Molecular Simulation Models of Carbon Dioxide Intercalation in Hydrated Sodium Montmorillonite

22 November 2016
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Cover Illustration: Schematic representation of the clay/water/CO$_2$ system.


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Molecular Simulation Models of Carbon Dioxide Intercalation in Hydrated Sodium Montmorillonite

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# Acronyms, Abbreviations, and Symbols

<table>
<thead>
<tr>
<th>Term</th>
<th>Description</th>
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</thead>
<tbody>
<tr>
<td>3-D</td>
<td>Three-dimensional</td>
</tr>
<tr>
<td>Å</td>
<td>Angstrom</td>
</tr>
<tr>
<td>B3LYP</td>
<td>Becke-3-parameter-Lee-Yang-Parr potential</td>
</tr>
<tr>
<td>BOMD</td>
<td>Born-Oppenheimer molecular dynamics</td>
</tr>
<tr>
<td>CCSD(T)</td>
<td>Coupled-cluster with single and double (triple) electron excitations</td>
</tr>
<tr>
<td>DFT</td>
<td>Density functional theory</td>
</tr>
<tr>
<td>DRIFTS</td>
<td>Diffuse reflectance infrared Fourier-transform spectroscopy</td>
</tr>
<tr>
<td>DZVP</td>
<td>Split-valence double-zeta basis set with polarizable functions</td>
</tr>
<tr>
<td>fs</td>
<td>Femtosecond</td>
</tr>
<tr>
<td>Γ point</td>
<td>A center point of a fundamental region (Brillouin zone) of wave vectors</td>
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<tr>
<td></td>
<td>propagating through a crystal lattice</td>
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<tr>
<td>EMP2</td>
<td>Force field for carbon dioxide</td>
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<tr>
<td>GPW</td>
<td>Gaussian-plane wave scheme</td>
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<tr>
<td>LJ</td>
<td>Lennard-Jones</td>
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<tr>
<td>MC</td>
<td>Monte-Carlo</td>
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<td>Molecular dynamics</td>
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<tr>
<td>MMT</td>
<td>Montmorillonite</td>
</tr>
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<td>NETL</td>
<td>National Energy Technology Laboratory</td>
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<tr>
<td>NMR</td>
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<tr>
<td>NPT</td>
<td>Isobaric-isothermal ensemble</td>
</tr>
<tr>
<td>NVT</td>
<td>Canonical ensemble</td>
</tr>
<tr>
<td>PPPPM</td>
<td>Particle-particle particle-mesh method</td>
</tr>
<tr>
<td>ps</td>
<td>Picosecond</td>
</tr>
<tr>
<td>RDF</td>
<td>Radial distribution function</td>
</tr>
<tr>
<td>scCO₂</td>
<td>Supercritical carbon dioxide</td>
</tr>
<tr>
<td>SPC</td>
<td>Force field for water</td>
</tr>
<tr>
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<td>Montmorillonite samples from Texas</td>
</tr>
<tr>
<td>SWy</td>
<td>Montmorillonite samples from Wyoming</td>
</tr>
<tr>
<td>TOT</td>
<td>Tetrahedral-octahedral-tetrahedral</td>
</tr>
<tr>
<td>VACF</td>
<td>Velocity autocorrelation function</td>
</tr>
<tr>
<td>W</td>
<td>Water</td>
</tr>
<tr>
<td>XRD</td>
<td>X-ray diffraction</td>
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Acknowledgments

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EXECUTIVE SUMMARY

Carbon capture and storage (CCS) technologies provide effective options for reducing carbon dioxide (CO$_2$) emissions and mitigating global climate change. Geologic CO$_2$ storage involves the injection of supercritical CO$_2$ into deep geologic formations overlain by sealing formations and geologic traps that prevent the CO$_2$ from escaping. The ability of seals to retain injected CO$_2$ depends on their permeability and geomechanical property evolution. Caprocks are often comprised of shale or mudstone enriched with swelling clay minerals that can expand or contract upon interaction with CO$_2$. Intercalation of CO$_2$ into interlayer of swelling clay causes evolution of the geomechanical stress and can promote fracture formation. The interlayer of expanded clay provides ample space for additional permanent CO$_2$ storage and its subsequent transformation into carbonates.

To evaluate the effectiveness of such CO$_2$ storage scenarios and to better understand multiphase flow in storage reservoirs and seals, for improved injectivity and trapping, investigators working at the National Energy Technology Laboratory (NETL) are conducting research to develop insights into important aspects of CO$_2$ interactions with mineral surfaces, CO$_2$ storage capacity and trapping mechanisms in clays as well as induced changes in geomaterials properties and diffusion rates.

This report provides a detailed description of results of theoretical work completed to date and preliminary discussion of findings and insights; and reports the results from CO$_2$-clay interactions modeling runs.

In this study, classical molecular dynamics simulations and density functional theory (DFT)-based molecular dynamics are used to elucidate the process of CO$_2$ intercalation into hydrated Na-montmorillonite at $P$-$T$ conditions relevant to geological formations suitable for CO$_2$ storage. Of particular interest are the structural and transport properties of interlayer species after CO$_2$ intercalation. The conducted simulations allowed the research team to quantify expansion/contraction of smectite as a function of CO$_2$ and H$_2$O compositions. The resulting swelling curves can be used to gauge the amount of stored CO$_2$, compare it to the experiment, and estimate changes in geomechanical properties of the storage formation. The obtained results showed that the infrared signal of the asymmetric stretch vibration of CO$_2$ molecule is extremely sensitive to the solvent environment. The extent of the frequency shift relative to the gas-phase value can be used to probe hydration level in the interlayer with intercalated CO$_2$. Interaction of supercritical CO$_2$ with brine in deep geological formations promotes an increase of hydrophobicity of clay surfaces. As a result of wettability alteration, estimated diffusion constants of CO$_2$ and H$_2$O increase with the increased CO$_2$ load; this can contribute to faster migration of CO$_2$ throughout the formation.
1. REVIEW OF EXPERIMENTAL AND THEORETICAL PAPERS DEVOTED TO CARBON DIOXIDE INTERCALATION INTO SMECTITE CLAY MINERALS

Long-term storage of industrial carbon dioxide (CO\(_2\)) in subsurface geological strata is considered a viable option for mitigating greenhouse gas emission (NETL, 2013). The technology of geologic CO\(_2\) storage involves the injection of supercritical CO\(_2\) (scCO\(_2\)) into deep geologic formations such as saline aquifers overlain by sealing caprocks and geologic traps that would prevent the CO\(_2\) from escaping. The ability of seals to retain injected CO\(_2\) depends on their permeability and geomechanical property evolution (Allen and Allen, 2005). Caprocks are often comprised of shale or mudstone enriched with clay minerals, including swelling clays like montmorillonite (MMT) (Abdou and Ahmaed, 2010). MMT is a layered aluminosilicate where the central sheet is composed of octahedrally coordinated aluminum (Al) atoms, and the adjacent sheets contain tetrahedrally coordinated silicon (Si) atoms. These sheets comprise a 2:1 or tetrahedral-octahedral-tetrahedral (TOT) layer. In MMT, the TOT layers are negatively charged due to substitution of divalent metals (e.g., Mg\(^{2+}\) or Fe\(^{2+}\)) for the octahedrally coordinated Al or by less common substitution of Al for Si at tetrahedral sites. Hydroxyl groups complete the coordination of each octahedra. The negative charge of the TOT layers is counterbalanced by interlayer cations (e.g., Na\(^+\), Li\(^+\), Ca\(^{2+}\)) that are usually hydrated allowing for expansion or contraction of the interlayer distance of the clay depending on the relative humidity (Fu et al., 1990). Swelling clay particles interacting with scCO\(_2\) can also undergo changes in interlayer content and in the basal spacing (Giesting et al., 2012; Schaef et al., 2012). This can lead to changes in porosity, permeability, and formation of micro fractures in caprocks. As a result, studies of the interactions between scCO\(_2\) and the minerals of caprocks are necessary for assessing impacts for the long-term exposure of injected CO\(_2\) to geological seals (Kwak et al., 2011).

