



# **Microstructure-Sensitive Crystal Viscoplasticity for Ni-base Superalloys**

**(with application to long-term creep-fatigue interactions)**

**Award DE-FE0011722**

**August 2013 – December 2017 (including NCE)**

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**University Turbine Systems Research Workshop**

**Pittsburgh**

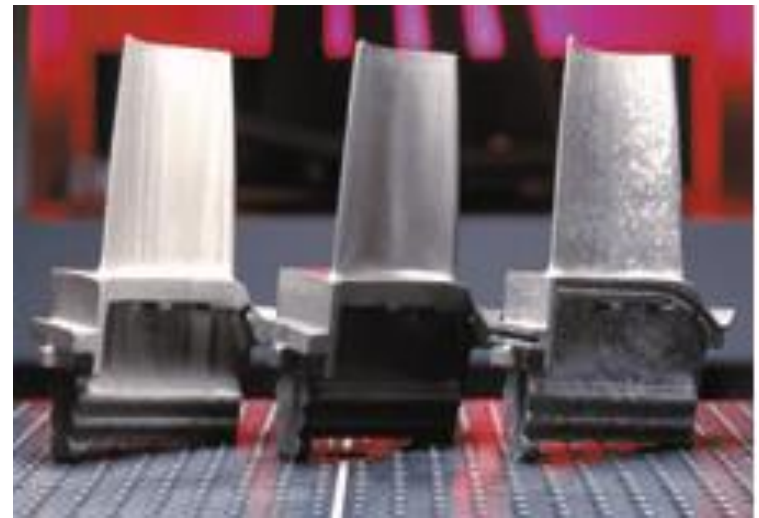
**November 1-2, 2017**



Power Output: 375 MW

## Land-based gas turbines

- drive to increase service temperature to improve efficiency; increase life; with minimal increase in cost
- replace large directionally-solidified Ni-base superalloys with single crystal superalloys





[Attari et al., 2013]

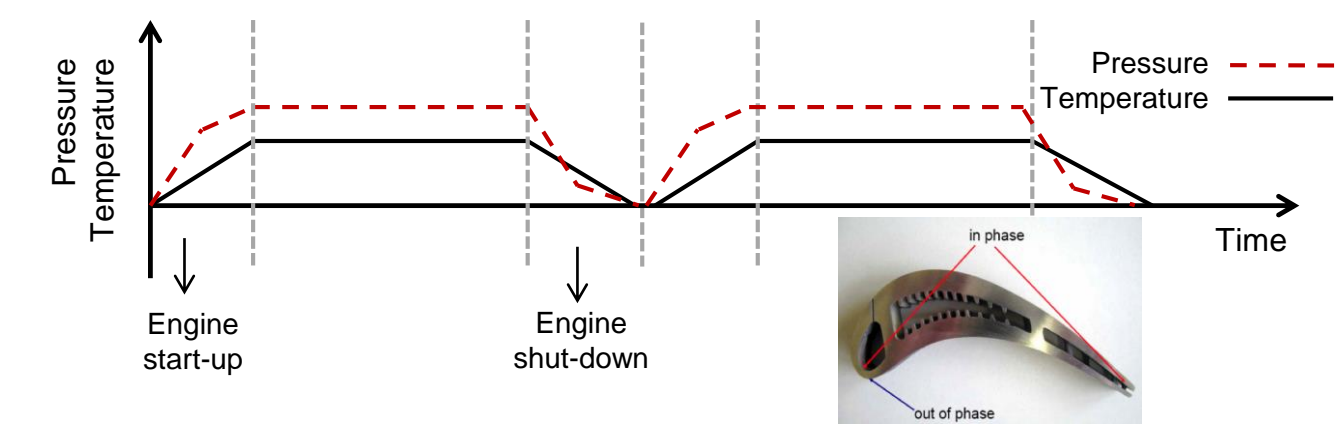
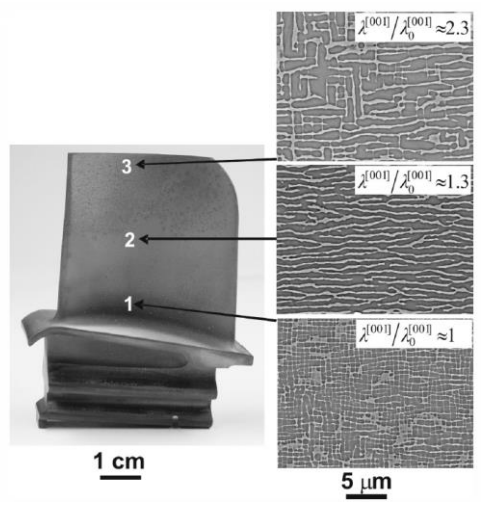


[Vardar et al., 2007]



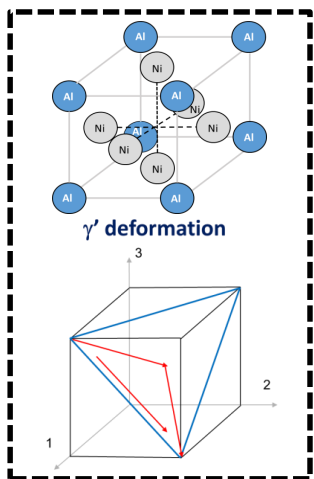
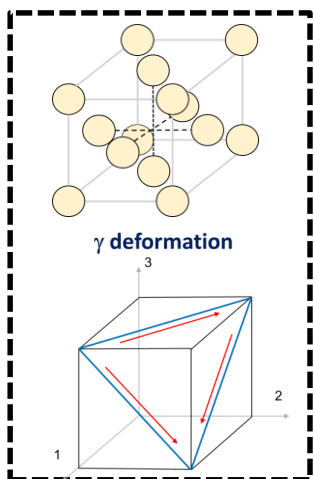
Microstructure Changes during Service

Complex Temperature and Loading Profiles

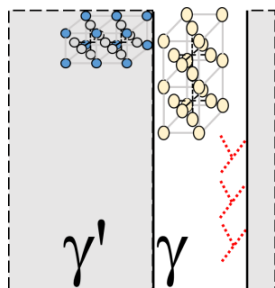


[Epishin et al., 2010]

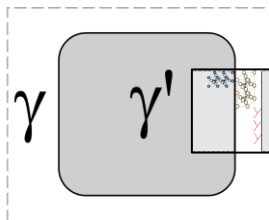
Atomic structure  
O( $10^{-10}$  m)



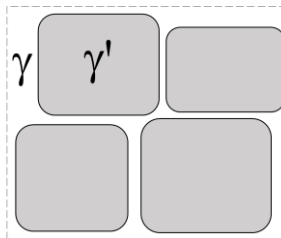
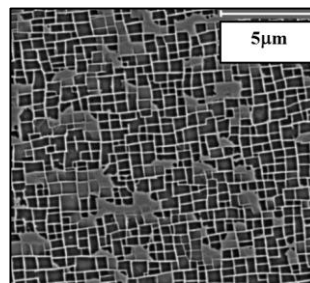
Channel dislocations  
O( $10^{-8}$  m)



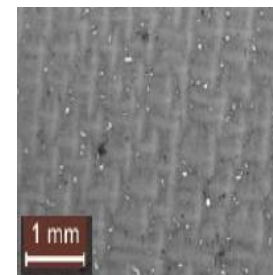
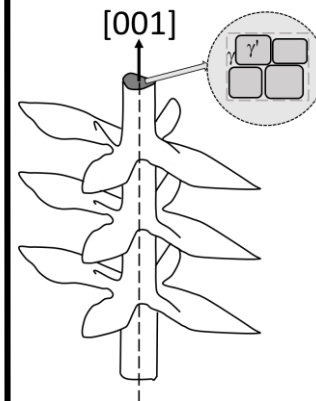
Precipitate  
O( $10^{-7}$  m)



Groups of precipitates  
O( $10^{-6}$  m)



Dendrites  
O( $10^{-5}$  m)



Bulk  
O( $10^{-1}$  m)

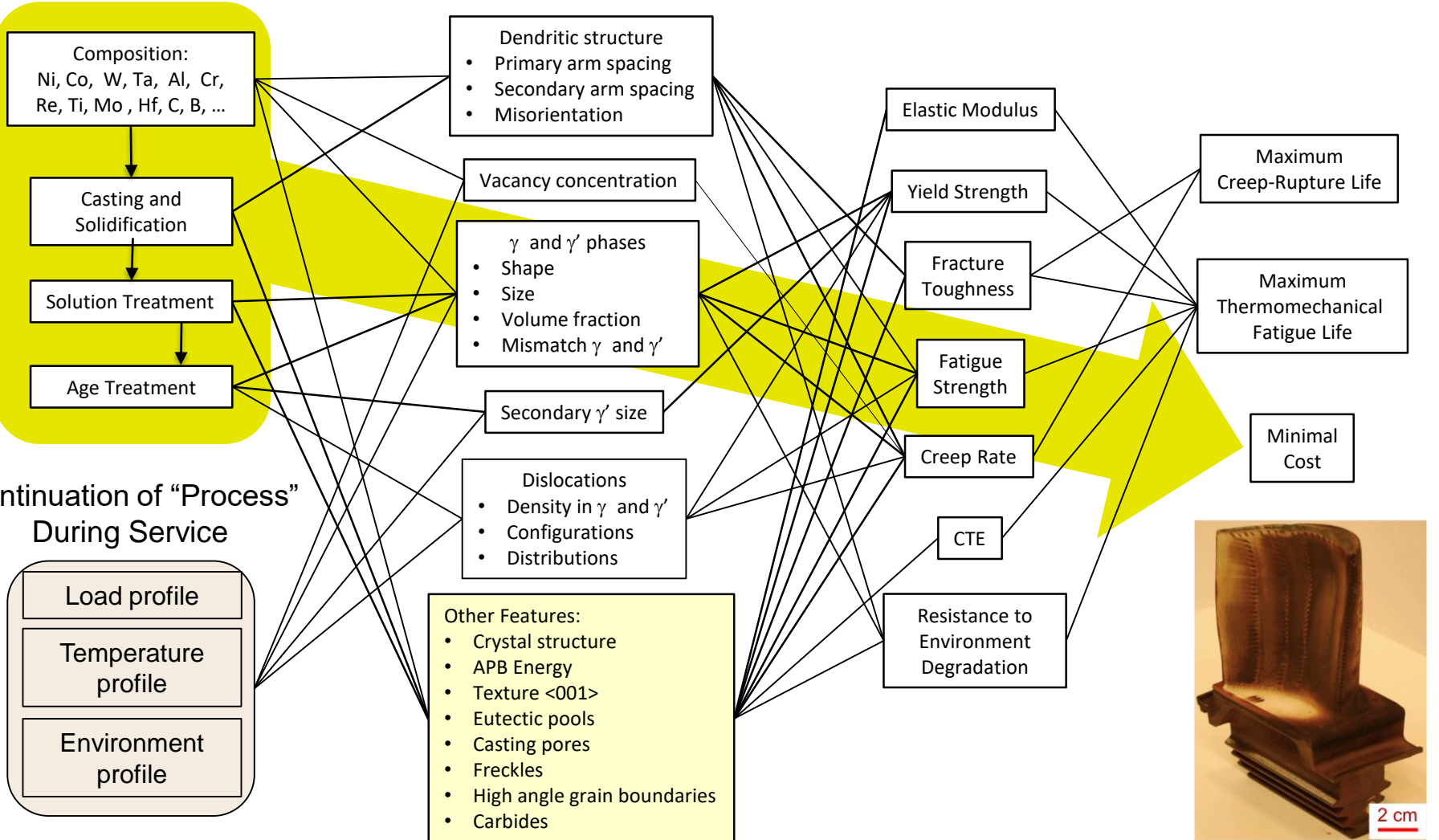


## PROCESS

## STRUCTURE

## PROPERTIES

## PERFORMANCE



## PROCESS

## STRUCTURE

## PROPERTIES

## PERFORMANCE

Composition:  
Ni, Co, W, Ta, Al, Cr,  
Re, Ti, Mo, Hf, C, B, ...

