -\int_{l} (\rho E \boldsymbol{u} \cdot \boldsymbol{n} + p \boldsymbol{u} \cdot \boldsymbol{n}) dl + \int_{l} (\bar{\tau} \cdot \boldsymbol{u}) \cdot \boldsymbol{n} dl + \iint_{S} \left\{ \frac{\boldsymbol{J}^{2}}{\sigma} + \boldsymbol{u} \cdot (\boldsymbol{J} \times \boldsymbol{B}) \right\} dS$$

Here,  $E = \sum_{s=1}^{N_{sp}} Y_s(h_{298}^{0} + \int_{T'=298 \text{ K}}^{T} c_p^0 \text{d}T') - p/\rho + \frac{1}{2} |\boldsymbol{u}|^2$ 

Mass conservation equation of Chemical Species:

$$\frac{\partial}{\partial t} \iint_{S} \rho Y_{S} dS = -\int_{l} \rho Y_{S} \boldsymbol{u} \cdot \boldsymbol{n} dl + \iint_{S} \rho \dot{Y}_{S} dS$$
Charge Neutrality Equation  $\frac{Y_{e}}{m_{e}} = \sum_{i} \frac{Y_{ion}}{m_{ion}}$ 

*h*: Specific Enthalpy  $Y_s$ : Mass Concentration  $\dot{Y}_s$ : Mass Production Rate  $c_p$ : Specific Heat at Constant Pressure



## **Governing Equations in Electrodynamics**

<u>Generalized Ohm's Law</u>  $\boldsymbol{j} = \sigma(\boldsymbol{E} + \boldsymbol{u} \times \boldsymbol{B}) - \frac{\beta}{|\boldsymbol{B}|} \boldsymbol{j} \times \boldsymbol{B}$ 

j: Electric Current Density E: Electric Field

Electrical Conductivity  $\sigma = \frac{e^2 n_e}{m_e \sum_{i=1}^{N_{sp}} v_{ei}}$ 

Hall Parameter  $\beta = \frac{e|B|}{m_e \sum_{i=1}^{N_{sp}} v_{ei}}$ 

Collision Frequency of Electron with Species  $v_{ei} = n_i Q_{ei} c_e$ 

Steady Maxwell Equations

$$\nabla \times \boldsymbol{E} = \boldsymbol{0}$$
$$\nabla \cdot \boldsymbol{j} = \boldsymbol{0}$$

**u**: Gas Velocity **B**: Magnetic Flux Density

e: Elementary Charge  $n_e:$  Electron Number Density  $m_e:$  Electron Mass  $n_i:$  Species Number Density  $Q_{ei}:$  Electron Collision Cross Section with Species  $c_e:$  Electron Mean Thermal Speed