Dry scCO\(_2\) injected into a geological aquifer will become hydrated as a result of contact with brine retained at mineral surfaces and nanopores (Spycher et al., 2003). The resulting hydrated CO\(_2\) interacts with the caprocks predominantly through diffusion unless pre-existing or evolved fractures provide pathways for CO\(_2\) migration (Gaus, 2010). Recently, Giesting et al. (2012) reported in situ X-ray diffraction (XRD) characterization of gaseous CO\(_2\) and scCO\(_2\) interacting with Na-rich-MMT at \(T = 45^\circ \text{C}\) and \(P = 50–650\text{ bar}\) (in experiments, Na-rich-MMT is typically represented by natural or Na-exchanged SWy montmorillonite samples from Wyoming, and Ca-rich-MMT by natural or Ca-exchanged STx montmorillonite samples from Texas. In addition to the prevailing interlayer cations there are differences in the distributions of Mg, Al, and Si within the silicate layers of SWy and STx clay samples, which may complicate interpretation of the results (Costanzo, 2001; Martin, 1979)). The study by Giesting et al. (2012) showed that for partially-hydrated samples the spacing between the mineral layers (basal \(d\)-spacing) expands upon CO\(_2\) adsorption and that the degree of expansion depends on the initial water content in the interlayers. In the absence of CO\(_2\), the basal \(d\)-spacing is around 10 Å for nearly dry clay (the 0W hydration state) and increases to 12.5 Å for a fully saturated monolayer water arrangement (the 1W hydration state characterized with basal \(d\)-spacings in the range of 11.5–12.5 Å) (Fu et al., 1990; Cygan et al., 2004; Marry et al., 2002). Upon incorporation of more water, the \(d\)-spacing can increase to 14.5–15.5 Å to the next stable state where water forms a bilayer structure (the 2W hydration state) (Fu et al., 1990; Cygan et al., 2004; Marry et al., 2002). The XRD measurements showed that nearly dry clay displays no significant response upon exposure to dry scCO\(_2\) and that residual water is required to intercalate CO\(_2\).
Maximum expansion upon CO$_2$ intercalation was found at initial $d = 11.3$ Å resulting in swelling to $d = 12.5$ Å, the value that corresponds to the 1W state. The in situ XRD study by Schaef et al. (2012) on scCO$_2$ interacting with Ca-MMT at submonolayer water content confirms the expansion of the clay phase to $d$ values corresponding to the 1W state after exposure to dry scCO$_2$ over a range of temperatures (50–100 °C) and pressures (90, 125, and 180 bar).

Interaction of dry scCO$_2$ with smectite clay in the 2W state results in a collapse of the $d$-spacing to that of the 1W state (Schaef et al., 2012). However, interaction of Na-exchanged SWy and Ca-exchanged STx samples with variably wet scCO$_2$ (2–100% saturation of H$_2$O) at $T = 50$ °C and $P = 90$ bar can lead to swelling even to the values equal to the 3W state with a $d$-spacing of 18.8 Å (Schaef et al., 2012; Ilton et al., 2012). Thus, dry scCO$_2$ has the capacity to dehydrate clay and to promote increase of seal permeability due to clay collapse. On the other hand, the presence of water in scCO$_2$ can facilitate further swelling of clay.

Loring et al. (2012) further confirmed intercalation of CO$_2$ by means of nuclear magnetic resonance (NMR) spectroscopy and attenuated total reflection infrared spectroscopy. They found that intercalated CO$_2$ molecules are rotationally constrained and do not appear to react with waters to form bicarbonate or carbonic acid (Loring et al., 2012). Using diffuse-reflectance infrared spectroscopy, Romanov et al. (2010a,b), Romanov (2013), and Hur et al. (2013) have analyzed the vibrational fingerprint of CO$_2$ trapped in SWy and STx samples and also concluded that CO$_2$ can be intercalated in the interlayers of smectite minerals. These experiments revealed 5–10 cm$^{-1}$ red shifts of the asymmetric stretch fundamental frequency for the trapped CO$_2$ relative to that of the gas-phase molecule (Romanov, 2013). CO$_2$ trapped in clay interlayers is in an intricate environment involving interactions with interlayer ions, water, and clay surfaces. As was shown by Duncan and co-workers (Gregoire and Duncan, 2002; Walker et al., 2003; Jaeger et al., 2004) the asymmetric stretch fundamental of CO$_2$ is shifted 10–80 cm$^{-1}$ to the blue when the molecule forms a complex with metal ions. This observation suggests that it is the interaction with water and/or internal clay surfaces that is responsible for the observed red shift of the asymmetric stretch of CO$_2$ in interlayers of MMT.

Recently, Botan et al. (2010) performed Monte-Carlo (MC) and molecular dynamics (MD) simulations of CO$_2$ intercalation into Na-MMT using a force field for clay from Smith (1998) and the force field for water (SPC) (Berendsen et al., 1981) and the force field for CO$_2$ (EMP2) (Harris et al., 1995) models for water and carbon dioxide, respectively. Specifically, they considered Na-MMT in equilibrium with H$_2$O-CO$_2$ mixtures at $T = 75$ °C, and $P = 25$ and 125 bar. Their simulations indicated that hydrated clay can intercalate CO$_2$ and that the thermodynamically stable structures are characterized with basal $d$-spacings corresponding to the 1W and 2W hydration states. That is consistent with the experiment which shows that exposure of MMT to CO$_2$ resulted in expansion of clay particles giving the basal $d$-spacings equal to those values at 1W or 2W (Giesting et al., 2012; Schaef et al., 2012). Monte Carlo simulations of non-hydrated Na-MMT clay in equilibrium with dry scCO$_2$ have shown that CO$_2$ intercalation is unfavorable until large $d$-spacing distances (>2W) (Yu and Yang, 2011). For $d$-spacings >15.5 Å, the Helmholtz free energy displays a set of closely-spaced local minima separated by small barriers (Yu and Yang, 2011). Other modeling studies (Yang and Zhang, 2005; Peng et al., 2007; Cole et al., 2010) using different force fields, also indicate that CO$_2$ molecules can exist in the interlayers of clay minerals. At the same time, little is known about the molecular details of CO$_2$ intercalation in the interlayer of smectite clays.
In the present study, classical molecular dynamics simulations are used to elucidate the process of CO$_2$ intercalation into hydrated Na-MMT at initial H$_2$O content and $P$-$T$ conditions relevant to geological formations for CO$_2$ storage. Of particular interest are the structural and transport properties of interlayer species after CO$_2$ intercalation. In addition, density functional theory (DFT)-based molecular dynamics is engaged to compute vibrational power spectra for comparison with the experimental IR spectra and the power spectra from force field simulations.
2. **COMPUTATIONAL DETAILS**

2.1 **MOLECULAR DYNAMICS SIMULATIONS USING DENSITY FUNCTIONAL THEORY (DFT)**

In recent years, computational resources have improved making it possible to tackle complex clay mineral systems by using electronic structure methods. DFT, in particular, provides reliable estimates of electrostatic potentials, thermodynamics, spectroscopic data, reaction mechanisms, and other properties (Cygan et al., 2009; Sholl and Steckel, 2009). DFT-based Born-Oppenheimer molecular dynamics (BOMD) simulations were carried out using the CP2K software package (CP2K, 2013). The evolution of a system using BOMD methods is governed by Newtonian dynamics with energies and forces at each time step being estimated from DFT calculations (Marx and Hutter, 2009). Goedecker-Teter-Hutter pseudopotentials (Goedecker et al., 1996; Krack, 2005) were used together with a hybrid Gaussian-plane wave scheme (GPW) with a split-valence double-zeta basis set with polarizable functions (DZVP) quality Gaussian basis set (VandeVondele and Hutter, 2007) for the Kohn-Sham orbitals and an energy cutoff of 350 Rydbergs for the plane-wave expansion of the electron density. The gradient-corrected correlation functional of Perdew et al. (1996) was employed, together with the DFT-D2 method (Grimme, 2006) to include long-range, two-body dispersion corrections (previous studies by Voora et al. (2011) and Zhang et al. (2012) demonstrated the importance of such corrections). In the DFT-D2 scheme (Grimme, 2006) dispersion-corrections are described in terms of damped atom-atom $C_6^{AB}$: $R_6^{AB}$ terms, where $R_{AB}$ is the distance between atoms $A$ and $B$. A damping factor is engaged to avoid double counting and divergence at small $R_{AB}$ (Tkatchenko and Scheffler, 2009).