Casting and  
Solidification

Solution Treatment

Age Treatment

Dendritic structure  
• Primary arm spacing  
• Secondary arm spacing  
• Misorientation

Vacancy concentration

$\gamma$  and  $\gamma'$  phases  
• Shape  
• Size  
• Volume fraction  
• Mismatch  $\gamma$  and  $\gamma'$

Secondary  $\gamma'$  size

Dislocations  
• Density in  $\gamma$  and  $\gamma'$   
• Configurations  
• Distributions

Other Features:  
• Crystal structure  
• APB Energy  
• Texture  $\langle 001 \rangle$   
• Eutectic pools  
• Casting pores  
• Freckles  
• High angle grain boundaries  
• Carbides

Elastic Modulus

Yield Strength

Fracture Toughness

Fatigue Strength

Creep Rate

CTE

Resistance to Environment Degradation

Maximum Creep-Rupture Life

Maximum Thermomechanical Fatigue Life

Minimal Cost

Continuation of "Process" During Service

Load profile  
Temperature profile  
Environment profile



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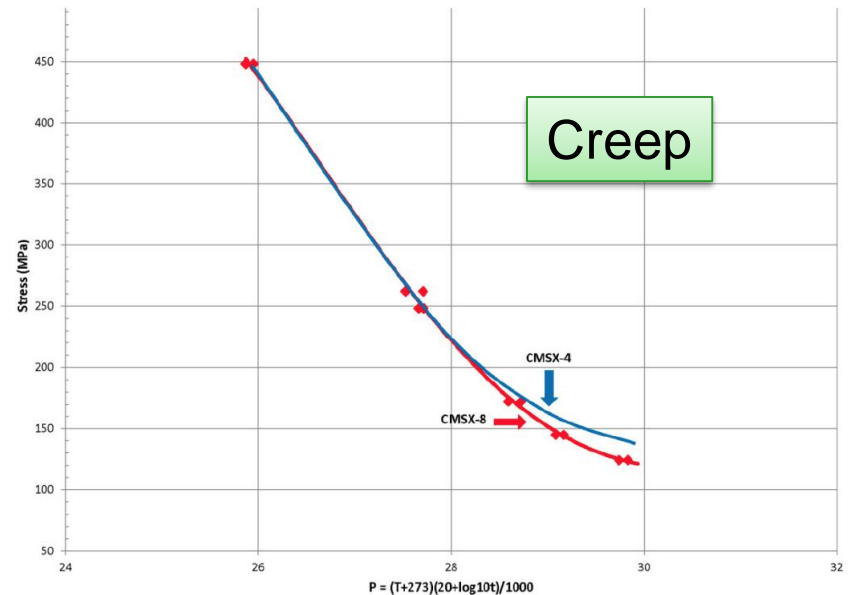
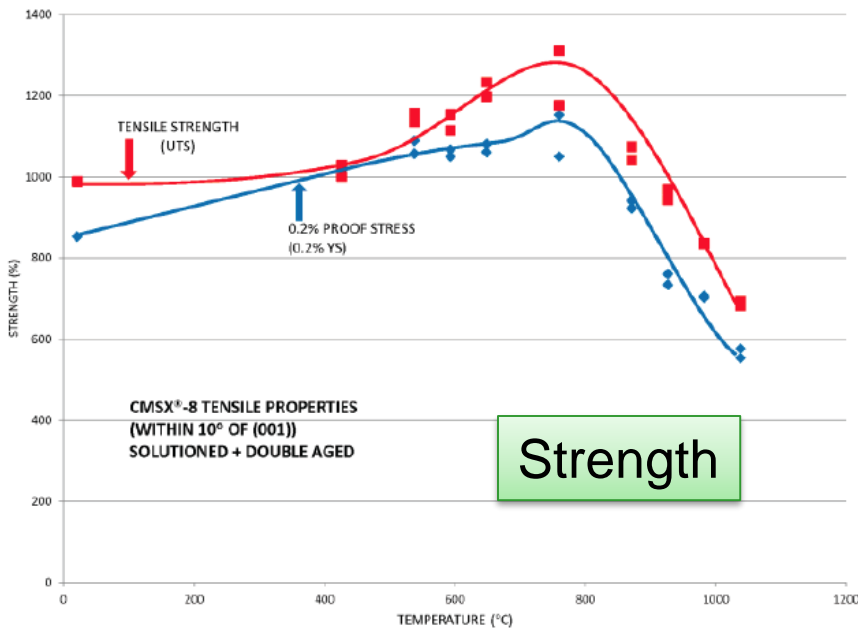
Continuation of "Process" During Service

Load profile  
Temperature profile  
Environment profile



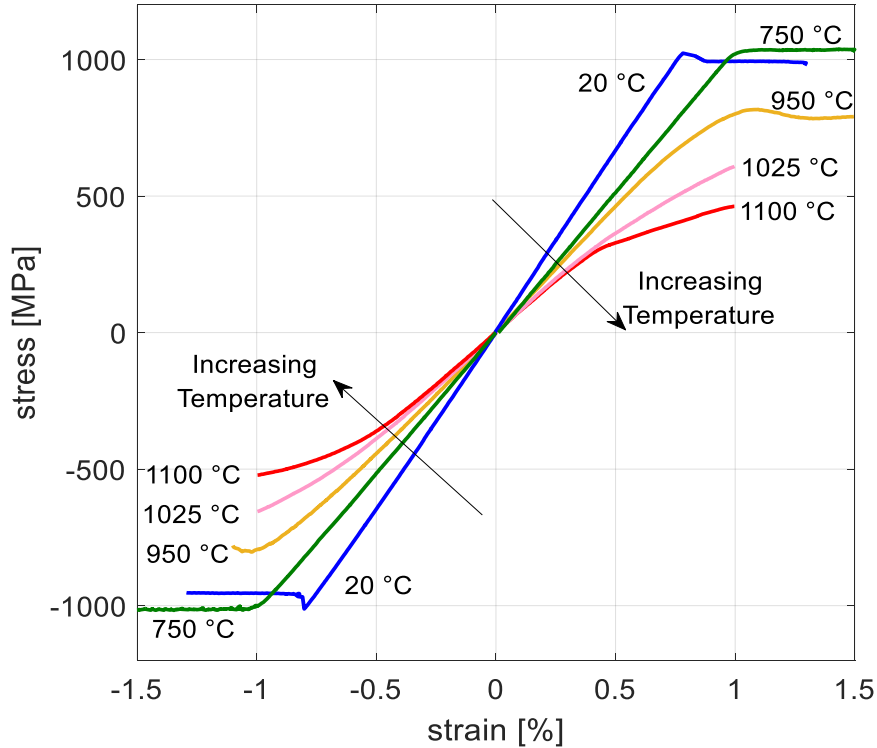
CMSX-8: 1.5% Re "alternative 2<sup>nd</sup> gen alloy" replacing 3.0% Re containing alloys (e.g., CMSX-4, PWA1484)

Alloy	Cr	Co	Mo	W	Al	Ti	Ta	Re	Hf	C	B	Zr	Ni
Mar-M247LC-DS	8.4	10.0	0.7	10.0	5.5	1.0	3.0	-	1.5	0.07	0.015	0.05	Bal
CM247LC-DS	8.1	9.2	0.5	9.5	5.6	0.7	3.2	-	1.4	0.07	0.015	0.01	Bal
CMSX-4	6.5	9.0	0.6	6.0	5.6	1.0	6.5	3.0	0.1	-	-	-	Bal
SC16	16	0.17	3.0	0.16	3.5	3.5	3.5	-	-	-	-	-	Bal
PWA1484	5.0	10.0	2.0	6.0	5.6	-	9.0	3.0	0.1	-	-	-	Bal
<b>CMSX-8</b>	<b>5.4</b>	<b>10.0</b>	<b>0.6</b>	<b>8.0</b>	<b>5.7</b>	<b>0.7</b>	<b>8.0</b>	<b>1.5</b>	<b>0.2</b>	<b>-</b>	<b>-</b>	<b>-</b>	<b>Bal</b>

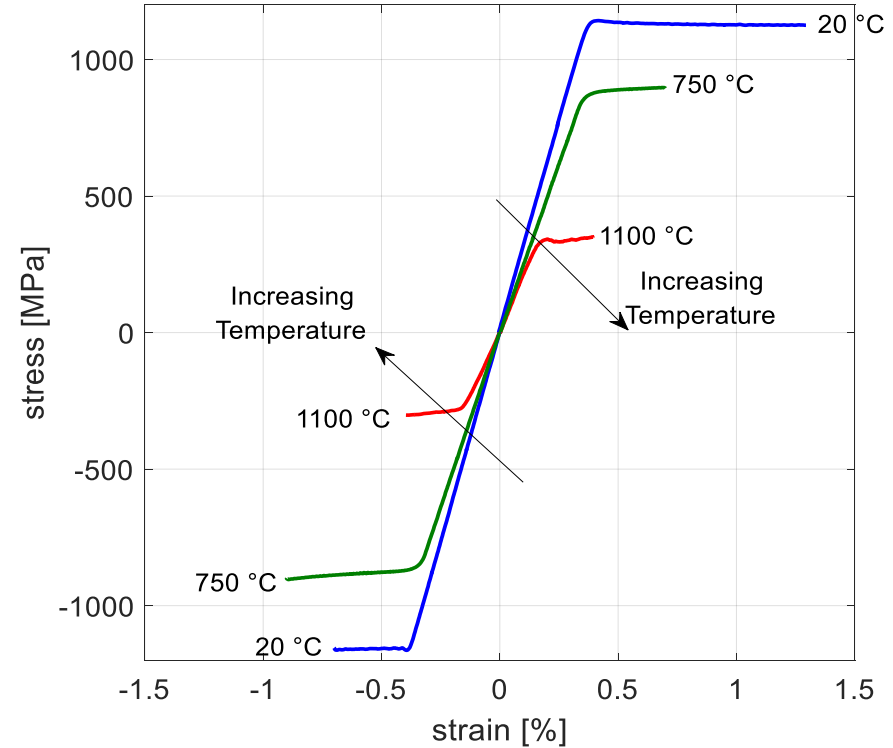




Virgin CMSX-8 monotonic response in the <001> dir



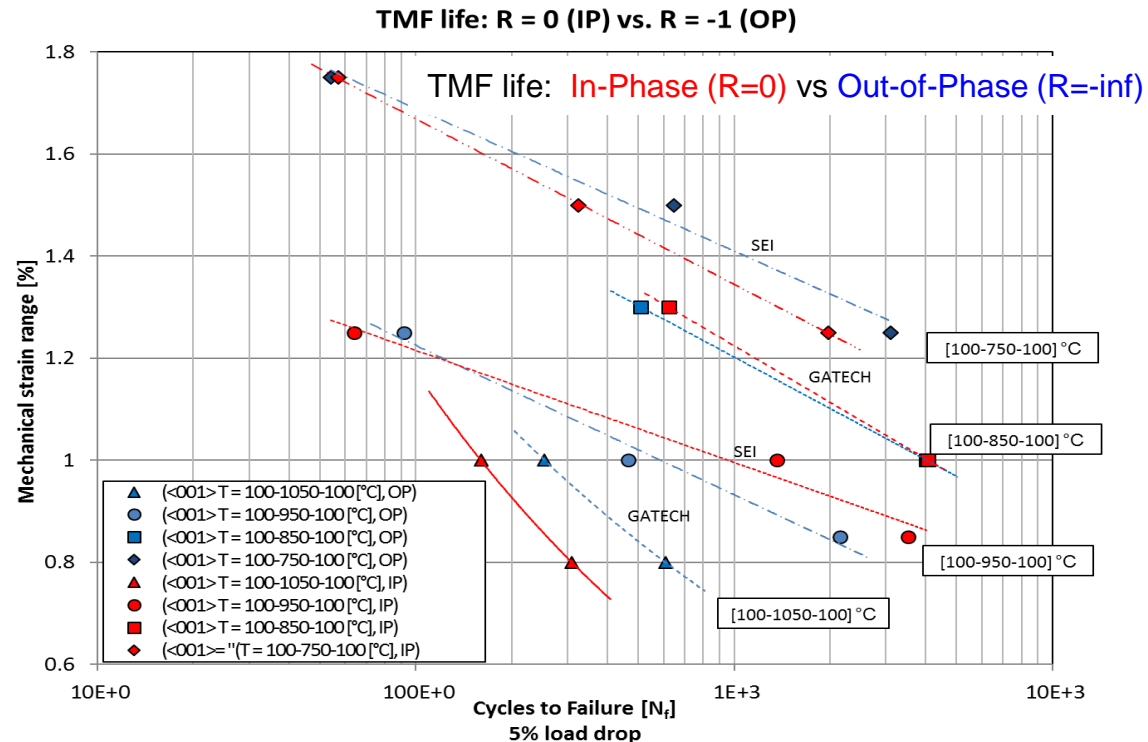
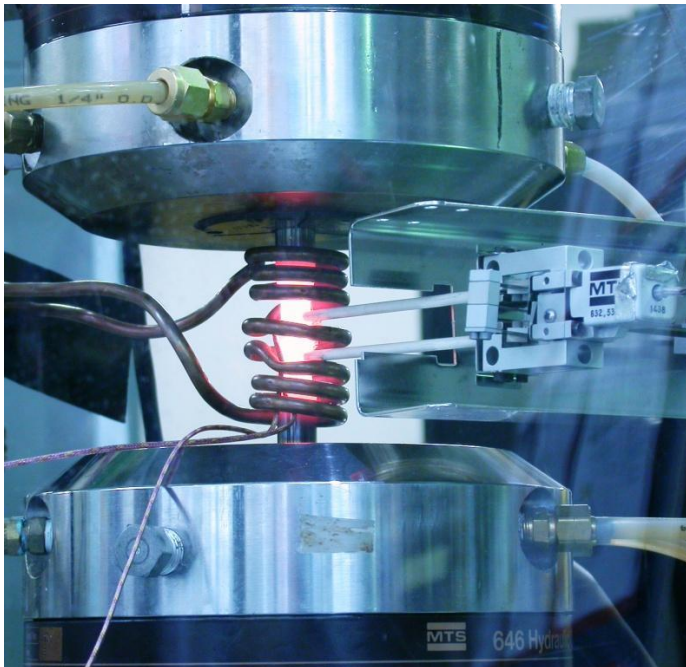
Virgin CMSX-8 monotonic response in the <111> dir

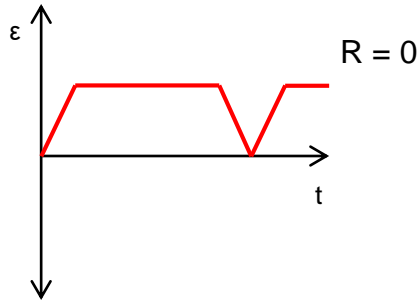


- Creep-fatigue interaction experiments on CMSX-8
- Influence of aging on microstructure and creep-fatigue interactions
- Microstructure-sensitive, temperature-dependent crystal viscoplasticity to capture the creep and cyclic deformation response