## **Electrical Conductivity**



19 Calculated electrical conductivity



## **Ionization Mechanism**

		•			
#	Reaction	Rate coeffic	ients ( $A$	, n, E)	Reference
57	$\mathrm{KO} + \mathrm{CO} = \mathrm{K} + \mathrm{CO}_2$	$1.00  imes 10^{14}$	0.0	0.0	[59]
58	$\mathrm{KO} + \mathrm{HCO} = \mathrm{KOH} + \mathrm{CO}$	$3.00  imes 10^{13}$	0.0	0.0	[45]
59	$\mathrm{KO} + \mathrm{CH}_4 = \mathrm{KOH} + \mathrm{CH}_3$	$1.20  imes 10^{12}$	0.0	14.64	[60]
60	$\rm KO + CH_2O = KOH + HCO$	$1.20 \times 10^{13}$	0.0	16.74	[45]
61	$\mathrm{KO} + \mathrm{KO} = \mathrm{KO}_2 + \mathrm{K}$	$1.00  imes 10^{13}$	0.0	0.0	[61]
62	$\mathrm{KO} + \mathrm{H} + \mathrm{M}_k = \mathrm{KOH} + \mathrm{M}_k$	$3.60  imes 10^{22}$	-2.0	0.0	[60]
63	$\mathrm{KO} + \mathrm{O} + \mathrm{M}_k = \mathrm{KO}_2 + \mathrm{M}_k$	$1.45  imes 10^{19}$	-1.0	0.0	[60]
64	$\mathrm{KO} + \mathrm{CH}_3 = \mathrm{K} + \mathrm{CH}_3\mathrm{O}$	$2.30  imes 10^{13}$	0.0	25.1	[45]
65	$\mathrm{KO} + \mathrm{C}_2\mathrm{H}_6 = \mathrm{KOH} + \mathrm{C}_2\mathrm{H}_5$	$1.20  imes 10^{13}$	0.0	25.1	[45]
66	$\mathrm{KO} + \mathrm{C}_2\mathrm{H}_4 = \mathrm{KOH} + \mathrm{C}_2\mathrm{H}_3$	$1.50 \times 10^{13}$	0.0	33.47	[45]
67	$\mathrm{KO} + \mathrm{C}_2\mathrm{H}_2 = \mathrm{KOH} + \mathrm{C}_2\mathrm{H}$	$2.00 \times 10^{13}$	0.0	37.66	[45]
68	$\mathrm{KO} + \mathrm{C}_3\mathrm{H}_8 = \mathrm{KOH} + \mathrm{C}_3\mathrm{H}_7$	$1.50  imes 10^{13}$	0.0	20.92	[45]
KC	D <sub>2</sub> reactions				
69	$\mathrm{KO}_2 + \mathrm{H} = \mathrm{KO} + \mathrm{OH}$	$2.21  imes 10^{12}$	0.5	0.0	[50]
70	$\mathrm{KO}_2 + \mathrm{H} = \mathrm{K} + \mathrm{HO}_2$	$1.90  imes 10^{12}$	0.0	0.0	[61]
71	$\mathrm{KO}_2 + \mathrm{H} = \mathrm{KOH} + \mathrm{O}$	$1.00  imes 10^{13}$	0.0	0.0	[61]
72	$\mathrm{KO}_2 + \mathrm{H} = \mathrm{KO} + \mathrm{OH}$	$5.00 \times 10^{13}$	0.0	29.29	[45]
73	$\mathrm{KO}_2 + \mathrm{O} = \mathrm{KO} + \mathrm{O}_2$	$1.30  imes 10^{13}$	0.0	0.0	[45]
74	$\mathrm{KO}_2 + \mathrm{CO} = \mathrm{KO} + \mathrm{CO}_2$	$6.00 \times 10^{13}$	0.0	96.23	[60]
75	$\mathrm{KO}_2 + \mathrm{OH} = \mathrm{KOH} + \mathrm{O}_2$	$1.20  imes 10^{13}$	0.0	0.0	[60]
76	$\mathrm{KO}_2 + \mathrm{H}_2 = \mathrm{KOH} + \mathrm{OH}$	$1.80  imes 10^{12}$	0.0	83.14	[60]
77	$\mathrm{KO}_2 + \mathrm{HCO} = \mathrm{KOH} + \mathrm{CO}_2$	$6.00  imes 10^{12}$	0.0	0.0	[60]
78	$\mathrm{KO}_2 + \mathrm{CH}_3 = \mathrm{KOH} + \mathrm{CH}_2\mathrm{O}$	$6.00 \times 10^{12}$	0.0	0.0	[60]
KC	OH reactions				
79	$\mathrm{KOH} + \mathrm{H} = \mathrm{K} + \mathrm{H_2O}$	$2.21 \times 10^{12}$	0.5	0.0	[50]
80	$\mathrm{KOH} + \mathrm{CH}_3 = \mathrm{K} + \mathrm{CH}_3\mathrm{OH}$	$3.50 \times 10^{12}$	0.0	41.84	[45]
81	$\mathrm{KOH} + \mathrm{HO}_2 = \mathrm{KO}_2 + \mathrm{H}_2\mathrm{O}$	$6.00  imes 10^{12}$	0.0	22.18	[60]
82	$\text{KOH} + \text{KOH} = (\text{KOH})_2$	$8.00  imes 10^{13}$	0.0	0.0	[57]
KF	I reactions				
83	$\mathrm{KH} + \mathrm{H} = \mathrm{K} + \mathrm{H}_2$	$1.00 \times 10^{14}$	0.0	0.0	[56]
84	$\rm KH + O = K + OH$	$5.00 \times 10^{13}$	0.0	0.0	[56]
85	$\rm KH + O = \rm KO + H$	$6.00  imes 10^{12}$	0.0	29.29	[45]
86	$\mathrm{KH} + \mathrm{OH} = \mathrm{K} + \mathrm{H_2O}$	$1.00  imes 10^{14}$	0.0	0.0	[59]
87	$\mathrm{KH} + \mathrm{OH} = \mathrm{KOH} + \mathrm{H}$	$1.00  imes 10^{13}$	0.0	0.0	[59]