The supercell for Na-MMT was developed starting from the structure of pyrophyllite (Lee and Guggenheim, 1981) which has no metal cation substitution and thus has neutral layers. A unit cell with [Al$_4$O$_8$(OH)$_4$(Si$_8$O$_{12}$)] composition was used for pyrophyllite. The lattice parameters of the unit cell are: $a = 5.16$ Å, $b = 8.97$ Å, and $c = 9.37$ Å, and $\alpha = 91.5^\circ$, $\beta = 100.5^\circ$ and $\gamma = 89.6^\circ$ (Lee and Guggenheim, 1981). To prepare the MMT structural model, a triclinic 2 x 1 x 1 supercell with one isomorphic octahedral Al$^{3+}$/Mg$^{2+}$ substitution per unit cell was employed. This introduces one negative charge for each O$_{20}$(OH)$_4$ unit, which is compensated by an Na$^+$ ion in the interlayer space. This produces a supercell with the formula Na$_2$[MgAl$_3$O$_8$(OH)$_4$(Si$_8$O$_{12}$)]$_2$.

The $\Gamma$ point sampling of the Brillouin zone is adequate because of the large size of the unit cell.

In the DFT/MD calculations the number of water molecules in the interlayer region was varied from two to eight in the presence of one carbon dioxide molecule. The system was first equilibrated using the isobaric-isothermal ensemble (NPT) with $T = 348.15$ K and $P = 130$ bar, conditions close to those existing in subsurface geological reservoirs and caprocks, and also to those used in CO$_2$ intercalation experiments in clays carried out at National Energy Technology Laboratory (NETL) (Romanov, 2013). Starting from initial structures relaxed using MD simulations with force fields (see Section 2.2), an equilibration time of 15 picosecond (ps) was employed, followed by 20 ps production runs using the microcanonical ensemble. The velocity Verlet algorithm was then used to update positions every 0.5 femtosecond (fs). To reduce the energy drift to 1 K/ps, the energy convergence tolerance for the electronic self-consistency cycle at each Born-Oppenheimer step was set to $10^{-6}$ eV. The atomic velocities were collected every 2
fs for up to 20 ps from production runs and used to calculate the velocity autocorrelation functions (VACF) (Allen and Tildesley, 1987), which, in turn, were used to calculate the power spectra. The velocity autocorrelation function for CO$_2$ was computed using the standard definition:

$$C(t) = \frac{1}{3N} \sum_i^3 v_i(0) \cdot v_i(t)$$

(1)

where \(v_i(t)\) is the velocity of the \(i\)-th CO$_2$ atom at time \(t\), and \(N\) is the number of molecules in the simulation.

2.2 MOLECULAR DYNAMICS SIMULATIONS USING FORCE FIELDS

The force field calculations were carried out using the GROMACS package (van der Spoel et al., 2013). For the clay system, the Clayff force field (Cygan et al., 2004) which consists of non-bonded (electrostatic and van der Waals) terms parameterized for use with layered minerals was used. In Clayff the pairwise energy between atoms \(i\) and \(j\) separated by a distance \(r_{ij}\) is given by:

$$E_{ij} = \frac{q_iq_je^2}{4\pi\varepsilon_0 r_{ij}} + 4\varepsilon_{ij} \left[ \left( \frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left( \frac{\sigma_{ij}}{r_{ij}} \right)^6 \right]$$

(2)

where \(q_i\) is the charge on atom \(i\), \(e\) is the elementary charge of an electron, \(\varepsilon_0\) is the vacuum permittivity, and \(\varepsilon_{ij}\) and \(\sigma_{ij}\) are the Lennard-Jones energy and distance parameters, respectively. The flexible SPC (Berendsen et al., 1981) model was engaged for the water molecules placed in the interlayer space and for the layer hydroxyl groups. For CO$_2$, a recently developed flexible potential including intramolecular bond stretch and angle bend was used (Cygan et al., 2012). The general expression for the total potential energy is:

$$E_{Total} = E_{Coul} + E_{VDW} + E_{Stretch} + E_{Bend},$$

(3)

where harmonic potentials are used for the bond stretch and angle bend terms:

$$E_{Stretch} = \frac{1}{2} k_s (r_{ij} - r_0)^2$$

(4)

and

$$E_{Bend} = \frac{1}{2} k_B (\theta_{ijk} - \theta_0)^2$$

(5)

The optimized force field parameters for CO$_2$, presented in Table 1, were combined with those in Clayff (Cygan et al., 2004) to model CO$_2$ intercalation into hydrated MMT. The Lorentz-Berthelot mixing rule (Allen and Tildesley, 1987) was used to obtain the Lennard-Jones (LJ) parameters for interactions between unlike atoms. The simulations were performed under periodic boundary conditions, with the long-range electrostatics treated by the particle-particle particle-mesh (PPPM) Ewald method (Allen and Tildesley, 1987). The cut-off radii for the non-bonded van der Waals interactions and for the Ewald summation of the electrostatics were chosen to be 12 Å, with switching distances starting from 11 Å. Due to the use of cut-offs for the LJ interactions, long-range dispersion corrections for energy and pressure were applied (van der Spoel et al., 2013). The leap-frog algorithm (van Gunsteren and Berendsen, 1988) was used to update positions every 1 fs.
Table 1: Force field parameters for CO$_2$

<table>
<thead>
<tr>
<th></th>
<th>Non-bonding</th>
<th>Bonding</th>
</tr>
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<tbody>
<tr>
<td>$q_C$</td>
<td>+0.6512 e</td>
<td>$k_{CO}$ 8443 kJ/mol Å$^2$</td>
</tr>
<tr>
<td>$q_O$</td>
<td>-0.3256 e</td>
<td>$r_{CO}$ 1.162 Å</td>
</tr>
<tr>
<td>$\varepsilon_C$</td>
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<td>$k_{OCO}$ 451.9 kJ/mol rad$^2$</td>
</tr>
<tr>
<td>$\varepsilon_O$</td>
<td>0.6683 kJ/mol</td>
<td>$\theta_{OCO}$ 180.0°</td>
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<tr>
<td>$\sigma_C$</td>
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<td>$\sigma_O$</td>
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</tbody>
</table>