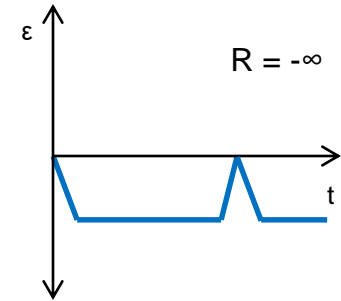
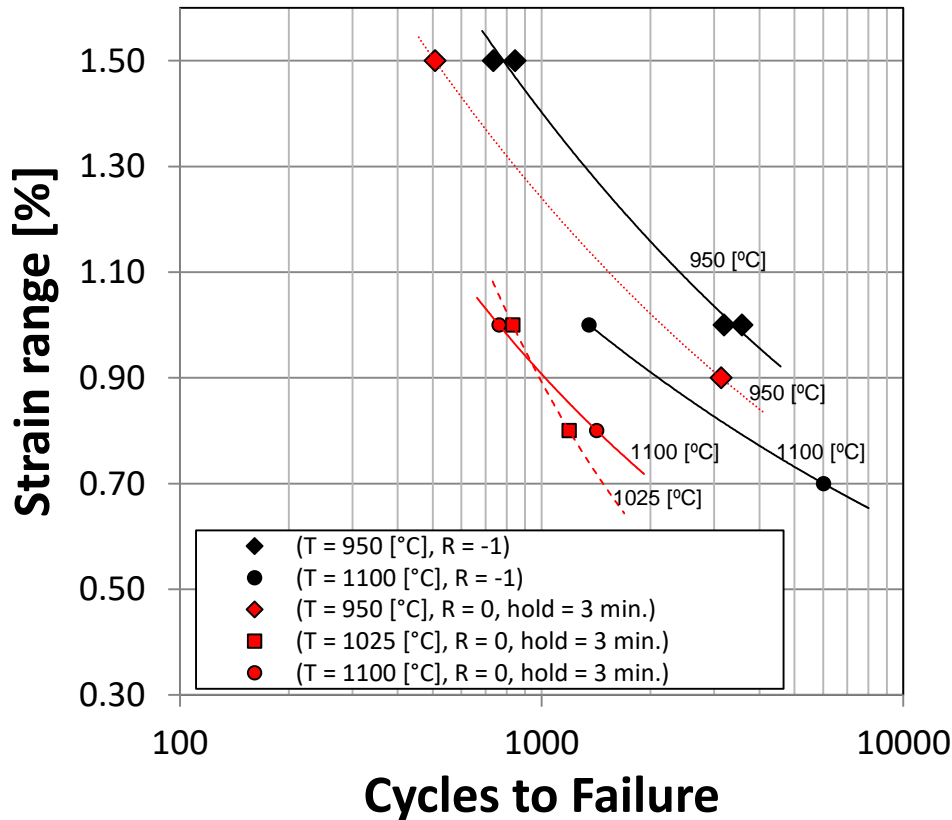
Experimentally establish the creep-fatigue interactions in a single-crystal Ni-base superalloy that is being targeted for use in industrial gas turbines (CMSX-8)

- Characterize creep-fatigue interactions on CMSX-8
  - Creep-fatigue
  - Thermomechanical fatigue
  - Creep (either tension or compression) followed by fatigue
  - Fatigue followed by creep
- Characterize the influence of aging on microstructure and creep-fatigue interactions

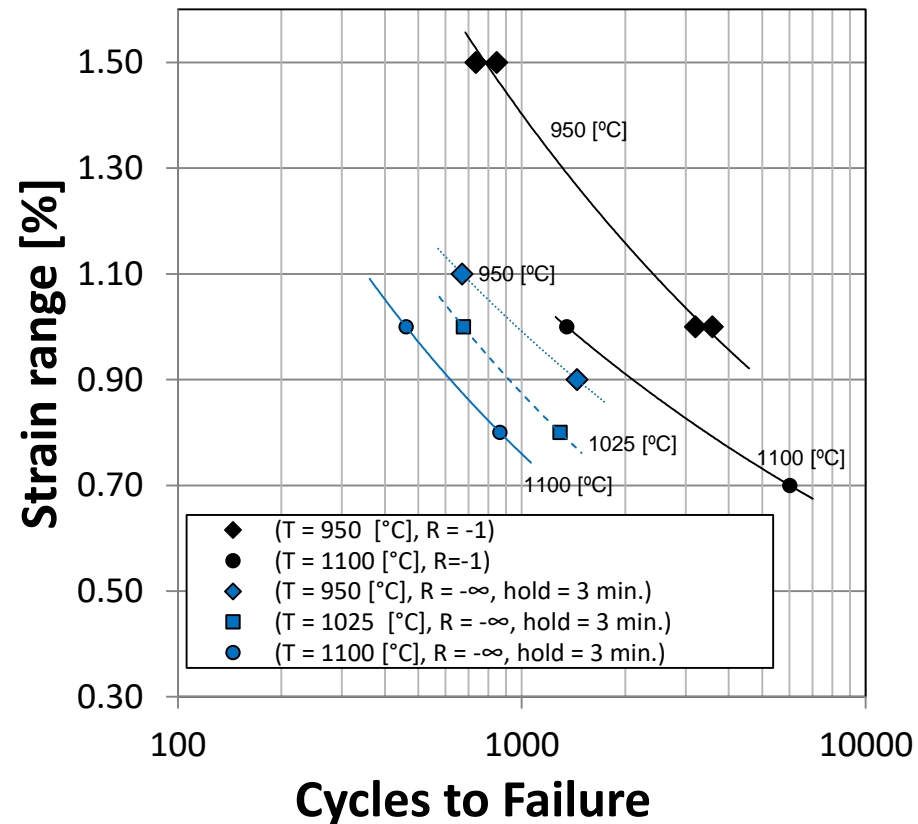


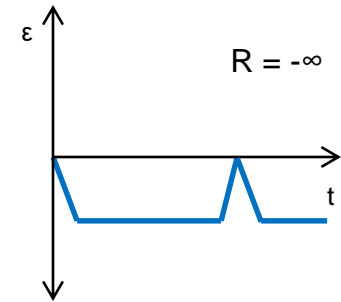
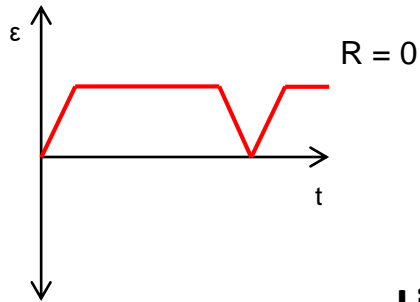


Effect of hold on LCF life:  $R = 0$

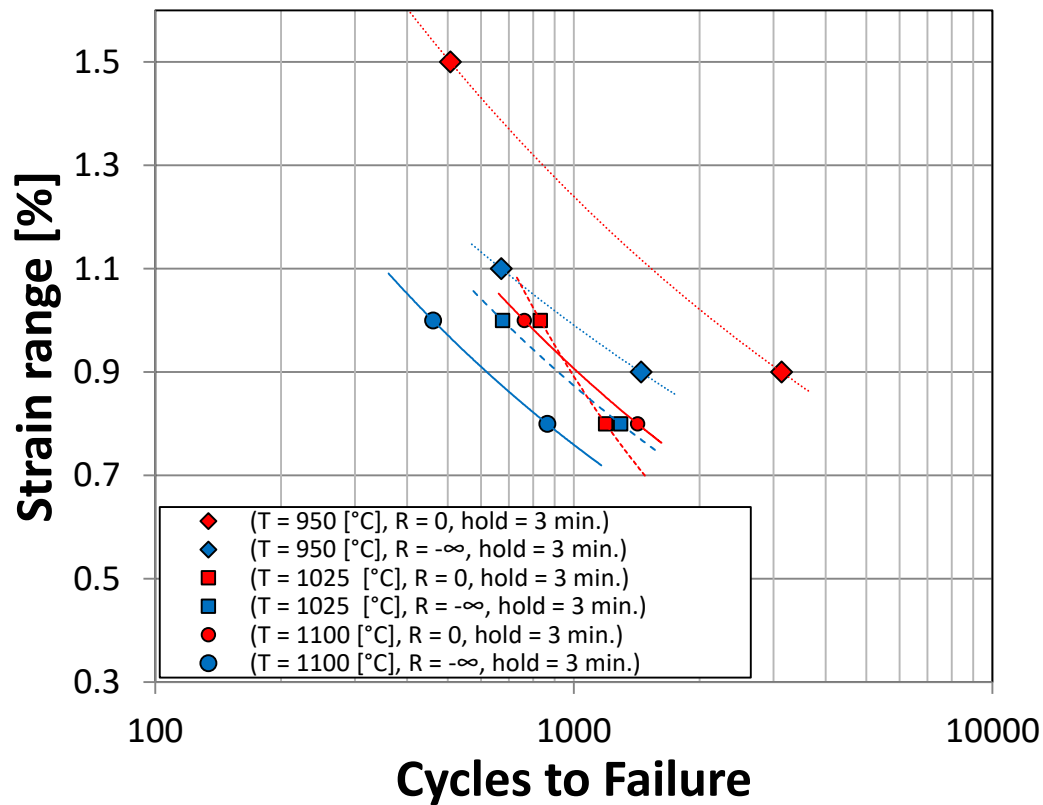


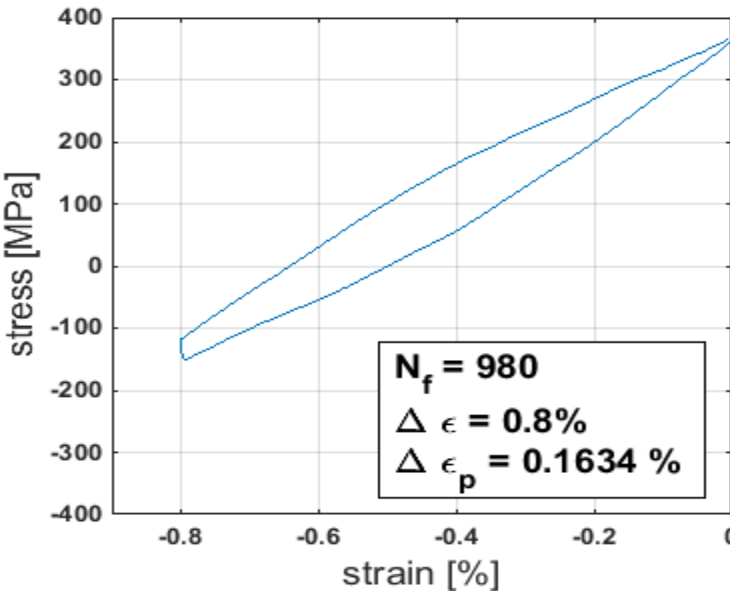
Effect of hold on LCF life:  $R = -\infty$





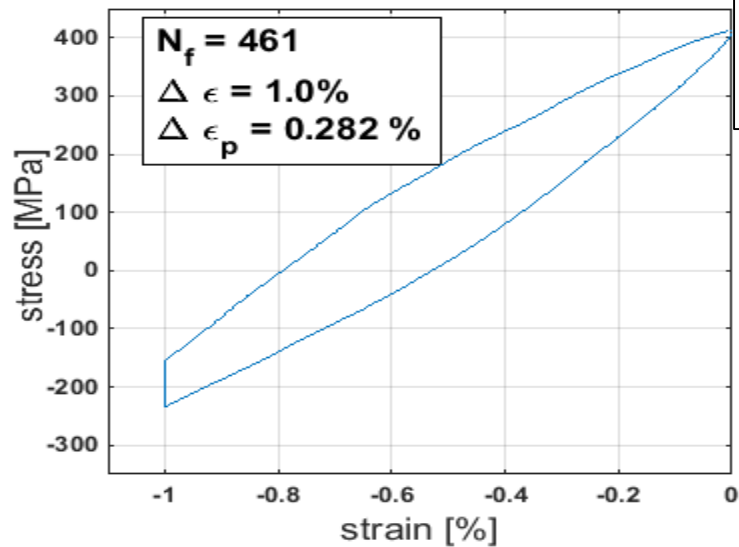
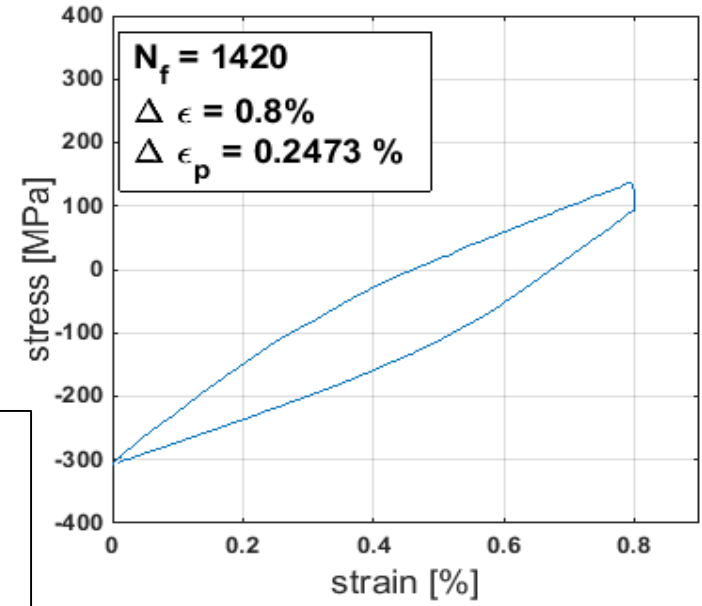
Life for low cycle creep-fatigue