#	Reaction	Rate coefficients $(A, n, E)$			Reference
88	$\rm KH + HCO = \rm K + \rm CH_2O$	$2.00  imes 10^{13}$	0.0	0.0	[45]
89	$\rm KH + CH_3 = CH_4 + K$	$1.00  imes 10^{14}$	0.0	0.0	[45]
90	$\rm KH + CH_3O = \rm K + CH_3OH$	$2.00  imes 10^{13}$	0.0	0.0	[45]
91	KH + KO = K + KOH	$1.00  imes 10^{14}$	0.0	0.0	[59]
$K_2$	O reactions				
92	$\mathrm{KO} + \mathrm{K} + \mathrm{M} = \mathrm{K}_2\mathrm{O} + \mathrm{M}$	$1.00\times10^{16}$	0.0	0.0	[45]
93	$K_2O + H = K + KOH$	$5.00  imes 10^{12}$	0.0	12.55	[45]
94	$\mathbf{K}_{2}\mathbf{O}+\mathbf{O}=\mathbf{K}_{2}\mathbf{O}_{2}$	$1.00  imes 10^{14}$	0.0	0.0	[45]
95	$\mathbf{K}_{2}\mathbf{O}+\mathbf{O}=\mathbf{K}\mathbf{O}+\mathbf{K}\mathbf{O}$	$1.00  imes 10^{13}$	0.0	41.84	[45]
96	$K_2O + OH = KO + KOH$	$1.00\times10^{13}$	0.0	20.92	[45]
KO	3 reactions				
97	$\mathrm{KO}_2 + \mathrm{O} + \mathrm{M}_k = \mathrm{KO}_3 + \mathrm{M}_k$	$1.45  imes 10^{19}$	-1.0	0.0	[60]
98	$\rm H + \rm KO_3 = \rm KO_2 + \rm OH$	$2.00  imes 10^{13}$	0.0	0.0	[45]
99	$O + KO_3 = KO_2 + O_2$	$2.00  imes 10^{13}$	0.0	0.0	[45]
100	$\mathrm{OH} + \mathrm{KO}_3 = \mathrm{KO}_2 + \mathrm{HO}_2$	$1.00\times10^{13}$	0.0	37.66	[45]
101	$\mathrm{CH}_3 + \mathrm{KO}_3 = \mathrm{CH}_3\mathrm{O} + \mathrm{KO}_2$	$1.00  imes 10^{13}$	0.0	20.92	[45]
102	$\mathrm{KO} + \mathrm{O}_2 + \mathrm{M}_k = \mathrm{KO}_3 + \mathrm{M}_k$	$3.40\times10^{14}$	0.0	0.0	[45]
KH	CO <sub>3</sub> , KCO <sub>3</sub> , K <sub>2</sub> CO <sub>3</sub> reactions				
103	$\mathrm{KOH} + \mathrm{CO}_2 + \mathrm{M}_k = \mathrm{KHCO}_3 + \mathrm{M}_k$	$4.09\times10^{14}$	0.0	0.0	[45]
104	$\mathrm{KO} + \mathrm{CO}_2 + \mathrm{M} = \mathrm{KCO}_3 + \mathrm{M}$	$3.90  imes 10^{14}$	0.0	0.0	[45]
105	$\mathrm{KCO}_3 + \mathrm{H} + \mathrm{M}_k = \mathrm{KHCO}_3 + \mathrm{M}_k$	$2.00\times10^{16}$	0.0	0.0	[45]
106	$\mathrm{KO}_2 + \mathrm{CO} + \mathrm{M} = \mathrm{KCO}_3 + \mathrm{M}$	$3.00  imes 10^{16}$	0.0	0.0	[45]
107	$\mathbf{K} + \mathbf{K}\mathbf{C}\mathbf{O}_3 + \mathbf{M}_k = \mathbf{K}_2\mathbf{C}\mathbf{O}_3 + \mathbf{M}_k$	$2.00\times10^{18}$	0.0	0.0	[45]
108	$\mathrm{KHCO}_3 + \mathrm{H} = \mathrm{K} + \mathrm{CO}_2 + \mathrm{H}_2\mathrm{O}$	$2.70 \times 10^{13}$	0.0	29.83	[58]
109	$\mathrm{KHCO}_3 + \mathrm{H} = \mathrm{KCO}_3 + \mathrm{H}_2$	$1.50\times10^{13}$	0.0	41.84	[45]
110	$\mathrm{KHCO}_3 + \mathrm{O} = \mathrm{KCO}_3 + \mathrm{OH}$	$1.00  imes 10^{13}$	0.0	52.3	[45]
111	$\mathrm{KHCO}_3 + \mathrm{OH} = \mathrm{KCO}_3 + \mathrm{H}_2\mathrm{O}$	$2.00\times10^{13}$	0.0	31.38	[45]
112	$\mathrm{KCO}_3 + \mathrm{H} = \mathrm{KOH} + \mathrm{CO}_2$	$3.00  imes 10^{12}$	0.0	16.74	[45]
113	$\mathrm{KCO}_3 + \mathrm{O} = \mathrm{KO}_2 + \mathrm{CO}_2$	$5.00 \times 10^{12}$	0.0	12.55	[45]
114	$\mathrm{KHCO}_3 + \mathrm{KO} = \mathrm{K}_2\mathrm{CO}_3 + \mathrm{OH}$	$6.00 \times 10^{12}$	0.0	29.29	[45]
115	$\mathrm{KHCO}_3 + \mathrm{KOH} = \mathrm{K}_2\mathrm{CO}_3 + \mathrm{H}_2\mathrm{O}$	$3.00\times10^{12}$	0.0	37.66	[45]
116	$\mathrm{KCO}_3 + \mathrm{KO} = \mathrm{K}_2\mathrm{CO}_3 + \mathrm{O}$	$7.00\times10^{12}$	0.0	20.92	[45]
117	$\mathrm{KCO}_3 + \mathrm{KO}_2 = \mathrm{K}_2\mathrm{CO}_3 + \mathrm{O}_2$	$1.00\times10^{13}$	0.0	12.55	[45]
118	$K_2CO_3 + M_k = K_2O + CO_2 + M_k$	$5.00 \times 10^{16}$	0.0	338.9	[45]