The general chemical formula used for the sodium montmorillonite is Na$_{x}$Mg$_{x}$Al$_{3-x}$Si$_{4}$O$_{10}$(OH)$_{2}$·nH$_2$O, where the layer charge resides on the octahedral sheet (tetrahedral substitutions such as Al$^{3+}$ for Si$^{4+}$ can also occur but are not considered here). For the molecular dynamics simulations with the Clayff force field (Cygan et al., 2004), the MMT structural model was created by replicating a pyrophyllite unit cell with an isomorphic octahedral Al$^{3+}$/Mg$^{2+}$ substitution to produce a triclinic 8 x 4 x 4 supercell (64 times larger than the supercell used for the DFT-based MD simulations). The negative charge introduced by the substitution is compensated by 96 sodium ions residing in the interlayers. The stoichiometry is Na$_{0.75}$Mg$_{0.75}$Al$_{3.25}$(OH)$_{4}$(Si$_{4}$O$_{10}$)$_{2}$ with a layer charge of 0.75 per O$_{20}$(OH)$_{4}$ layer unit. This results in 5,120 atoms constituting the clay phase. The CO$_2$ content was varied from 0.5 to 4 molecules per unit cell and the water content was varied from one to nine molecules per unit cell. The H$_2$O/CO$_2$ composition in the interlayer region is designated as $X$-$Y$, where $X$ and $Y$ are, respectively, the numbers of water and CO$_2$ molecules per unit cell. Particular emphasis is placed on scenarios with three and five water molecules per unit cell. The former composition provides a partially saturated water monolayer (with $d$ ~ 11.4 Å), which is close to that of the samples used to study the impact of CO$_2$ exposure to Na-MMT in high pressure experiments (Giesting et al., 2012; Schaeff et al., 2012). The latter composition gives a $d$-spacing of 12.2 Å, which corresponds to a fully saturated monolayer (1W). In the 1 W state MMT structure demonstrates a sharp decrease in ability to capture dry CO$_2$ as reported in high-pressure X-ray diffraction experiments (Giesting et al., 2012; Schaeff et al., 2012). Relaxation of MMT with intercalated species was performed using the NPT ensemble at $T = 348.15$K and $P = 130$ bar as well as at $T = 300$ K and $P = 1$ bar to study the dependence of the basal spacing on pressure. Equilibration runs of 1 ns were carried out followed by 20 ns production runs in the NPT ensemble, with semi-isotropic pressure coupling permitting the $z$-dimension to fluctuate independently from the $x$ and $y$ directions. Pressure was controlled by a Parrinello-Rahman barostat (Parrinello and Rahman, 1981; Nóse and Klein, 1983) with a relaxation time of 4 ps, and temperature was controlled by a Nóse-Hoover thermostat (Nóse, 1984; Hoover, 1985) with a relaxation time of 2 ps. A time step of 1 fs was used in the simulations.
The radial distribution function (RDF) for species $B$ around $A$ is calculated as:

$$G_{A-B}(r) = \frac{1}{4\pi \rho_B r^2} \frac{dN_{A-B}}{dr}$$  \hspace{1cm} (6)$$

where $\rho_B$ is the number density of species B, and $dN_{A-B}$ is the average number of type $B$ particles lying in the region $r$ to $r+dr$ from a type A particle. $N_{A-B}$ is the coordination number for $B$ around $A$.

To calculate the diffusion coefficients of the interlayer species, the Einstein relation was employed using equilibrated atomic trajectories from the $NVT$ ensemble simulations with 1 ps sampling to evaluate the mean square displacement of the molecules and ions:

$$D = \lim_{t \to \infty} \frac{1}{6N_m} \sum_{j=1}^{N_m} \left[ r_j(t) - r_j(0) \right]^2$$  \hspace{1cm} (7)$$

where $N_m$ is a number of a selected species and $r_i(t)$ is the center-of-mass position of the $i^{th}$ species at time $t$. The averages were over 4 ns trajectories. The diffusion coefficients were derived from the linear slope of the mean square displacement as a function of the simulation time. Different restart points in the analysis were taken to monitor convergence.
3. **EXPERIMENTAL DETAILS**

Diffuse Reflectance Infrared Fourier-Transform Spectroscopy (DRIFTS)

The clay samples used in this work were powders of SWy-2 (natural Na-rich-MMT from Wyoming) and STx-1b (natural Ca-rich-MMT from Texas) acquired from the Source Clays Repository (Costanzo, 2001; Martin, 1979). An FT-IR spectrometer (Thermo Electron Corporation, Model Nicolet 8700) with a Smart Collector and dual environmental chamber was used to obtain diffuse reflectance infrared spectra. The spectra were collected in a nitrogen flow-through environment, after 8 hrs of exposure of the clay samples to 1,500 psig (~10 MPa) pressure of CO$_2$ at 55 °C. In each measurement, 100 scans were completed with 4 cm$^{-1}$ resolution. KBr diffuse reflectance spectra were used as a background reference. More details on the experimental setup and execution can be found in Romanov (2013) and other studies.
4. **ANALYSIS OF D-SPACING, RADIAL DISTRIBUTION FUNCTIONS, AND DENSITY PROFILES FOR CARBON DIOXIDE-WATER-SODIUM-MONTMORILLONITE SYSTEMS**

Figure 1 shows a schematic representation of the montmorillonite TOT layers and interlayer species (H$_2$O, CO$_2$, Na$^+$) considered in this study. Figure 2 reports the expansion of the $d$-spacing of Na-MMT upon intercalation of water computed using MD simulations with the Clayff force field (Cygan et al., 2004). Comparison with experimental data shows that the MD results closely reproduce the experimental trend in the $d$-spacing, displaying plateaus corresponding to formation of monolayer and bilayer water in the interlayer. It is important to note that it is a generally accepted paradigm among clay mineralogists that coexistence of different hydration states (0W, 1W, 2W) in a smectite sample is common even under controlled conditions (Ferrage et al., 2005). It is also generally accepted that fractional hydration states correspond to a sample with different integer hydration structures. For example, the diffuse character of the (00l) reflections, at the transition between two discrete hydration states, and the asymmetric (001) peak profile provides evidence that the MMT structure evolves gradually from one hydration state to the other through mixed-layer structures composed of discrete hydration states (Sato et al., 1992; Ferrage et al., 2007). Therefore, the experimental data outside of the ranges designated by the dotted lines in Figure 2 may have originated from a mixture of montmorillonite at different hydration states. In the simulations the structures corresponding to the intermediate $d$-spacing values were obtained from well-defined model systems with controlled amounts of water in the interlayer. Hydration levels intermediate between 0W and 1W and intermediate between 1W and 2W provide equilibrated structures with parallel TOT clay layers as necessary to obtain a series of basal diffraction peaks. Thus, these calculations suggest that smectite minerals could exist at fractional hydration states. However, it is possible that these are obscured in experimental diffraction studies by the mixed hydration states.
Figure 1: Schematic representation of the clay/H₂O/CO₂ system. Color designation: red balls – oxygens, purple – sodium ions, white – hydrogens, and grey – carbon.
The spacing calculated for the $P$-$T$ conditions employed in the NETL experiment ($T = 75 \, ^\circ\text{C}$ and $P = 130 \, \text{bar}$) (Romanov, 2013) deviates only slightly from that calculated at $P = 1 \, \text{bar}$ and lower temperature. Thus, the $d$-spacing is relatively insensitive to changes in pressure and temperature, with the degree of water content being the main factor controlling the extent of swelling. This is consistent with XRD-measurements of $d$-spacings showing that hydrate states are relatively stable with pressure (Fu et al., 1990; Giesting et al., 2012; Ilton et al., 2012).

DFT calculations have shown that the adsorption of dry CO$_2$ in the interlamellar space of non-hydrated Na-MMT is energetically unfavorable (Voora, 2013). This is consistent with results of Gibbs ensemble Monte Carlo simulations using classical force fields that revealed that dry CO$_2$ in Na-MMT is unstable except at large (>2W) $d$-spacing values (Yu and Yang, 2011). In order to study CO$_2$ intercalation, force field MD simulations with the water content varied from 1–9 H$_2$O molecules per unit cell were performed. Figure 3 displays the calculated interlayer distance as a function of the number of water molecules for selected numbers of intercalated carbon dioxide molecules per unit cell. The bottom curve, which reports the results in the absence of intercalated CO$_2$ molecules, serves as the reference. As seen in Figure 3, intercalation of CO$_2$ causes an expansion of the interlamellar spacing comparable to that caused by increasing hydration. Full monolayer coverage is achieved for 5 H$_2$O molecules per unit cell, as well as for 4H$_2$O+1CO$_2$, 2H$_2$O+2CO$_2$, or 1H$_2$O+3CO$_2$. In the latter two cases, the fact that $n$H$_2$O+$m$CO$_2$ = 4 rather than 5 reflects the larger size of the CO$_2$ molecule compared to H$_2$O. Similarly, full bilayer coverage can be achieved with compositions ranging from 9 H$_2$O molecules to 3 H$_2$O molecules with 3 CO$_2$ molecules. At a water content of 6 molecules per unit cell, the addition of a single CO$_2$
molecule per unit cell results in expansion of the $d$-spacing to a value close to that of the 2W state. However, the latter process appears to be thermodynamically unfavorable as intercalation of CO$_2$ was not observed in several in-situ XRD studies (Giesting et al., 2012; Schaeff et al., 2012; Ilton et al., 2012) on Na- and Ca-MMT with the initial $d$-spacing corresponding to the fully saturated 1W state (i.e., 5–6 H$_2$O molecules per unit cell). At $d$-spacing distances of ~14–15 Å (corresponding to the 2W state) a distinct plateau is observed for fixed CO$_2$ concentrations over a range of initial water content (Figure 3). For example, 8–0.5, 7–1, and 6–2 water-CO$_2$ compositions all have similar $d$-spacings. As a result, in the 2W hydration state CO$_2$ incorporation can displace water keeping the $d$-spacing nearly constant rather than further expanding the interlayer spacing.