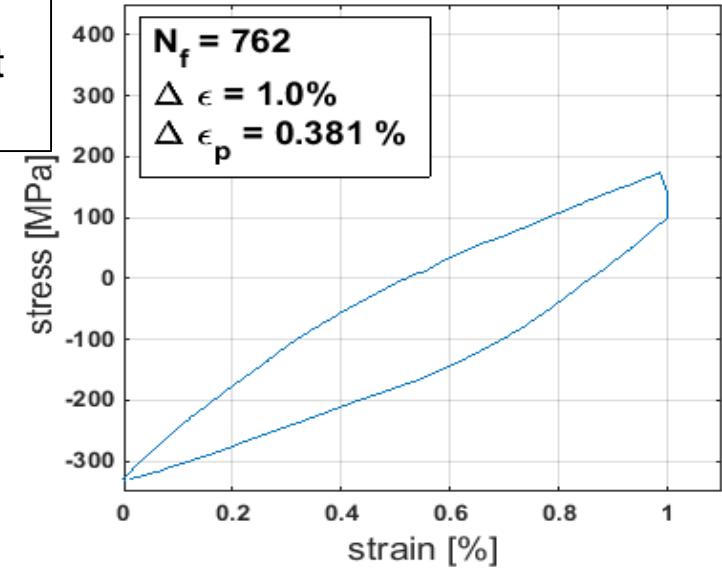


$\Delta \epsilon = 0.8 [\%]$

Plastic strain range alone does not explain life data at high temperatures. A Coffin-Manson relations would not be sufficient

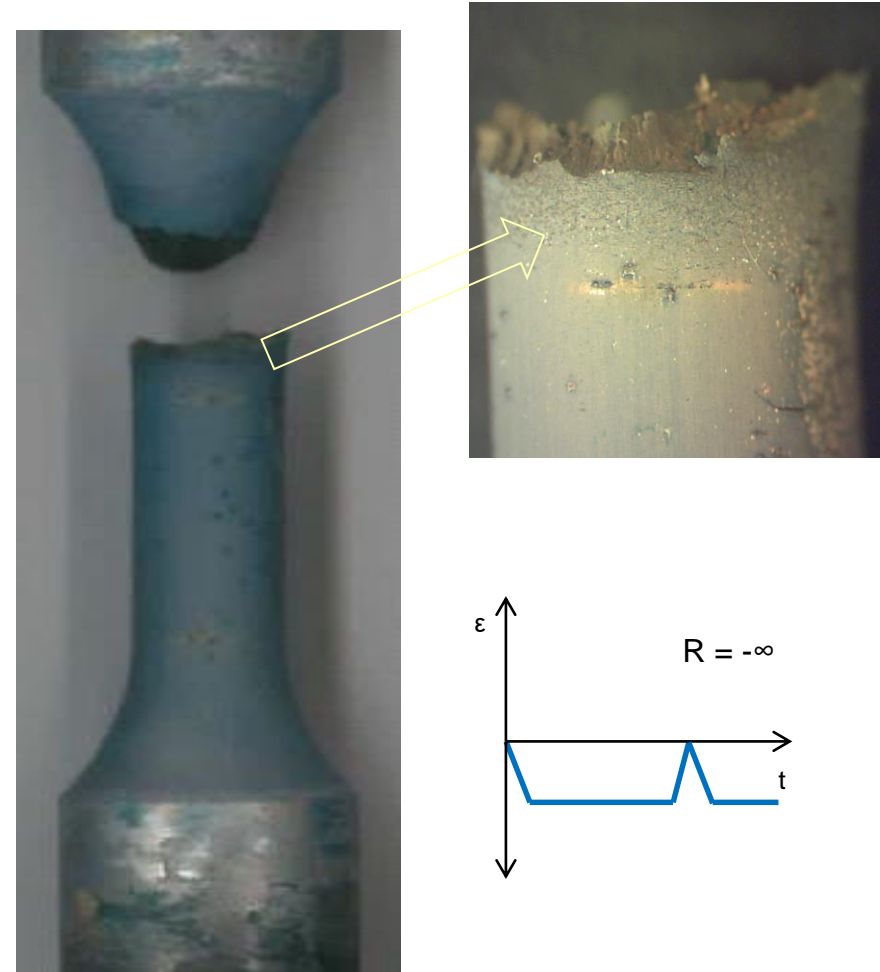
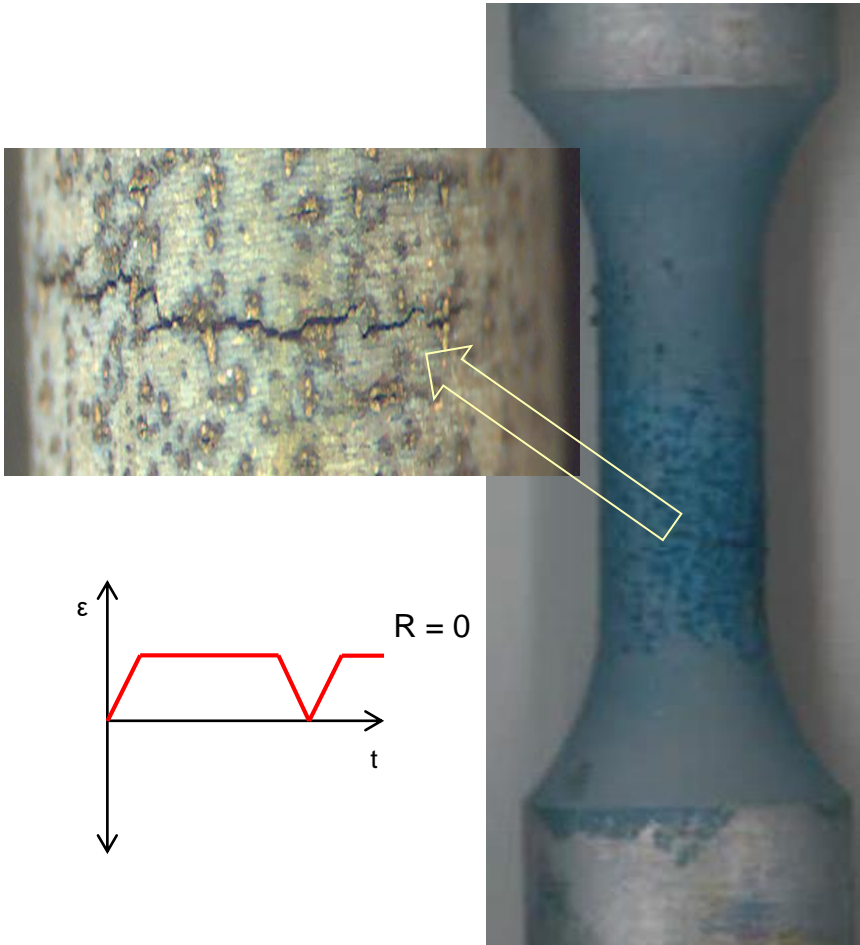


$\Delta \epsilon = 1.0 [\%]$



$R = 0, T = 1100^{\circ}\text{C}, \Delta\varepsilon = 0.8\%$   
 $N_f = 1420$

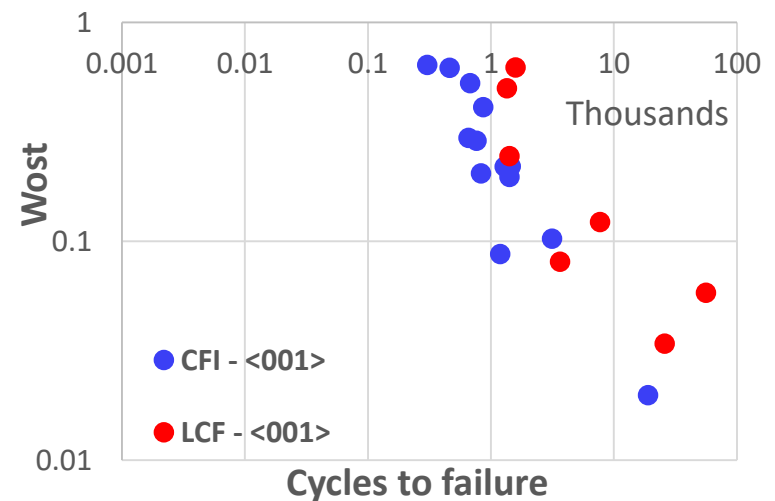
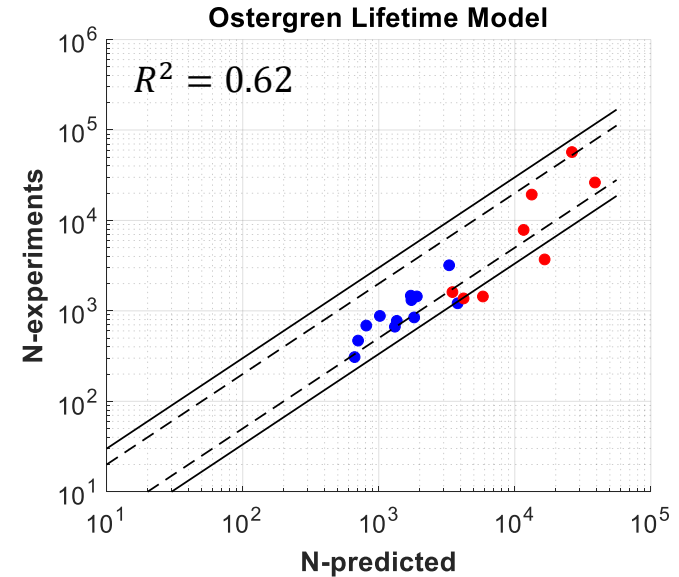
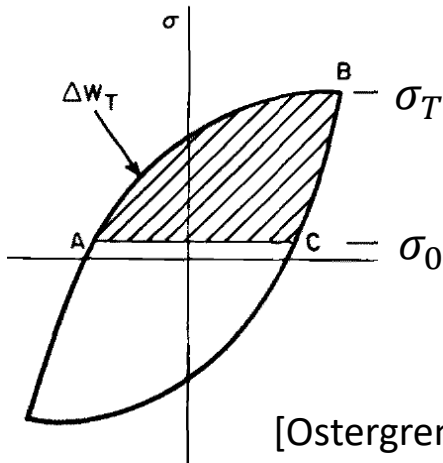
$R = -\infty, T = 1100^{\circ}\text{C}, \Delta\varepsilon = 0.8\%$   
 $N_f = 980$



## Ostergren Model

- Energy-based life prediction model based on the net hysteretic energy.
- Accounts for the mean stress and cycle time (frequency) effect.
- The accuracy of prediction relies on precision of inelastic strain measurement.

$$\sigma_T \Delta \epsilon_P N_f^\beta \nu^{\beta(k-1)} = C$$





## Zamrik and Renauld Model

- Introducing hold-time and elevated temperature function to account for creep effect and exponentially increasing creep/or environmental damage with increasing temperature, respectively.
- Substituting inelastic strain with maximum tensile strain range.

$$N = A \left[ \overbrace{\left( \frac{\epsilon_{ten}}{\epsilon_f} \right) \left( \frac{\sigma_{max}}{\sigma_u} \right)}^{W_{zam}} \right]^B \left( 1 + \frac{t_h}{t_c} \right)^C \exp\left( \frac{-Q}{R(T_{max} - T_0)} \right)$$

$\sigma_{max}$  : maximum tensile stress in mid-life hysteresis loop

$\epsilon_{ten}$  : tensile strain range in mid-life hysteresis loop for which the stress is tensile

$\sigma_u$  : ultimate strength measured under monotonic tensile loading

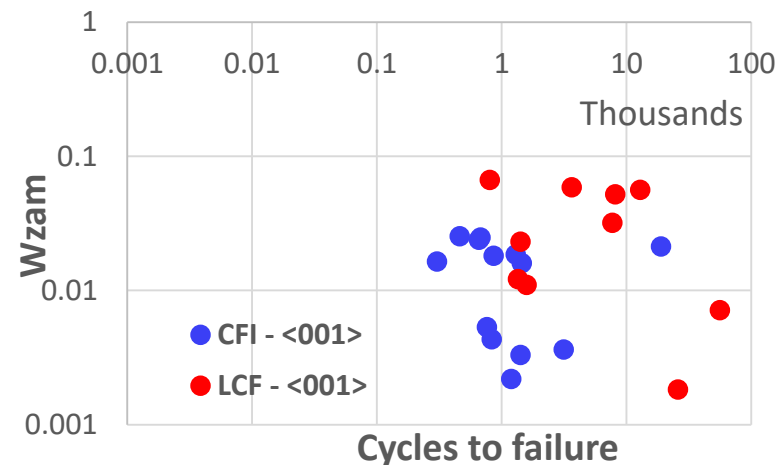
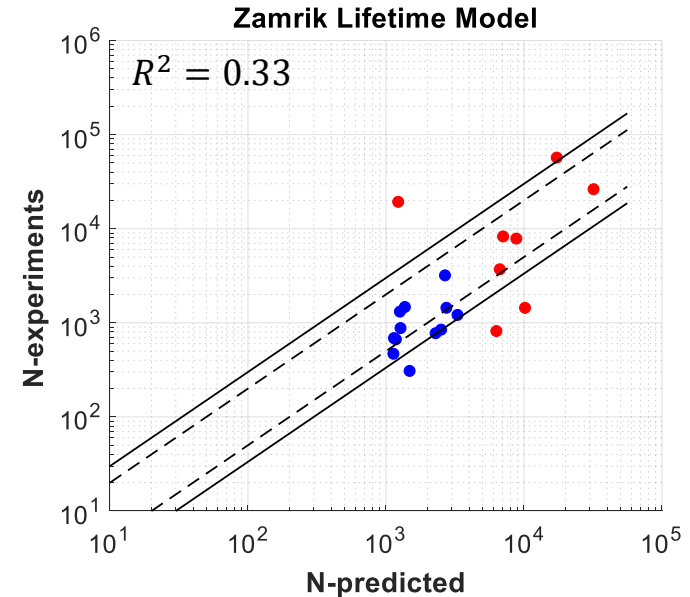
$\epsilon_f$  : elongation to failure measured under monotonic tensile loading