**Zaiger, 2019** 20



# **Detonation Speeds with 0.01% K<sub>2</sub>CO<sub>3</sub>**



- Up to an 8% decrease in the detonation speed
- Decrease in power



# **Progression of Research**

- Multi-species & multi-step reacting flow CESE solver
- Fully implicit & dual time stepping source term for stiff chemistry
- Oxy-fuel detonation simulation
- 2D solver framework



# CH<sub>4</sub>–O<sub>2</sub> Detonation: JLR mechanism

- Detonation propagation in CH<sub>4</sub>/O<sub>2</sub> mixtures
- Modified JL-R mechanism
  - Chemical kinetics for a multistep, Arrhenius-type chemical reaction for nine species: CH<sub>4</sub>, O<sub>2</sub>, H<sub>2</sub>, CO<sub>2</sub>, CO, OH, H, O and H<sub>2</sub>O adopted

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No	Reaction	Reaction Kinetics
1	$CH_4 + 0.5O_2 \longrightarrow CO + 2H_2$	$r_1 = 3.06.10^{11} \exp\left(\frac{-30000}{RT}\right) [CH_4]^{0.5} [O_2]^{1.30}$
2	$CH_4 + H_2O \longrightarrow CO + 3H_2$	$r_2 = 3.84.10^9 \exp\left(\frac{-30000}{RT}\right) [CH_4][H_2O]$
3	$CO + H_2O \Longrightarrow CO_2 + H_2$	$r_3 = 2.01.10^9 \exp\left(\frac{-20000}{RT}\right)$ [CO][H <sub>2</sub> O]
4	$H_2 + 0.5O_2 \Longrightarrow H_2O$	$r_4 = 8.03.10^{16} T^{-1} \exp\left(\frac{-40000}{RT}\right) [\text{H}_2]^{0.3} [\text{O}_2]^{1.55}$
5	$O_2 \rightleftharpoons 2O$	$r_5 = 1.5.10^9 \exp\left(\frac{-113000}{RT}\right) [O_2]$
6	$H_2O \Longrightarrow H + OH$	$r_6 = 2.3.10^{22} T^{-3} \exp\left(\frac{-120000}{RT}\right) [\text{H}_2\text{O}]$

- Radical dissociation accounted in modified JL-R mechanism
- Critical in appropriately limiting heat release during oxycombustion, thereby predicting detonation temperature and velocity accurately