![Figure 3: $d$-spacing as a function of number of water molecules at fixed numbers of CO$_2$ molecules per unit cell. Dashed lines indicate ranges of basal $d$-spacing corresponding to 1W and 2W hydration states.](image)

To explore the distribution of the various species in the interlamellar space of the clay, density profiles were calculated for 3-Y and 5-Y compositions. Figures 4 and 5 display the resulting density profiles computed along the $z$ axis (perpendicular to the clay surface) and averaged over the interlayer region of the simulation box. The amounts of CO$_2$ were chosen to induce $d$-spacing expansion toward the 1W, 2W, and 3W hydration states. The distributions confirm that H$_2$O and CO$_2$ molecules indeed form well-defined layered structures similar to pure 1W and 2W hydration states. Figure 4a reports the profiles for the 1W state, which, upon addition of one more CO$_2$ molecule per cell, starts to form the 2W state (Figure 4b). Figure 4b reports the profiles for a "non-saturated" 2W system, while Figure 5b represents a fully saturated 2W. Figures 4c and 5c report the density profiles at the interlayer distances corresponding to the 3W
hydration state. At those spacings (3W) the simulations show that the center layer is composed almost entirely of CO$_2$ molecules sandwiched between two layers of the CO$_2$/H$_2$O mixture.

![Graph showing density profiles along the interlayer distance](image)

**Figure 4:** Density profiles along the interlayer distance perpendicular to the internal surfaces of Na-MMT showing distribution of the intercalated species for a) 3-1, b) 3-2, and c) 3-4 compositions. Dashed lines designate the planes of basal oxygens.
Figure 5: Density profiles along the interlayer distance perpendicular to the internal surfaces of Na-MMT showing distribution of the intercalated species for a) 5-1, b) 5-2, and c) 5-4 compositions. Dashed lines designate the planes of basal oxygens.
The ability of water molecules to induce swelling in a stepwise fashion is related to the formation of an extended hydrogen bonding network and interaction of the water molecules with clay surface (Fu et al., 1990). The carbon dioxide can be expected to participate in interaction with water and clay surfaces. In this regard, it is instructive to consider the orientational behavior of CO\textsubscript{2} in the confining environment of MMT. This is accomplished by examining the distribution of angles between the CO\textsubscript{2} axial orientation and the axis perpendicular to the clay surfaces. Figure 6 reports this distribution computed for each CO\textsubscript{2} molecule using the C-O bond most nearly perpendicular to the surface at H\textsubscript{2}O/CO\textsubscript{2} compositions corresponding to 1W, 2W, and 3W hydration states. At each state a normal distribution centered around 90° is obtained indicating that the carbon dioxide molecules are preferentially oriented parallel to the confining clay surfaces. With increasing number of water-CO\textsubscript{2} layers, the CO\textsubscript{2} molecules explore a wider range of angles consistent with greater rotational freedom in the interlayer. Inspection of the corresponding MD trajectories reveals that the CO\textsubscript{2} molecules display no specific coordination to the atoms comprising MMT. These data are consistent with experimental observations that MMT has to be wetted in order to intercalate CO\textsubscript{2} (Giesting et al., 2012; Schaef et al., 2012; Ilton et al., 2012). Thus, the compositions providing the density profiles depicted in Figures 4c and 5c with a central CO\textsubscript{2} layer are likely to be unstable with respect to collapse to a more stable bilayer form (Figures 4b, 5b) by expelling CO\textsubscript{2} molecules or to expansion into the 3W hydration state by incorporating more water molecules.

Figure 6: Histograms of angular distribution for CO\textsubscript{2} orientation relative to the axis perpendicular to clay surface. Data averaged over 30 CO\textsubscript{2} molecules for every composition during 4 ns.
As seen in Figures 4 and 5, pronounced changes occur in the density profiles of the \( \text{Na}^+ \) ions with increasing \( \text{CO}_2 \) content. Specifically, the incorporation of \( \text{CO}_2 \) molecules into the interlayer region enhances the probability of finding \( \text{Na}^+ \) ions near the surfaces, thus splitting the \( \text{Na}^+ \) profiles into several peaks. The surface-bound sodium ions (inner-sphere adsorption) are coordinated above the centers of the hexagonal rings of silicon tetrahedra linked by shared basal oxygens. However, these ions retain strong interactions with nearby water molecules. In this regard, the amount of water should be an important factor determining the degree of ion adsorption. Indeed, comparison of Figures 4 and 5 shows that cation adsorption at the surface is less important in the systems having five water molecules per unit cell than in the systems with only three water molecules per unit cell. To quantify the adsorption process the concentrations of the \( \text{Na}^+ \) ions at the surfaces were calculated as a function of the carbon dioxide concentration. Figure 7 displays occupancy values of \( \text{Na}^+ \) ions near the centers of the hexagonal rings as a percentage of a total number of the rings for the 3-Y and 5-Y compositions.

Figure 7: Fractional occupancy of the hexagonal sites on the internal clay surfaces by \( \text{Na}^+ \) as a function of \( \text{H}_2\text{O}/\text{CO}_2 \) composition in the interlayer.

To calculate these values the sodium atoms were counted as being adsorbed at the hexagonal rings when the ions had a residence time at the surface greater than 50% of the total simulation time. A \( \text{Na}^+ \) ion was considered adsorbed at the surface if three and more distances between the sodium ion and basal oxygens become less than 2.9 Å. The adsorption of \( \text{Na}^+ \) ions on the internal surfaces depends strongly on the water content, with the extent of surface adsorption being greater for the 3-Y than for 5-Y composition. The 3-Y and 5-Y composition plots are reminiscent of a typical adsorption isotherm showing increase of \( \text{Na}^+ \) adsorbate concentration with increase of \( \text{CO}_2 \) content in the interlayer. The plot for the 5-Y composition reveals a more smooth behavior, with the preference for \( \text{Na}^+ \) to stay solvated in the interlayer in the absence of \( \text{CO}_2 \) content. Increasing the carbon dioxide concentration promotes migration of the ions to the clay.
surfaces where they form inner-sphere surface complexes (Bourg and Sposito, 2011). The adsorption of sodium ions at the clay surfaces increases the hydrophobicity of the surfaces since the ions effectively shield the basal oxygens from hydrogen bonding with water molecules. This process could also be responsible for observed dewetting and increased contact angles on mica and silica surfaces during scCO$_2$ invasion under high ionic strength of brine (Wan et al., 2011).

In order to characterize how the various interactions impact the hydrogen bonding, hydrogen-bond lifetimes were computed following the approach described in van der Spoel et al. (2006). Table 2 reports the calculated hydrogen-bond lifetimes for water-clay, water-water, and water-carbon dioxide pairs at different carbon dioxide concentrations and two levels of water content. In general, the longest lived hydrogen bonds are those between water molecules followed by water-clay and then water-CO$_2$. This is consistent with the results of our recent investigation of water loading on the pyrophyllite surface that displayed stronger water-water than water-surface interactions (Zhang et al., 2012). Increased intercalation of carbon dioxide is accompanied by decreased H-bond lifetimes for all three types of interactions. This indicates that as the interlayer space is expanded, the molecular coordination becomes less structured (Table 2, Figure 6). Thus, expansion of the confining space to accommodate more CO$_2$ molecules translates into a more orientationally disordered arrangement of the interlayer water and carbon dioxide molecules.