$t_h$ : length of compressive hold-time

$t_c$ : length of total time including hold-time

$Q$ : activation energy for high temperature damage

[Zamrik and Renauld, 2000]



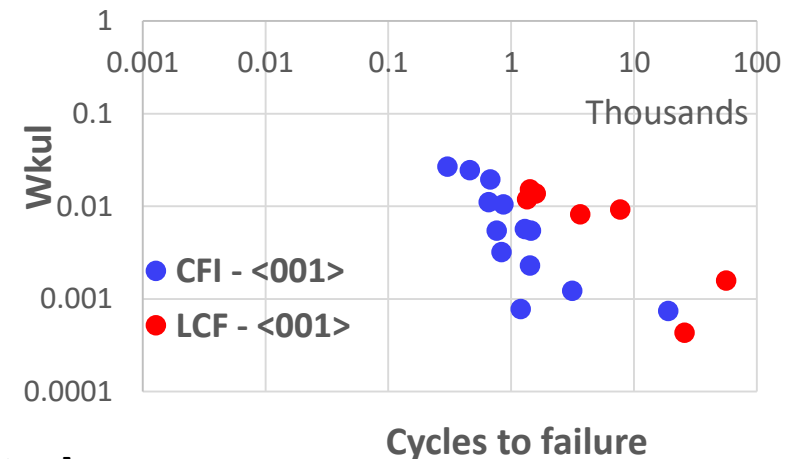
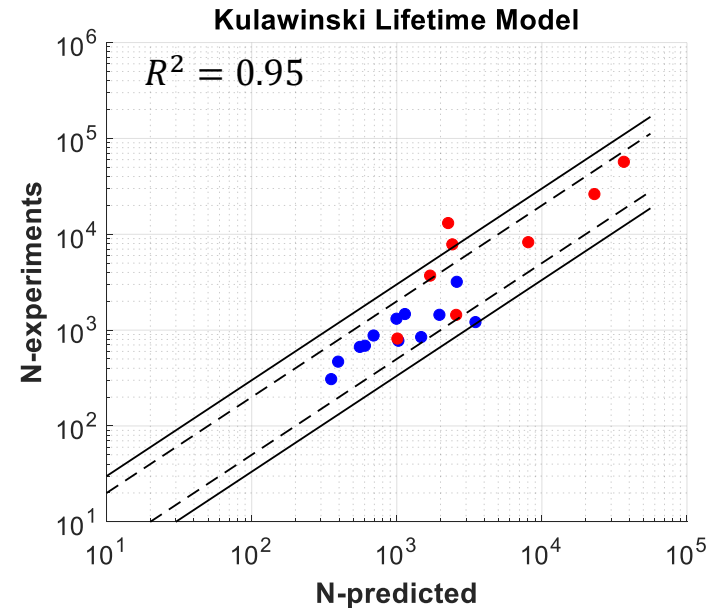
## Kulawinski et al. Model

- The model is based on Zamrik model and the energy density term includes:

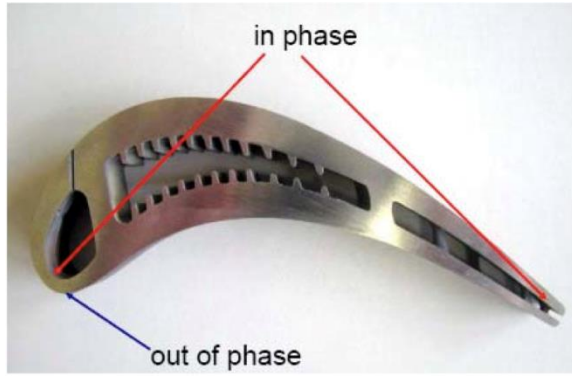
- Zamrik damage parameter
- Inelastic strain range
- Stress range
- Arrhenius term

$$N_f = A \left[ \underbrace{\Delta\sigma_{eq} \cdot \Delta\varepsilon_{eq}^{in} \cdot W_{zam}}_{W_{Kul}} \cdot \exp\left(\frac{-Q}{RT}\right) \right]^B$$

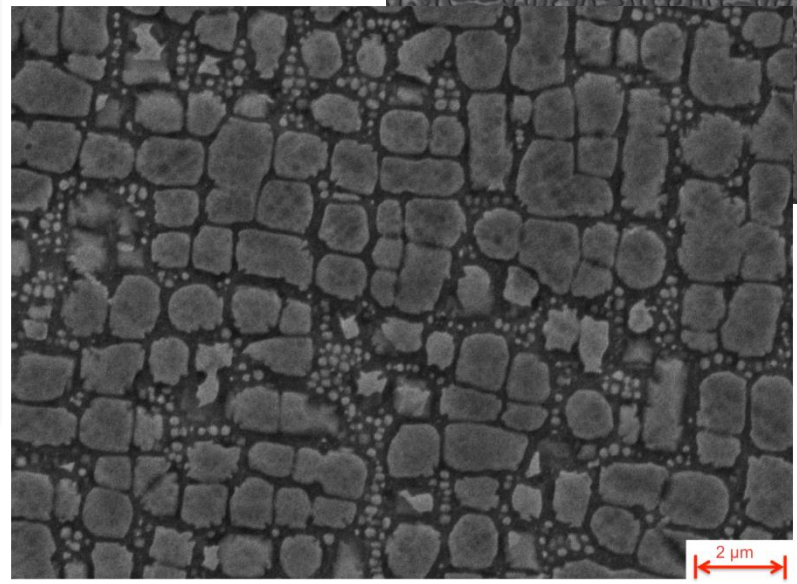
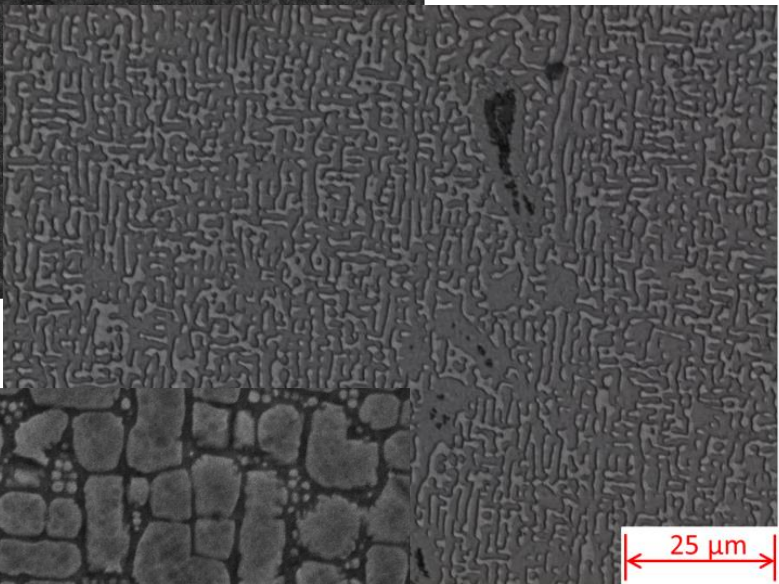
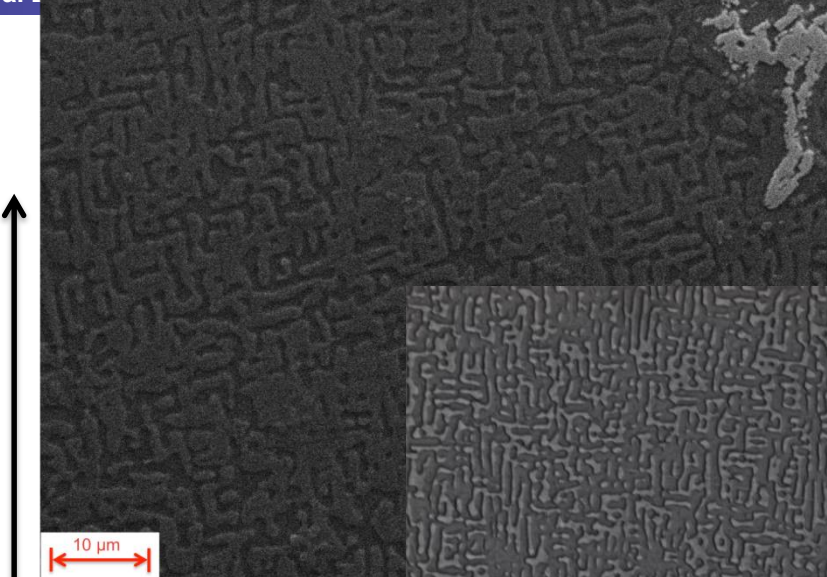
- The goodness of fit plot shows majority of life predictions using Kulawinski model lie within the scatter band of factor two.
- 95% of the variance of the low cycle fatigue (LCF) and creep-fatigue (CFI) life data is captured by this lifetime model.



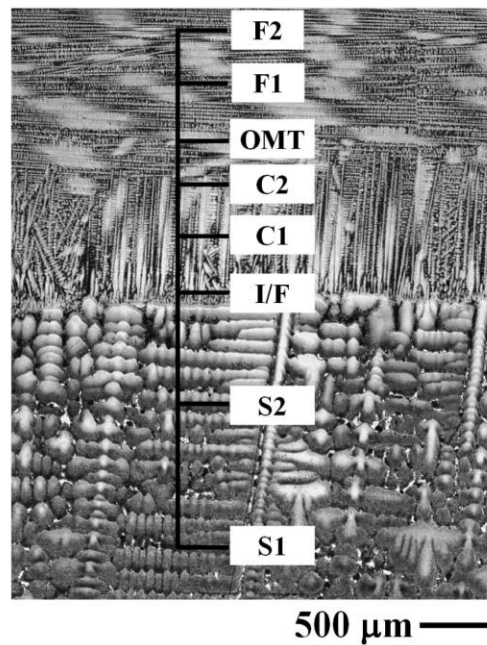
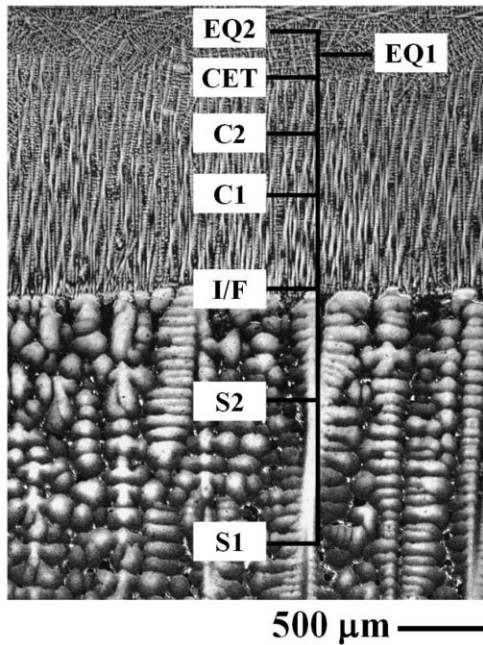
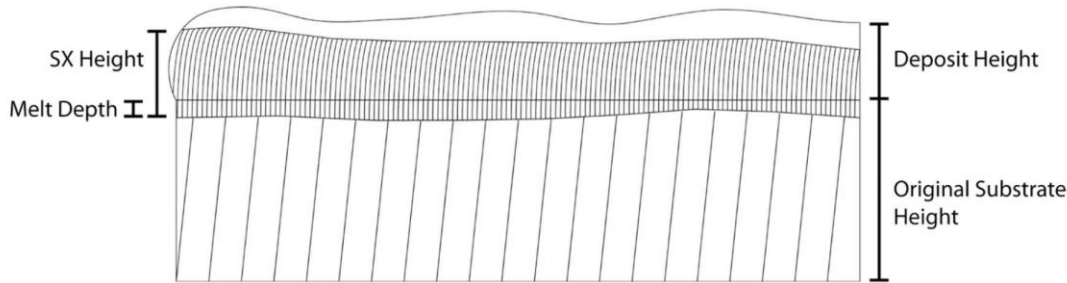
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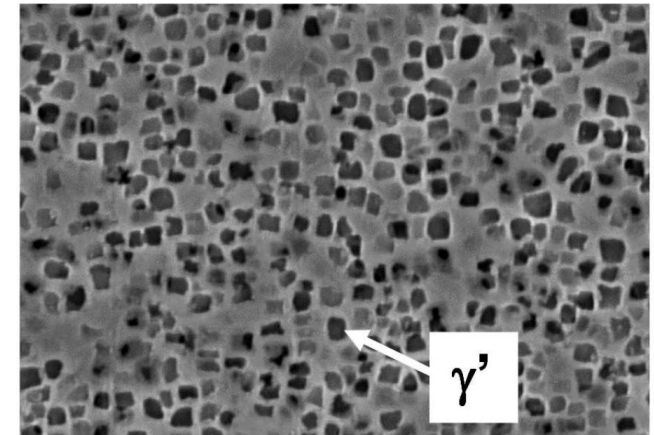
Distance from Root