### $CH_4 - O_2$ Detonation ( $\Phi = 1$ )





**Oregon State University** 

## CH<sub>4</sub>–O<sub>2</sub> Detonation: Comparison with Experimental Data





## Conservation Element Solution Element (CESE) Numerical Method Basics

- Flux conservation over discretized space-time domain – not just along spatial domain as in traditional FV method
- Staggered integration volumes (CE) and solution volumes (SE)
  - Riemann solution not needed
- Genuine multi-dimensional formulation
  - No dimensional/directional splitting necessary
  - Applicable to unstructured grids
- Non-dissipative baseline "a-scheme"
  - Numerical dissipation added as necessary



### Vortex in a Box

# Hermann, 2005Current 2D CE/SE SolverT=0T=1T=20T=1T=200064x6400<td



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### **Evaluation of CESE 2D Solver**





# **Key Findings**

$$P \propto \sigma \times V^2 \times B^2$$

- 1) Particle seeder developed for unsteady detonations
- 2) Data collected for  $CH_4$ - $O_2$  detonations
- 3) Electrical conductivity measurements being collected, preliminary results indicate seeding needed
- 4) Ionization chemistry of seed particles reduces detonation speed
- 5) Detonation solver developed for oxygen-fuel combustion
- 6) Residual combustion products suppress detonations



## **Future Work**









# **Detonation Initiation Studies**

 Effect of driver shock pressure and temperature on detonation initiation was studied to establish operational envelope for CH<sub>4</sub>–O<sub>2</sub> detonations

	P <sub>driver</sub> (atm)	$T_{driver} = 3000$ (K)	$T_{driver} = 250$ (K)	$\begin{array}{c} 0  T_{driver} = 200 \\ (\text{K}) \end{array}$	0
	60	$\checkmark$	$\checkmark$	$\checkmark$	
	45	$\checkmark$	$\checkmark$	$\checkmark$	
	30	$\checkmark$	$\checkmark$	$\checkmark$	
	15	×	×	×	
P <sub>driver</sub> (atm)	T <sub>driver</sub> (K)	$L_{driver} = 0.2$ (cm)	$L_{driver} = 0.1$ (cm)	$L_{driver} = 0.05$ (cm)	$L_{driver} = 0.005$ (cm)
60	3000	$\checkmark$	$\checkmark$	$\checkmark$	$\checkmark$
45	3000	$\checkmark$	$\checkmark$	$\checkmark$	$\checkmark$



## **Detonations with Coal**



23k frames per second with  $0.3 \ \mu s$  integration time



### **CESE Solver Validation (ZND Detonation)**

- ZND Detonation Propagation in a Tube
- Arrhenius-type chemical reaction for two species (reactant & product)

 $Reactant(R) \rightarrow Product(P) + heat release(q)$ 

- 20cm tube filled with premixed stochiometric  $H_2/O_2$  reactant mixture
- 0.2 cm spark region placed near closed head end to initiate detonation
- Validated against ZND theory and with Wu, 2002





### **CESE Solver Validation (ZND Detonation)**



### $H_2$ -Air and $CH_4$ – $O_2$ Detonation comparison

- Temperature higher in  $CH_4$ - $O_2$  detonation than  $H_2$ -Air detonation
  - Consistent with expectation of oxy-fuel combustion.
  - Higher temperature and high detonation wave velocity should result in more power extraction for MHD unit
- WD scheme over predicts combustion temperature as result of not accounting for dissociation reactions
- At temperatures higher than 2500 K (which are very common in oxy-fuel combustion), the CO-CO<sub>2</sub> equilibrium is in favor of CO



## Governing Equations for 1D Reacting Flows

Conservation equations for chemically reacting system involving  $\ensuremath{\mathsf{N}_{\mathsf{s}}}$ 

species

$$\frac{\partial Q}{\partial t} + \frac{\partial E}{\partial x} = S$$

$$Q = \begin{bmatrix} \rho \\ \rho u \\ \rho e_t \\ C_1 \\ C_2 \\ \vdots \\ C_{N_{s-1}} \end{bmatrix}, E = \begin{bmatrix} \rho u \\ \rho u^2 + p \\ \rho u \left( e_t + \frac{p}{\rho} \right) \\ u C_1 \\ u C_2 \\ \vdots \\ u C_{N_{s-1}} \end{bmatrix}, S = \begin{bmatrix} 0 \\ 0 \\ \omega_1 \\ \omega_2 \\ \vdots \\ \omega_{N_{s-1}} \end{bmatrix}$$
$$e_t = e + \frac{1}{2}u^2$$
$$e_t = e + \frac{1}{2}u^2$$
$$\rho e = \sum_{i=1}^{N_s} C_i \left( \int_{T_{ref}}^T C_{pi} dt + h_{fi}^0 \right) - p$$
$$\dot{\omega}_j = M W_j \sum_{i=1}^{N_s} \left( v_{ij}'' - v_{ij}' \right) \left( k_{fi} \prod_{l=1}^N n_l^{v_{ij}'} - k_{bi} \prod_{l=3}^N n_l^{v_{ij}'} \right)$$