<table>
<thead>
<tr>
<th>Composition (X-Y)</th>
<th>3-0 (1L)</th>
<th>3-0.5 (1L)</th>
<th>3-1 (1L)</th>
<th>3-2 (2L)</th>
<th>3-3 (2L)</th>
<th>3-4 (3L)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\tau_{\text{H}_2\text{O}-\text{H}_2\text{O}}$</td>
<td>7.36</td>
<td>9.31</td>
<td>15.28</td>
<td>12.21</td>
<td>6.28</td>
<td>5.92</td>
</tr>
<tr>
<td>$\tau_{\text{H}_2\text{O}-\text{CO}_2}$</td>
<td>-</td>
<td>6.48</td>
<td>8.65</td>
<td>2.77</td>
<td>2.64</td>
<td>1.71</td>
</tr>
<tr>
<td>$\tau_{\text{H}_2\text{O}-\text{clay}}$</td>
<td>20.25</td>
<td>12.98</td>
<td>13.54</td>
<td>6.25</td>
<td>4.21</td>
<td>3.69</td>
</tr>
<tr>
<td>5-0 (1L)</td>
<td>11.76</td>
<td>9.97</td>
<td>5.88</td>
<td>8.36</td>
<td>5.24</td>
<td></td>
</tr>
<tr>
<td>$\tau_{\text{H}_2\text{O}-\text{H}_2\text{O}}$</td>
<td>-</td>
<td>2.4</td>
<td>0.68</td>
<td>1.84</td>
<td>0.31</td>
<td></td>
</tr>
<tr>
<td>$\tau_{\text{H}_2\text{O}-\text{CO}_2}$</td>
<td>5.15</td>
<td>7.22</td>
<td>2.17</td>
<td>4.57</td>
<td>1.43</td>
<td></td>
</tr>
</tbody>
</table>

*Number of layers is indicated in parenthesis.
5. **CALCULATION OF DIFFUSION COEFFICIENTS FOR INTERLAYER SPECIES IN SODIUM MONTMORILLONITE**

Table 3 reports the diffusion coefficients for interlayer species computed in this work as well as those obtained from experimental measurements in similar systems. The calculated values are reported for both diffusion in three-dimensional (3-D) space and for diffusion parallel to the clay surfaces. In the confining environment of nano-channels the lateral diffusion coefficients are more relevant. The data reported in Table 3 show that for both water and carbon dioxide molecules the diffusivities for lateral motion are about 30% greater than those for 3-D motion. Moreover, the diffusion coefficients of both CO\textsubscript{2} and H\textsubscript{2}O increase with increasing concentration of CO\textsubscript{2} due to the associated expansion of the interlayer space. The diffusion coefficients of water computed for the systems without CO\textsubscript{2} (3-0 and 5-0) are in close agreement with the experimental values for interlayer water in MMT obtained using QENS spectroscopy (Marry et al., 2008) and neutron spin echo for synthetic Na- Hectorite (Marry et al., 2011), a trioctahedral smectite with isomorphous substitution in the octahedral sheet that displays the similar swelling properties as MMT and has comparable diffusion coefficients (Malikova et al., 2007). The diffusion coefficients of H\textsubscript{2}O and CO\textsubscript{2} in the interlayer of Na-MMT calculated for the 3-1 composition are in agreement with those computed by Botan et al. (2010) for a similar composition. Formation of the second and third water/CO\textsubscript{2} layers induced by CO\textsubscript{2} intercalation leads to stepwise increases in diffusivity of carbon dioxide compared to the values obtained for the monolayer arrangement. The effect of clay swelling on the diffusion coefficients is more pronounced for CO\textsubscript{2} than for water. For example, for the 3-Y composition the change from mono- to the bilayer arrangement is accompanied by nearly an order of magnitude increase of the CO\textsubscript{2} diffusion coefficients, while the corresponding change for water is only about a factor of two (Table 3). The greater impact of the interlayer spacing on the CO\textsubscript{2} diffusivity can be understood in terms of the preferred parallel orientation of the CO\textsubscript{2} molecules relative to the clay surface.
Table 3: Diffusion coefficients ($\times 10^{-5}$ cm$^2$/s) of water, carbon dioxide molecules, and Na$^+$ cations in the interlayer space of sodium montmorillonite.

<table>
<thead>
<tr>
<th>Composition X-Y</th>
<th>Diffusion coef.</th>
<th>3-0 (1L)</th>
<th>3-0.5 (1L)</th>
<th>3-1 (1L)</th>
<th>3-2 (2L)</th>
<th>3-3 (2L)</th>
<th>3-4 (3L)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$D_{H^2O}^a$</td>
<td></td>
<td>0.26±0.02</td>
<td>0.26±0.02</td>
<td>0.14±0.02</td>
<td>0.24±0.05</td>
<td>0.35±0.03</td>
<td>0.68±0.07</td>
</tr>
<tr>
<td>$D_{xy}^{H^2O}$</td>
<td></td>
<td>0.39±0.03</td>
<td>0.39±0.02</td>
<td>0.21±0.02</td>
<td>0.36±0.04</td>
<td>0.52±0.07</td>
<td>1.01±0.09</td>
</tr>
<tr>
<td>5-0 (1L)</td>
<td></td>
<td>0.30±0.02</td>
<td>0.28±0.20; 1.0±0.1</td>
<td>0.70±0.08</td>
<td>0.80±0.03</td>
<td>0.80±0.06</td>
<td>1.08±0.08</td>
</tr>
<tr>
<td>$D_{CO_2}^b$</td>
<td></td>
<td>0.16±0.01</td>
<td>0.12±0.01</td>
<td>0.92±0.05</td>
<td>1.10±0.07</td>
<td>2.23±0.15</td>
<td></td>
</tr>
<tr>
<td>$D_{xy}^{CO_2}$</td>
<td></td>
<td>0.23±0.01</td>
<td>0.18±0.01; 0.17(2)$^d$</td>
<td>1.38±0.08</td>
<td>1.65±0.08</td>
<td>3.12±0.17</td>
<td></td>
</tr>
<tr>
<td>5-0 (1L)</td>
<td></td>
<td>0.30±0.02</td>
<td>0.28±0.20; 1.0±0.1</td>
<td>0.70±0.08</td>
<td>0.80±0.03</td>
<td>0.80±0.06</td>
<td>1.08±0.08</td>
</tr>
<tr>
<td>$D_{Na^+}^c$</td>
<td></td>
<td>0.04±0.01</td>
<td>0.08±0.01</td>
<td>0.07±0.01</td>
<td>0.05±0.01</td>
<td>0.06±0.01; 0.25±0.17</td>
<td>0.10±0.02; 0.48±0.22</td>
</tr>
<tr>
<td>$D_{xy}^{Na^+}$</td>
<td></td>
<td>0.06±0.02</td>
<td>0.12±0.01</td>
<td>0.10±0.02; 0.13(2)$^d$</td>
<td>0.09±0.02</td>
<td>0.08±0.01; 0.37±0.26</td>
<td>0.12±0.03; 0.58±0.31</td>
</tr>
<tr>
<td>5-0 (1L)</td>
<td></td>
<td>0.06±0.02</td>
<td>0.12±0.01</td>
<td>0.10±0.02; 0.13(2)$^d$</td>
<td>0.08±0.02</td>
<td>0.08±0.01; 0.37±0.26</td>
<td>0.12±0.03; 0.58±0.31</td>
</tr>
</tbody>
</table>

$^a$ The italic font is used to designate coefficients calculated for sodium cations solvated by water in the interlayer space. $D_{xy}$ denotes lateral diffusion coefficients for motion parallel to clay surfaces. Number of layers is given after a composition notation in the parenthesis.