## CMSX-4 via Scanning Laser Epitaxy (SLE)

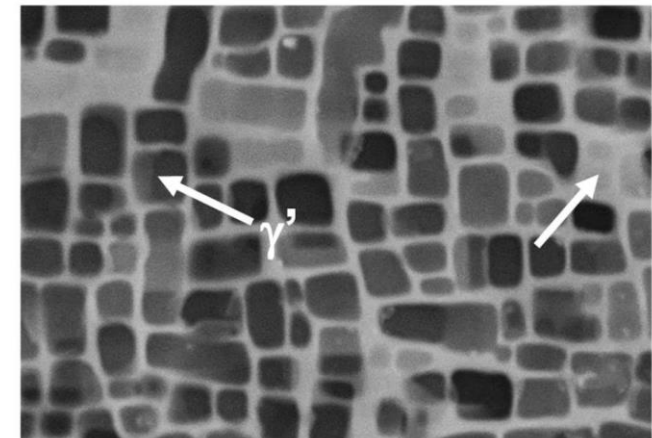


As-built

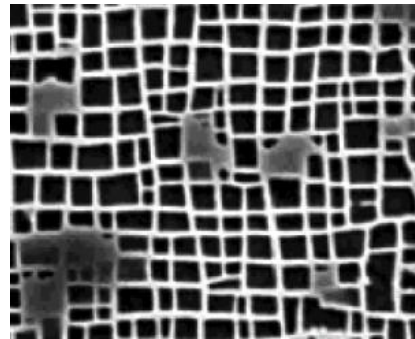


500 nm

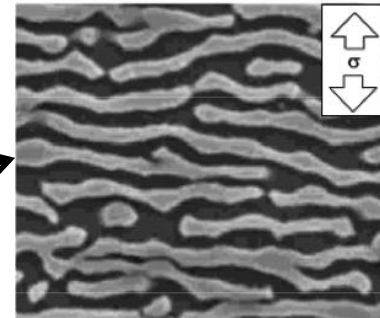
After Heat Treatment



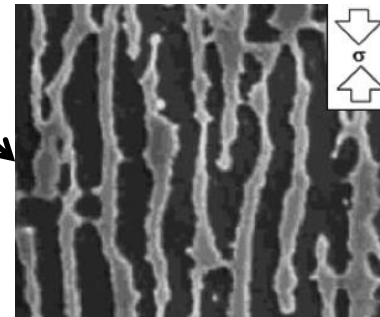
500 nm



Tension  
Compression

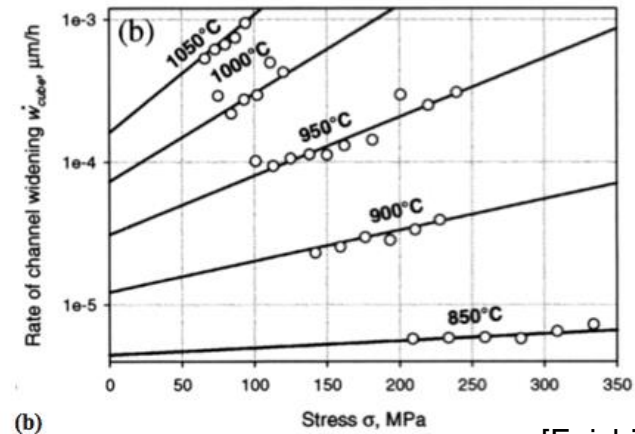
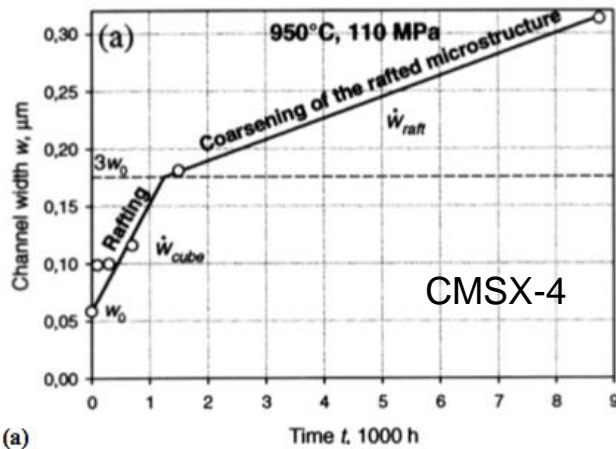


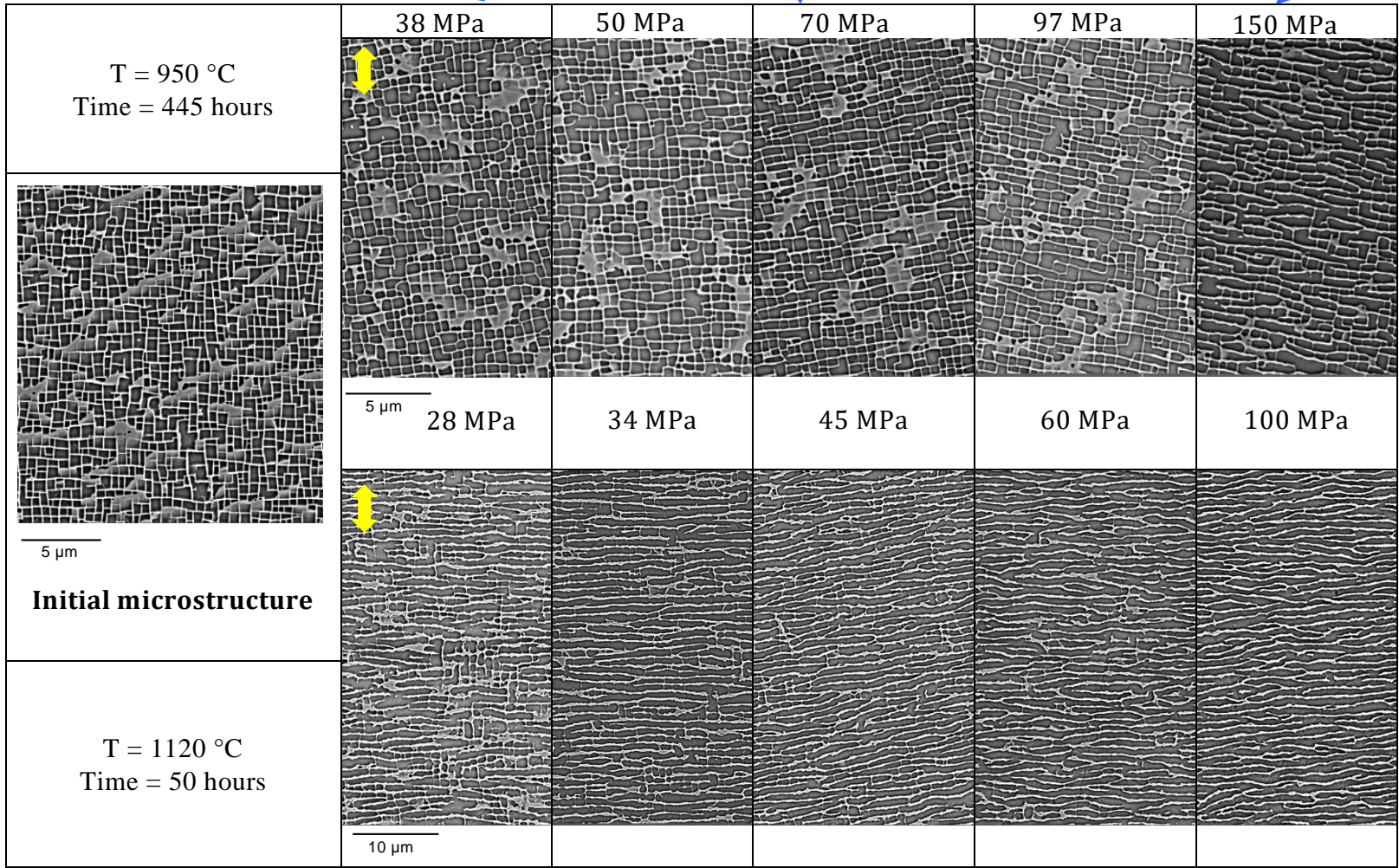
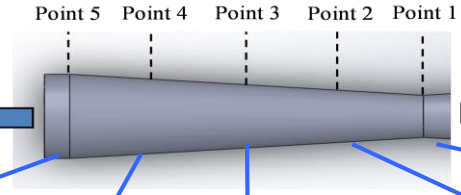
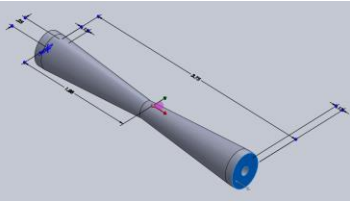
N-raft



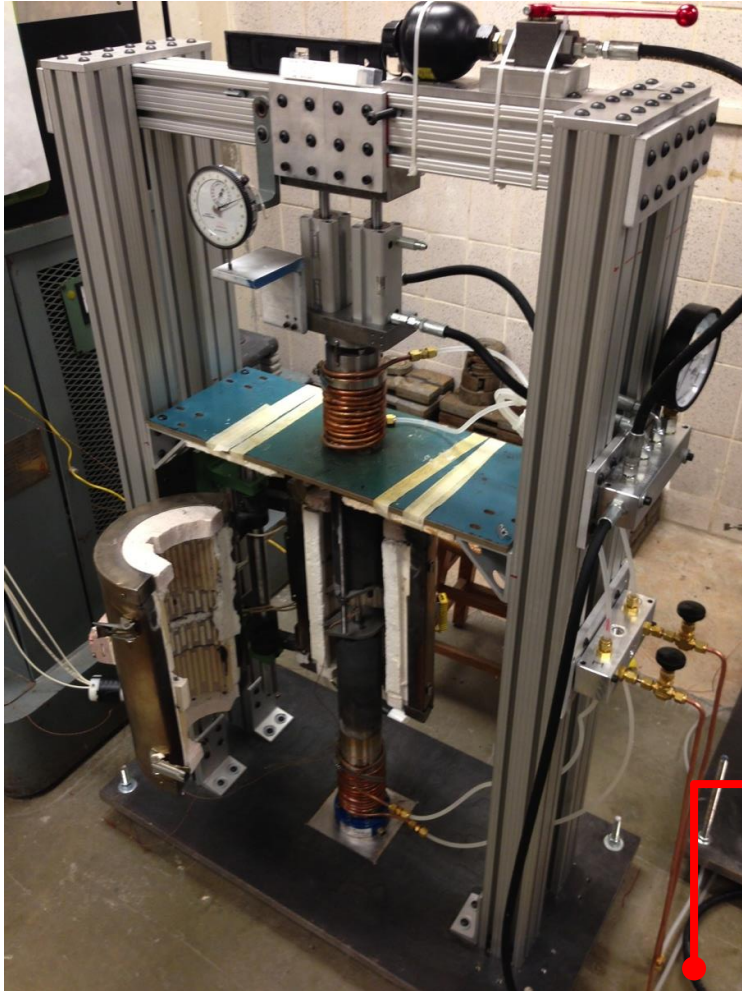
P-raft

$$\delta = \frac{2(a_{\gamma'} - a_{\gamma})}{a_{\gamma'} + a_{\gamma}}$$

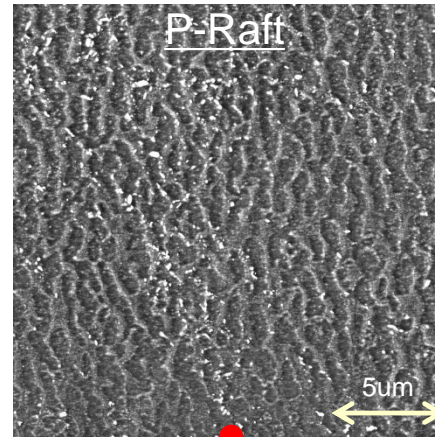




## Compression Creep Frame

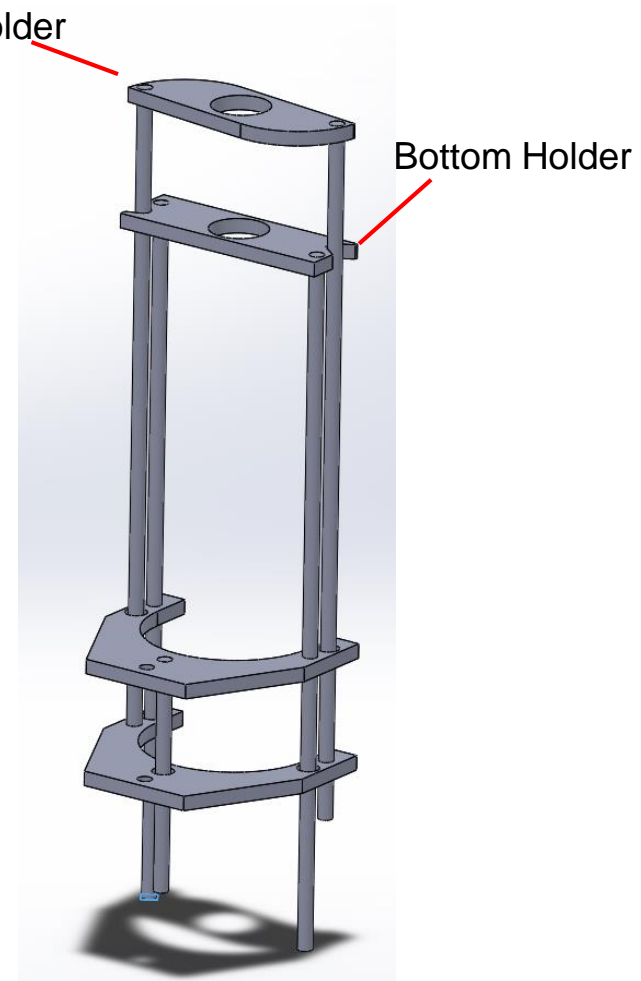


## Ceramic Compression Creep Extensometer



Top Holder

Bottom Holder





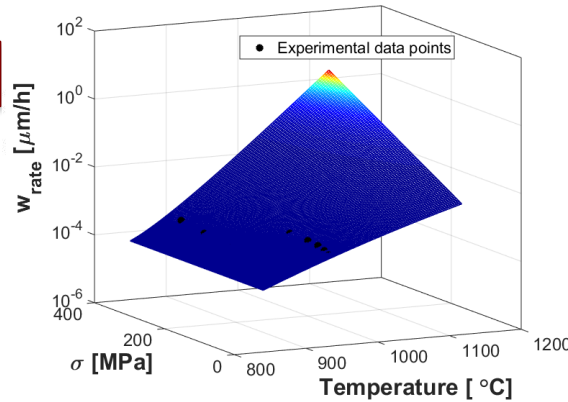
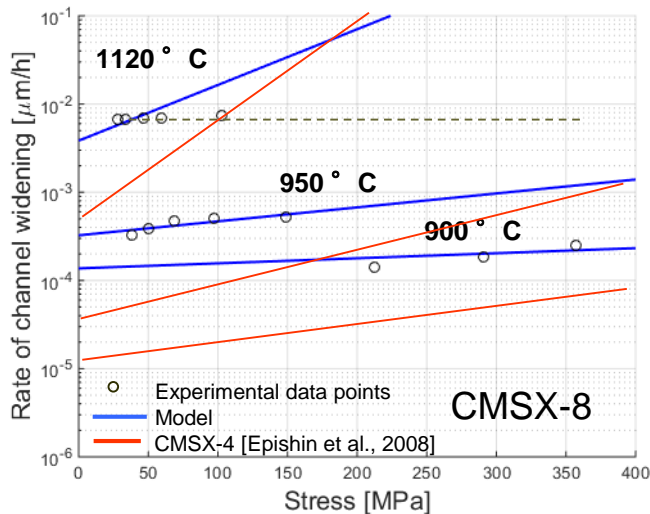
## Physical aging models