- $\rho = density$
- u = velocity

 $C_i = species mass concentration$ 

p = pressure

 $\dot{\omega}_i = mass \ production \ rate \ of \ ith$ species per unit volume

 $n_j = molar \ concentration \ of \ species \ j$ 

 $k_{fi} = forward reaction rate$ 

 $k_{bi} = backward reaction rate$ 

 $v_{ij}^{\prime\prime}$  and  $v_{ij}^{\prime}$  = stochiometric coefficients



# **CESE 1D Solver Features**

- Solver implements well known a-α numerical scheme
  - To accurately resolve flow discontinuities such a shock waves
- Courant Number insensitive scheme
  - To decrease numerical diffusion at low courant numbers
- Fully-implicit source term implemented
  - Dual time stepping for stiff source terms



# H<sub>2</sub>-Air Detonation

- Detonation propagation in H<sub>2</sub>/Air mixtures
- Chemical kinetics for a global, 1 step reversible, Arrhenius-type chemical reaction for four species: H<sub>2</sub>, O<sub>2</sub>, N<sub>2</sub> and H<sub>2</sub>O adopted

$$2H_2 + O_2 \leftrightarrow 2H_2O$$
  
 $k_f = A_f \exp\left(\frac{-T_f}{T}\right)$   
 $A_f = 1.102 \times 10^{13} \ \frac{1}{sec}, T_f = 8052 \ K$ 



20cm



### H<sub>2</sub>-Air Detonation Results



# **Oxy-Fuel Reduced Kinetics**

### Westbrook-Dryer (WD)

- Widely used for turbulent flame combustion modeling with air
- No dissociation reactions accounted, hence over predicts adiabatic flame temperature

### Jones-Lindstedt revised (JL-R)

• Accounts O<sub>2</sub> dissociation; accurate prediction of adiabatic flame temperature

### JL-R Mechanism

- 1)  $CH_4 + 0.5 O_2 \rightarrow CO + 2H_2$
- 2)  $CH_4 + H_2O \rightarrow CO + 3H_2$
- 3)  $CO + H_2O \leftrightarrow CO_2 + H_2$
- 4)  $H_2 + 0.5 O_2 \leftrightarrow H_2 O$
- *5)*  $0_2 \leftrightarrow 20$

6)  $H_2 0 \leftrightarrow H + 0H$ 



# CH<sub>4</sub>-O<sub>2</sub> Detonation Results



# Use of Coal for Detonations

- Coal abundant resource in United States (and funding specific to its use)
- Prior (limited) research has considered detonations coupled with MHD for gaseous fuels
- Most research investigating coal detonations has focused on safety
- Physical and thermal properties of coal detonations need to be measured to understand coupling with MHD

Anthracite coal, picture courtesy of Wikipedia





## **Overview of Tasks**





# **Future Work**

### **Experimental**

- 1) Transition PDE to operate using oxy-coal
- 2) Measure boundary conditions and velocities for calculations
- 3) Quantify changes in detonation characteristics between solid and gaseous fuels

### Computational

- 1) Couple MHD solver with detonation code
- 2) Develop detonation code
- 3) Parametric study of MHD performance for detonations (long-term)



### **Conductivity analysis**



1. Shao Chi Lin, E. L. Resler, and Arthur Kantrowitz. Electrical conductivity of highly ionized argon produced by shock waves. Journal of Applied Physics, 26(1):95–109, 1955.



### **CE/SE Method: 2D Detonation Example**









Distribution of electric potential

#### Maximum error for an amount of node

ConditionNo Exact
$$\delta = 1 \text{ S/m}$$
 $u_x = -\cos 2\pi x \sin 2\pi y$ Solution $\beta = 2$  $u_y = \cos 2\pi y \sin 2\pi x$ Solution $|B| = 3 \text{ T}$  $52$  $\phi = 6$ 

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