$^b$ Marry et al., 2008

$^c$ Marry et al., 2011

$^d$ Botan et al., 2010
At basal \(d\)-spacings corresponding to three layers (where the central layer comprised solely of \(\text{CO}_2\) molecules is sandwiched by two \(\text{CO}_2\)/water layers), the lateral diffusion coefficient for \(\text{CO}_2\) attains a value of \(4.23\pm0.17\times10^{-5}\) cm\(^2\)/s. This value comprises contributions from both the \(\text{CO}_2\) in water layers and the central \(\text{CO}_2\) layer, and is comparable to that measured for diffusion of \(\text{CO}_2\) in bulk water at \(5.40\pm0.10\times10^{-5}\) cm\(^2\)/s (\(T = 348.15\) K) (Lindeberg and Wessel-Berg, 1997). Expansion of the interlayer space due to an increase of the carbon dioxide content and subsequent formation of multilayers formed by interlayer species leads to an increase in diffusion coefficients of water (Table 3). The calculated diffusion constants of \(\text{H}_2\text{O}\) in MMT are in good agreement with measured diffusion constants for water in clay interlayer spaces. The measured diffusion coefficient of water in the bulk at \(T = 343\) K is \(5.65\times10^{-5}\) cm\(^2\)/s (Thomas and Adams, 1965) which is more than an order of magnitude greater than that for water confined between clay layers.

In the case of \(\text{Na}^+\) ions, direct comparison of the computed and experimental values of the diffusion constants can be misleading since measured ionic mobilities in montmorillonite samples can have contributions from pores and external surfaces as well as from the interlayer spaces depending on experimental conditions and ionic strength (Kozaki et al., 1998, 2008). Kozaki et al. (1998, 2008) reported a diffusion constant of \(1.8\times10^{-6}\) cm\(^2\)/s for interlayer sodium ions in the 2W hydration state of MMT at \(T = 323\) K and 0.1-0.3 M concentrations. This value is close to the computed diffusion constants of sodium ions in the interlayer space (Table 3). The intercalation of \(\text{CO}_2\) has only a moderate effect on the diffusion coefficient of the sodium ions. However, the computed diffusion constants include contributions from the surface-adsorbed ions which grow in importance as the \(\text{CO}_2\) content increases (Figures 4 and 5). Calculations were also carried out where diffusion of the interior sodium ions was separated from contributions from surface-bound \(\text{Na}^+\) ions. Not surprisingly, the diffusion coefficients for non-surface bound \(\text{Na}^+\) ions are much larger than those computed for total \(\text{Na}^+\) ions for compositions with high \(\text{CO}_2\) content (Table 3). Such behavior is attributed to increased adsorption of \(\text{Na}^+\) at the surface as \(\text{CO}_2\) concentration increases (Figure 7).
6. **INTERPRETATION OF INFRARED SPECTRA OF CO$_2$ TRAPPED IN SODIUM MONTMORILLONITE**

CO$_2$ trapped in MMT produces a distinctive infrared reflectance spectrum (Romanov et al., 2010a,b; Romanov, 2013). Figure 8 compares the asymmetric stretching region of Fourier transform infrared spectra of gaseous CO$_2$ and of CO$_2$ trapped in Ca-MMT (STx-1b) and Na-MMT (SWy-2) clays. The gas-phase CO$_2$ molecule has rotational-vibrational adsorption bands even though it has a zero permanent dipole. This is a consequence of the asymmetric (v$_3$) stretch and bending modes inducing oscillating dipole moments. The selection rule for the band involving excitation of v$_3$ is $\Delta J = \pm 1$ corresponding to P and R branches (where J is the rotational quantum number). The Q branch with $\Delta J = 0$ is forbidden and deduced to occur at ~2,349 cm$^{-1}$ (Figure 8, the vertical line). For CO$_2$ intercalated in a clay phase the selection rule that makes the Q-branch forbidden in the gas phase is lifted, and the spectra reveal a strong signal due to the CO$_2$ asymmetric stretch vibrational mode (Papousek and Aliev, 1982).

Rotational states of adsorbed molecules are frustrated by orientation-dependent perturbations within the surface potential wells (Brown et al., 1999; Schaffert et al., 2013) and the ro-vibrational P, Q, R branches collapse into a broad vibrational band, which is characteristic of physisorption (Kono et al., 1983). The peak maximum is red-shifted by 5 cm$^{-1}$ in Na-MMT and by 10 cm$^{-1}$ in Ca-MMT relative to that of the fundamental of gaseous CO$_2$. These small frequency shifts indicate that carbon dioxide molecules are not engaged in strong interactions.

Classical molecular dynamics simulations were carried out to compute the power spectra of CO$_2$ intercalated in Na-MMT with (H$_2$O)$_n$(CO$_2$)$_m$, compositions of $n=1$-$9$ and $m=1$-$4$ per unit cell. These calculations provide a frequency of the CO$_2$ asymmetric stretch vibration essentially identical to that of the gas-phase molecule calculated using the same theoretical method. The failure of the classical MD simulations to predict a red shift of the CO$_2$ asymmetric stretch vibration is indicative of a deficiency in the force field. This led us to also calculate the power spectra using DFT-based MD simulations. Details of these calculations are given in Section 2.1. The supercell employed is comprised of two unit cells and contains one CO$_2$ molecule and two to eight water molecules in the interlayer region. The calculated power spectra are reported in Figure 9 from which it is seen that the calculated asymmetric stretch vibration of CO$_2$ is shifted 6 cm$^{-1}$ to the blue in MMT1 and 11 cm$^{-1}$ to the red in MMT4 compared to the corresponding gas-phase fundamental. For the systems incorporating intermediate numbers of water molecules the calculated value of the CO$_2$ asymmetric stretch frequency resides between these limits. This demonstrates that the hydration level strongly affects the direction and magnitude of the frequency shift. Inspection of the snapshots from the simulation trajectory of the MMT1 system reveals that the CO$_2$ molecule is primarily coordinated to a sodium cation due to an insufficient number of water molecules to efficiently hydrate the cations. The blue shift calculated for CO$_2$ interacting with a sodium cation is consistent with the experimental results for CO$_2$–cation complexes (Gregoire and Duncan, 2002; Walker et al., 2003; Jaeger et al., 2004). Increasing water content leads to formation of a hydration shell, release of CO$_2$ from coordination with the interlayer Na$^+$ ions, which, in turn, leads to a red shift of the asymmetric stretch vibration.
Figure 8: FT-IR diffuse-reflectance spectra of CO$_2$-treated smectite clay powders, Ca-MMT (STx-1b) and Na-MMT (SWy-2). KBr reflectance spectra were used for background subtraction. The vertical line marks the position of CO$_2$ asymmetric stretch fundamental ($\nu_3$) for the gas phase; P, Q, and R branches represent the rovibrational coupling.

Figure 9: Comparison of the FT-IR asymmetric stretch mode for CO$_2$ intercalated into Na-MMT (expt, SWy-2) with the signal predicted using the power spectra for Na-MMT with 4 H$_2$O and 0.5 CO$_2$ molecules per unit cell (MMT4); with 1 water and 0.5 CO$_2$ molecules per unit cell (MMT1) with 4 water and 0.5 CO$_2$ molecules per unit cell with interlayer distance increased by 5 Å (MMT4_EXT5); and for a cluster of water and CO$_2$ molecules (clstr, see the text). The adjustment coefficient is 0.9941. The vertical line marks the CO$_2$ asymmetric stretch fundamental for the gas-phase.
To gain additional insight into the role of the CO$_2$-H$_2$O interactions, the $O_w$–C and $H_w$–O$_{CO_2}$ RDFs were calculated. Figures 10a and 10b report the RDFs for $O_w$–C and $H_w$–O$_{CO_2}$ pairs obtained from DFT-based and classical MD simulations at various H$_2$O/CO$_2$ compositions.