### Directional coarsening (Rafting)

$$\dot{w}(T, \sigma) = A \cdot \exp\left[-\frac{Q - U(T) \cdot \sigma}{RT}\right]$$

$$U(T) = U_T(T - T_0)^n$$

[Epishin et al., 2008]



### Isotropic Coarsening

Lifshitz-Slyozov-Wagner (LSW) model:

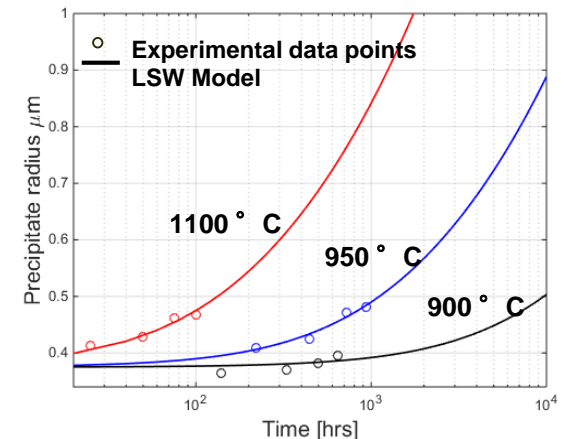
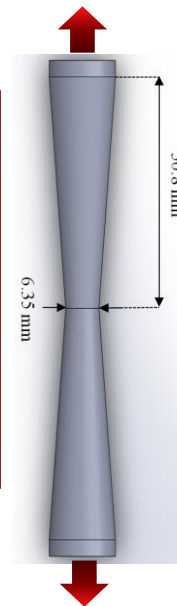
$$(r)^3 - (r_0)^3 = Kt$$

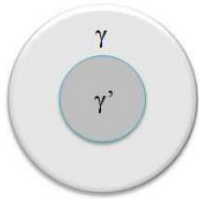
$$K = K_0 \exp\left(-\frac{Q_{coar}}{RT}\right)$$

$$Q_{coar} (\text{CMSX} - 8) = 269.4 \text{ kJ/mol}$$

### High-throughput experimental technique

Stress gradient in longitudinal direction resulting in morphology evolution gradient





## Thermo-Calc DICTRA

Databases: TCNi5 / MOBNI2

Composition sensitive diffusivity parameter

Aging behavior

Temperature-dependent constitutive models

LSW model

$$r^3 - r_0^3 = K(t - t_0)$$

$$\dot{g}^a = \dot{g}_0 Q(T) \left\langle \frac{t_u^a}{D^a} \right\rangle^n \exp \left\{ B_0 \left\langle \frac{t_u^a}{D^a} \right\rangle^{n+1} \right\} \text{sgn}(t^a - c^a)$$

$$K = \frac{64 D_{eff} C_{\infty} \sigma \Omega^2}{9RT}$$

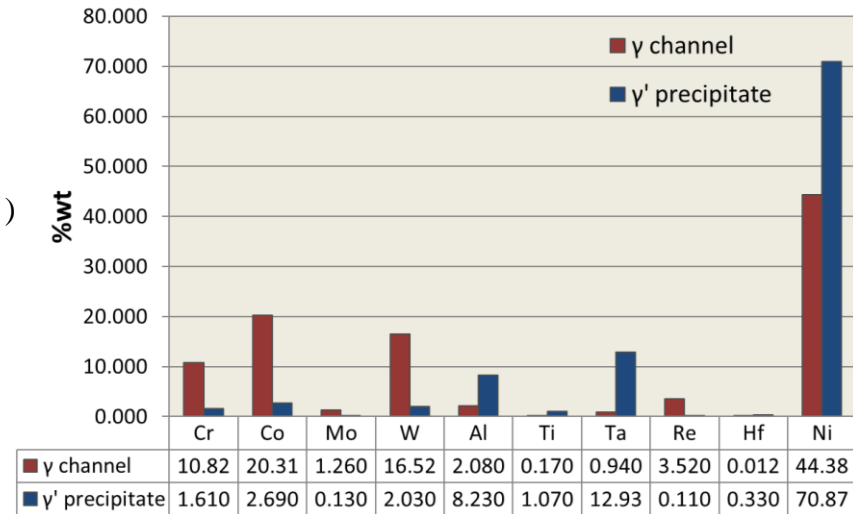
$$Q(T) = \exp\left(-\frac{Q_0}{RT}\right)$$

Diffusivity parameter

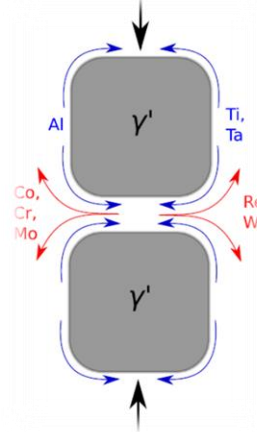
$$D_{eff} = D_{0,eff} \left(-\frac{Q_{eff}}{RT}\right)$$

Coarsening effective diffusivity

Composition segregation  
*Thermo-Calc*



- Effective diffusivity of system is equivalent to effective diffusivity in  $\gamma$  channels.
- Diffusivity of Ni-m binary systems computed from mobility databases using DICTRA from Thermo-Calc.



[Mushongera et al. 2015]

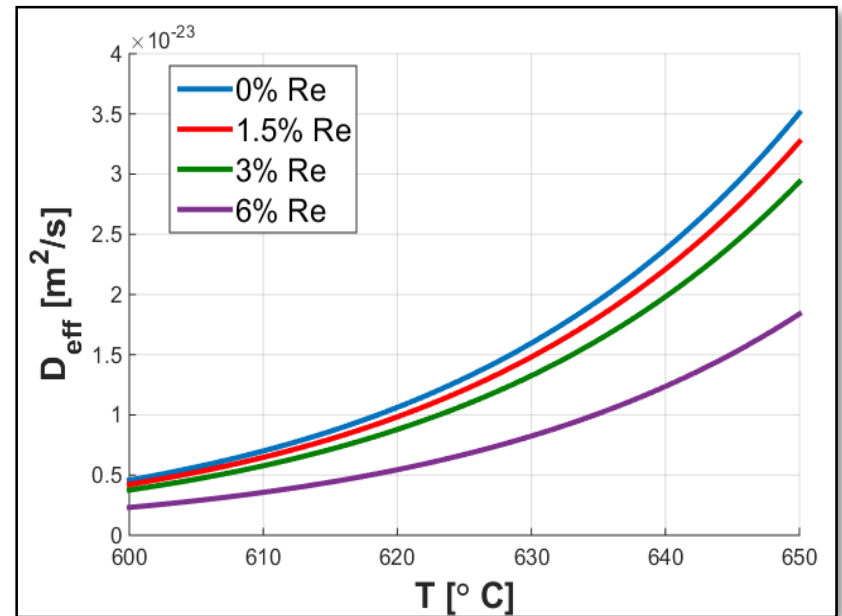
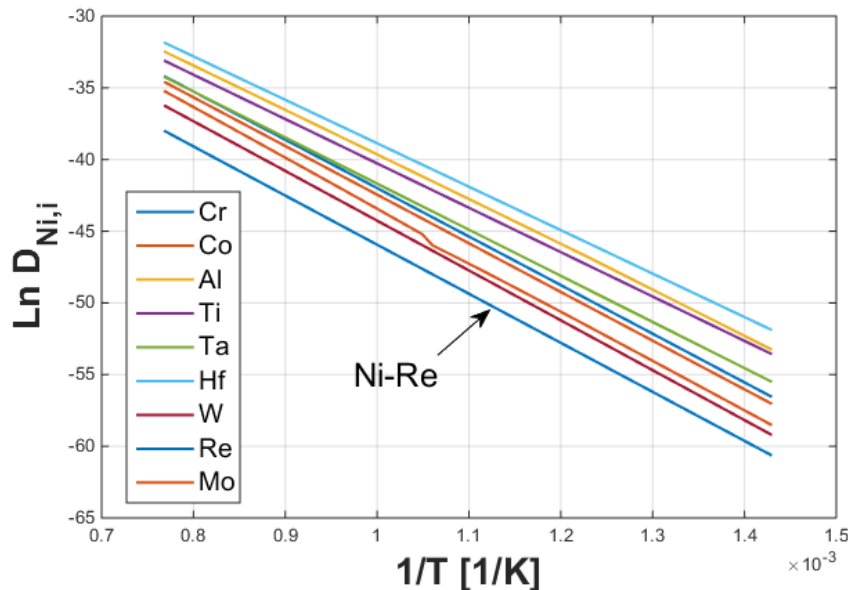
$$D_{eff} = D_{0,eff} \exp\left(-\frac{Q_{eff}}{kT}\right)$$

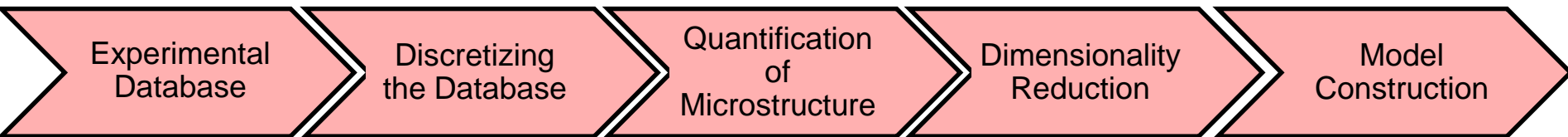
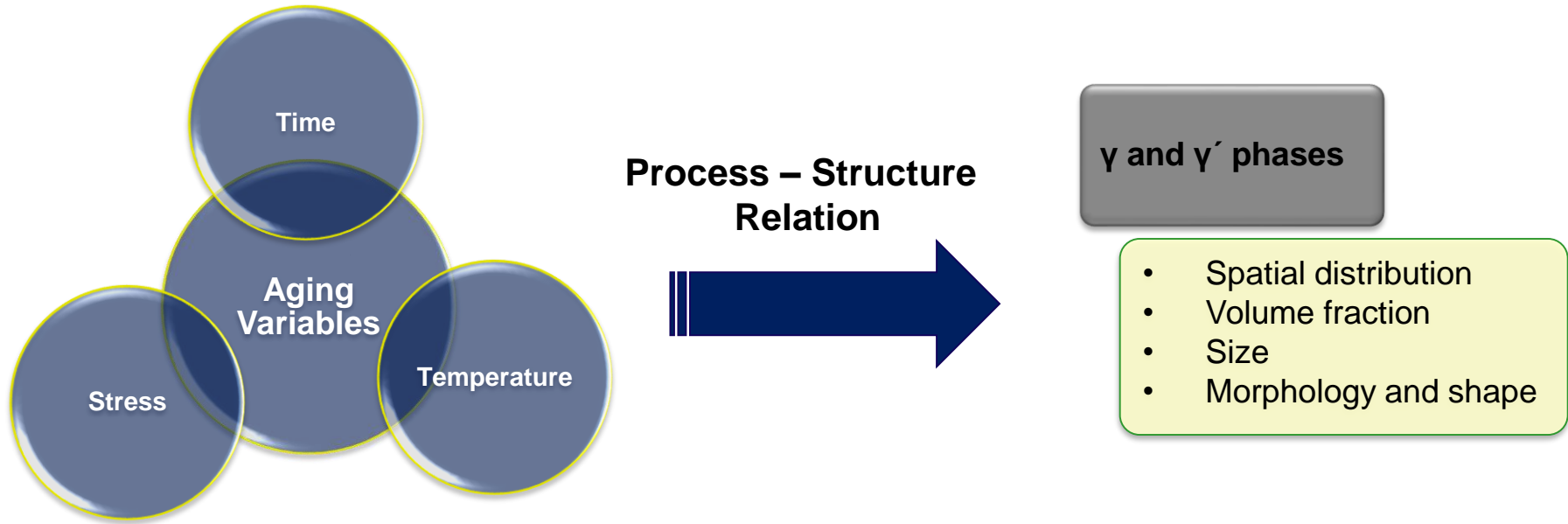
$$Q_{eff} = \sum_m C_m Q_{Ni-m}$$