![Figure 10: Oxygen (CO$_2$)–hydrogen (H$_2$O), and b) oxygen (H$_2$O)-carbon radial distribution functions for Na-MMT at various compositions of H$_2$O and CO$_2$. The RDFs designated as X-Y were obtained from classical MD simulations. The RDF marked as DFT was obtained from the DFT/MD simulations on the Na-MMT system with 4 H$_2$O and 0.5 CO$_2$ molecules per unit cell.](image)

The $H_w$–O$_{CO_2}$ RDFs from the simulations using the force field display a shoulder near 2.3 Å, indicating formation of H-bonds between H$_2$O and CO$_2$. However, this shoulder recedes as the water content increases, and it is absent in the DFT-based MD simulations. Kumar et al. (2009), using Car-Parrinello MD simulations, obtained a similar $H_w$–O$_{CO_2}$ RDF consistent with little H-bonding between water and CO$_2$ molecules. The $O_w$–C RDF from the force field simulations give displays a weak shoulder near 3.1 Å, while that from DFT-based MD simulations has a pronounced peak around 2.9 Å which is close to the value reported for the global minimum of the CO$_2$–H$_2$O complex at the CCSD(T) level of theory (Garden et al., 2006; de Lange et al., 2011). These results indicate a possible shortcoming in the description of the CO$_2$–water interactions in the force field calculations. Recently, Vlcek et al. (2011) reported “polarization-corrected” LJ parameters for the unlike pair interactions in water/carbon dioxide mixtures, and used SPC/E and EPM2 force fields to simulate CO$_2$ in liquid water. The resulting RDFs closely
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resemble those obtained from the classical force field simulations of CO\(_2\) in hydrated MMT. Thus, the deficiency in the force field appears not to be related to the use of combination rules in determining the van der Waals parameters for CO\(_2\) – water. It could reflect the inadequacy of a 3-point charge model for representing the electrostatic potential of CO\(_2\).

In order to further explore the effect of the confining environment on the frequency of the CO\(_2\) asymmetric stretch vibration, DFT-based MD simulations were also conducted on the MMT4 system with the basal distance extended by 5 Å. The extended interlayer space diminishes the effect of the basal oxygens and allows for a more flexible rearrangement of water molecules and interlayer ions during interaction with CO\(_2\). For this system the asymmetric stretch vibration appears at 2,334 cm\(^{-1}\), red-shifted by 15 cm\(^{-1}\) relative to the gas-phase value (Figure 9). This result provides further evidence of the pivotal role of the water molecules in the confining environment of clay in determining the frequency of the CO\(_2\) asymmetric stretch fundamental. DFT-based MD simulations were also performed using a simulation box with a cluster of eight water molecules and one CO\(_2\) molecule, and having dimensions corresponding to the interlayer space of the equilibrated MMT4 system. The frequency of the CO\(_2\) asymmetric stretch is calculated to occur 8 cm\(^{-1}\) to the red from the fundamental vibration of the gas-phase CO\(_2\) molecule (Figure 9). This is consistent with the peak in the experimental band of the asymmetric stretch showing a red shift about 6 cm\(^{-1}\) relative to the gas-phase molecule (Garrett-Roe et al., 2009; Moin et al., 2011).

To explore the origin of the red shift in the asymmetric stretch vibration of CO\(_2\) intercalated in Na-MMT, snapshots were extracted from a DFT-based MD trajectory. The sampled structures show that the CO\(_2\) molecule is surrounded by water molecules, many of which point OH groups toward the O atom of the CO\(_2\) molecule. In several of the snapshots, the C-O bonds in the carbon dioxide molecule are slightly elongated in comparison with those of the gas-phase molecule (1.167 Å). Selected CO\(_2\) molecules were then extracted and their vibrational frequencies were calculated at the B3LYP/aug-cc-pVDZ level of theory. As expected, the asymmetric stretch vibration is red-shifted in the distorted molecules compared to the equivalent vibrational mode of the optimized gas phase CO\(_2\) molecule computed at the same level of theory. The frequency shift correlates in a linear manner with the extent of the distortion as seen from Figure 11. The insert 1 in Figure 11 reveals a histogram of the value summing the deviation of C-O bonds from the gas-phase value for MMT4 (Figure 9). The data shows that a normal distribution is centered around 0.02 Å indicating stretch of the bonds in interior space of montmorillonite. The similar trend is found for the neutral cluster of water and a carbon dioxide molecule (Insert 2, Figure 11). These results provide strong evidence that the observed red shift is primarily due to geometry distortions of the CO\(_2\) molecule induced by the water molecules. In several cases with large CO bond length increases and large red shifts of the asymmetric stretch vibration, all H--O(CO\(_2\)) distances are greater than 4Å, strongly suggesting that it is electric field effects that are primarily responsible for the observed red shift. This also suggests that in the reported experiments (Loring et al., 2012; Romanov et al., 2010a,b; Romanov, 2013) hydration of CO\(_2\) in the interlayer space is sufficient to form a solvation shell and preclude a direct interaction of CO\(_2\) with sodium cations, which would act so as to cause a blue-shift (Gregoire and Duncan, 2002; Walker et al., 2003; Jaeger et al., 2004). Remarkably, a similar red shift in the stretch fundamental was found by Moin et al. (2011), in their mixed ab initio/force field MD simulations of carbon dioxide in water.
These results explain why the classical MD simulations did not predict a red shift for the intercalated carbon dioxide. Specifically, the force field employed uses a harmonic C-O stretch term, whereas it is necessary to include an anharmonic C-O stretch term in the CO$_2$ force field to account for the frequency shift accompanying the stretch of the CO bonds upon hydration. This deficiency can be readily remedied, for example, by adopting a Morse-type potential to describe the C-O stretch potential.
7. **CONCLUSION**

One option for CO\textsubscript{2} storage is to use subsurface geological brine aquifers bound by low-permeability sealing caprocks. Caprock is often enriched with expandable clay minerals, and understanding the interaction between clay minerals, brines, and injected CO\textsubscript{2} is crucial for predictions of the natural seal integrity and site selection for long-term CO\textsubscript{2} storage. The integrity of the caprock is important because CO\textsubscript{2}, being more buoyant than brine and oil, will tend to migrate above these relatively immiscible fluids.

Experimental measurements show that trapping of carbon dioxide in Na- and Ca-montmorillonite leads to a red shift in the asymmetric stretch frequency of the CO\textsubscript{2} molecule. DFT-based MD simulations were carried out to explain the origin of this red shift. The simulations reproduce the experimentally observed red shift and identify electric field induced elongation of the CO bonds of CO\textsubscript{2} as being primarily responsible for the frequency shift.

Force field molecular dynamics simulations were engaged to characterize in clay–water–CO\textsubscript{2} systems at pressure and temperature relevant to geological carbon sequestration. The simulations show that the degree of induced swelling caused by intercalation of CO\textsubscript{2} strongly depends on the initial water content in the interlayer space. Accumulation of CO\textsubscript{2} in the interlayer with humidity levels below those corresponding to the 1W hydration state first produces structures with basal \(d\)-spacings equivalent to 1W. Further carbon dioxide load promotes a stepwise expansion of the \(d\)-spacing to values equal to higher hydration states (2W and 3W). At water and CO\textsubscript{2} concentrations that give rise to mono- or bilayer arrangements in the interlayer region, the CO\textsubscript{2} molecules are preferentially oriented parallel to the clay surfaces. The hydrogen bond lifetimes are longest for H\textsubscript{2}O-H\textsubscript{2}O interactions followed by H\textsubscript{2}O-O\textsubscript{basal}, then by H\textsubscript{2}O-CO\textsubscript{2}. An important finding is that increasing the concentration of CO\textsubscript{2} promotes migration of the positively charged sodium ions to the clay basal surfaces. Sodium cations are found to absorb reversibly at the centers of hexagonal rings and form surface complexes that contribute to charge screening of the electrical layer and acting so as to increase the hydrophobicity of the surface. This process could be related to the increase of contact angle and dewetting on mica and silica surfaces during CO\textsubscript{2} invasion reported in series of experiments under conditions of high ionic strength of electrolyte (Wan et al., 2011). Thus, intercalation of CO\textsubscript{2} within smectite minerals in brine aquifers can cause significant changes in the clay phase \(d\)-spacing and modify wetting properties of the clay surfaces.
8. REFERENCES


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