[Ai et al. 2015]

$$D_{0,eff} = \frac{1}{\sum_m \frac{C_m}{D_{0,Ni-m}}}$$

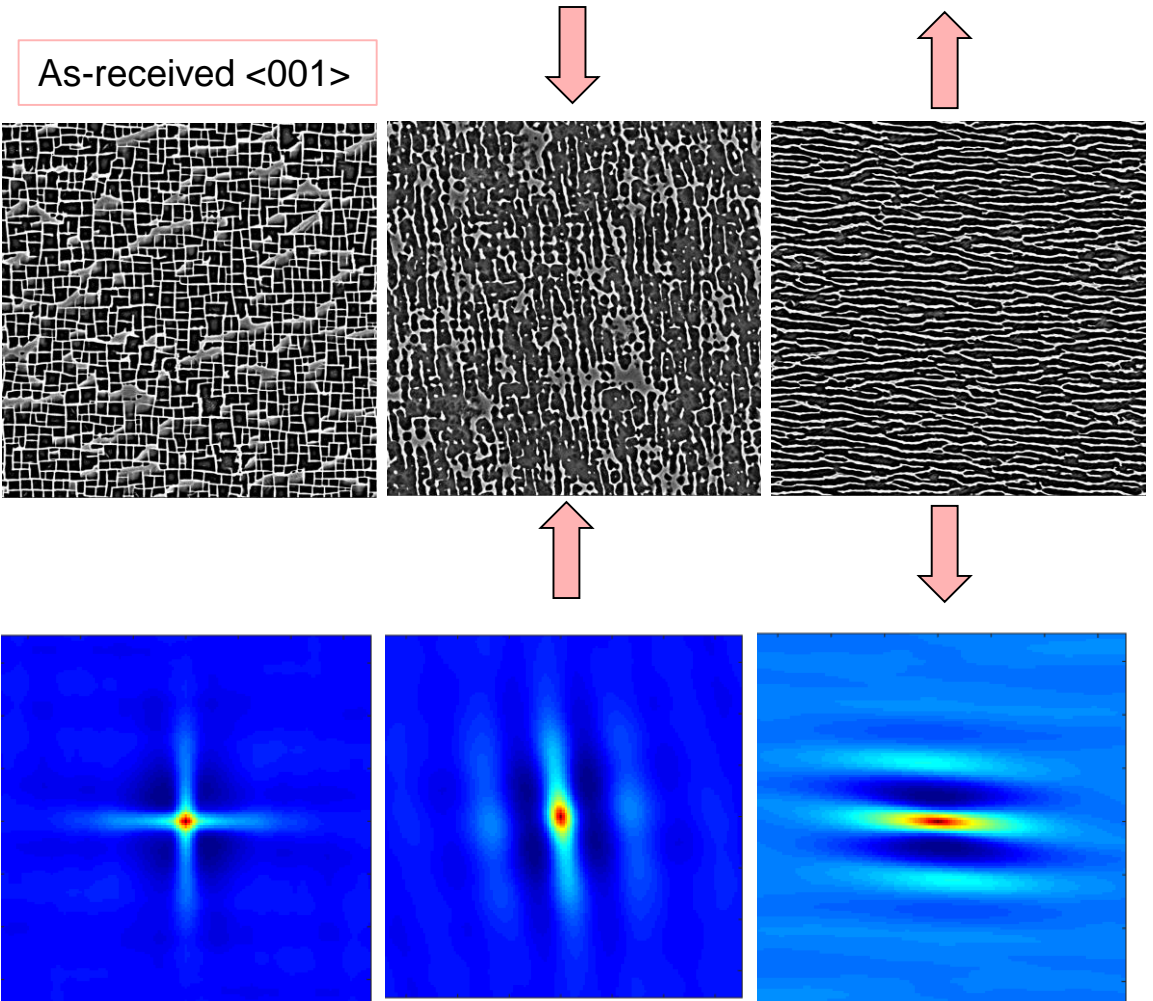
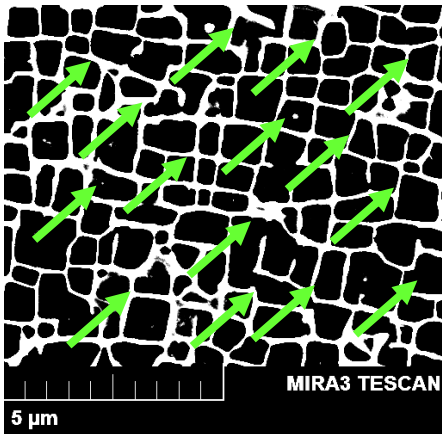
\*  $C_m$  : atomic concentration of element m





A database comprising of coarsened and rafted (P-type and N-type) microstructure as a result of various aging histories is generated

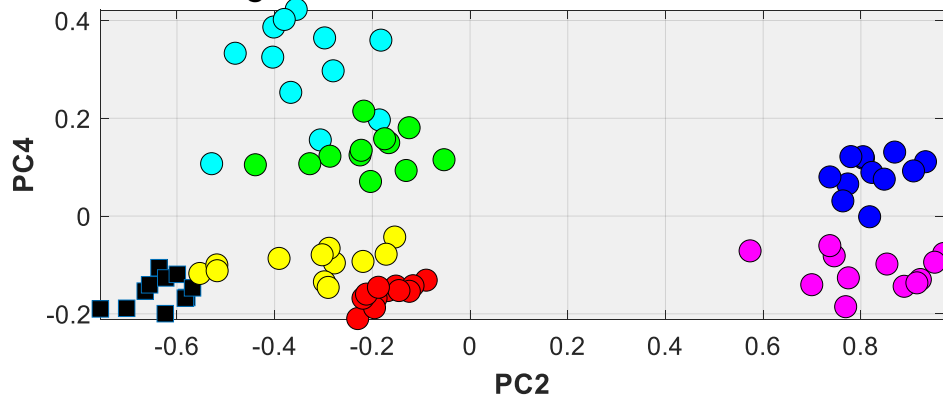
- The 2-point statistical correlation is a rigorous quantification method that describes spatial correlation and critical structural information with microstructure reconstruction capability.
- It is computed based on the probability density associated with finding an ordered pair of specific phase at the head and tail of a randomly placed vector  $r$  into the microstructure.



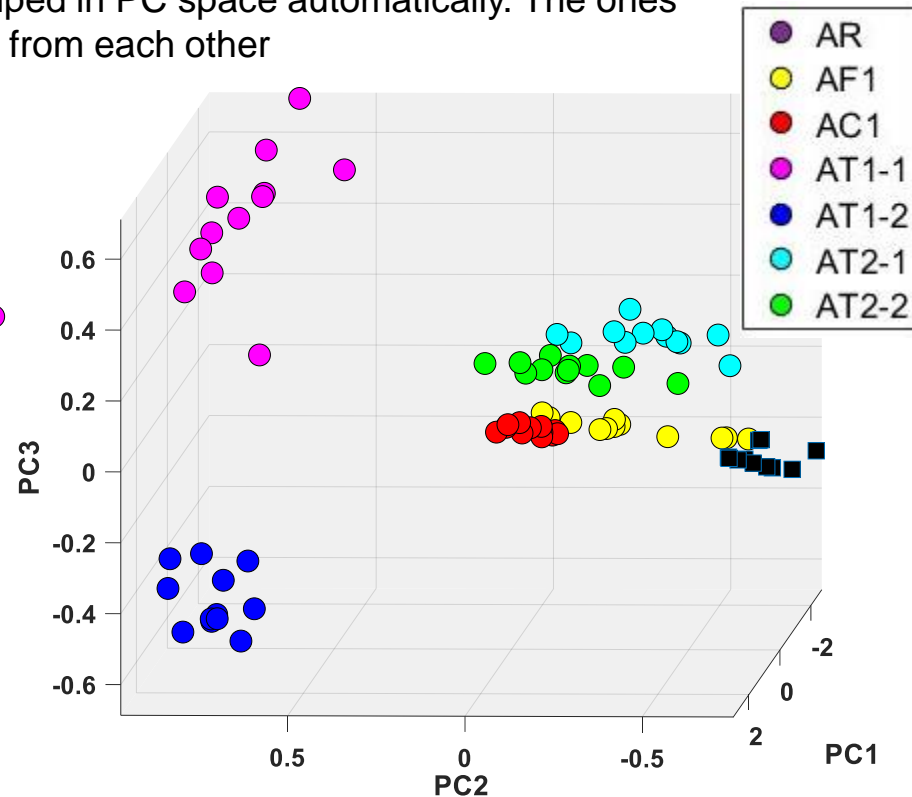
Large Dimensional Dataset generated by 2-point statistical spatial correlation

- Application of PCA to the high dimension 2-point spatial correlation results in a reduced-order representation of microstructure ensemble.
- The axes are ordered descendingly by the extent of variation each explain.
- Powerful classification and visualization tool:  
Micrographs with similar microstructures are grouped in PC space automatically. The ones with significant different structures are located far from each other

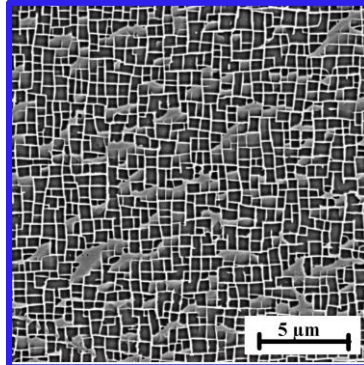
- PCA is a linear approach to dimensionality reduction by coordinate transform.
- The axes are defined by the directions of the highest variance



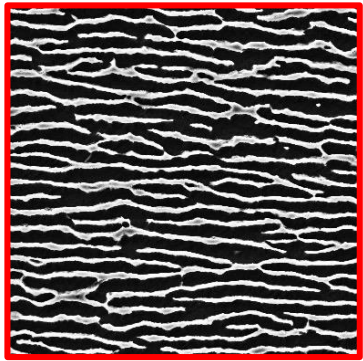
Sample ID	Temperature [°C]	Stress [MPa] (min, max)	Dwell time (h)
AR	23	0	0
AT1-1	1120	95	50
AT1-2	1120	30	50
AT2-1	950	206	450
AT2-2	950	112	450
AC1	900	-208	850
AF1	950	0	940



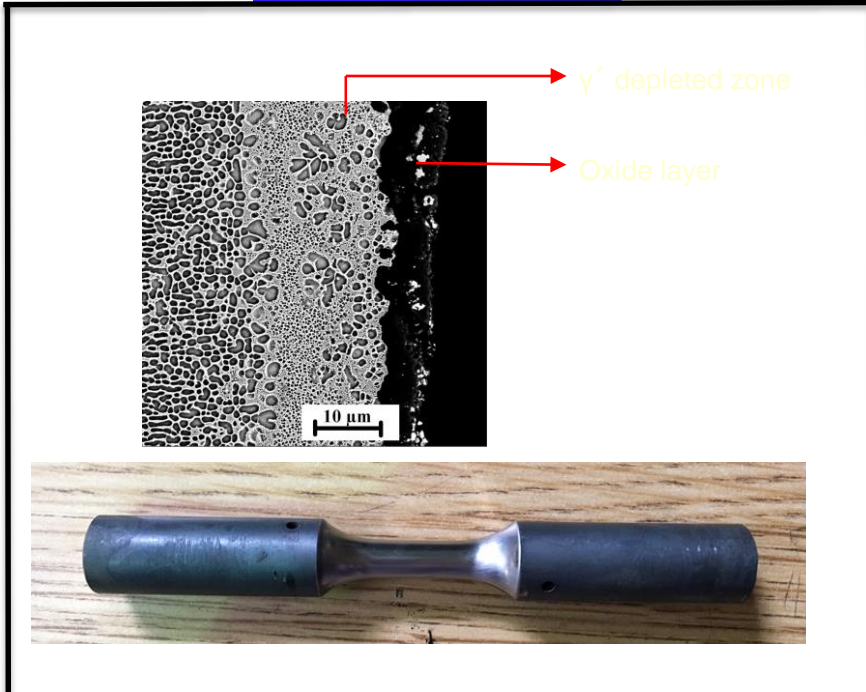
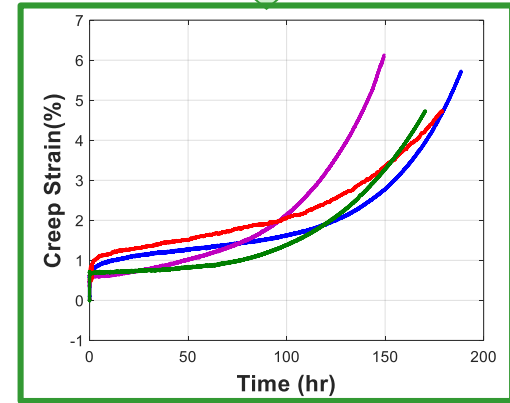
Initial as-heat-treated microstructure



**Pre-Aging**  
 $\sigma = 130 \text{ MPa}$ ,  
 $T = 1100 \text{ }^\circ\text{C}$ ,  
 $t = 50 - 60 \text{ hours}$   
 $\epsilon_{\text{creep}} < 2 \%$



**Pre-Creeping**  
 $\sigma = 392 \text{ MPa}$ ,  
 $T = 900 \text{ }^\circ\text{C}$ ,  
 $\epsilon = 5 - 6 \%$

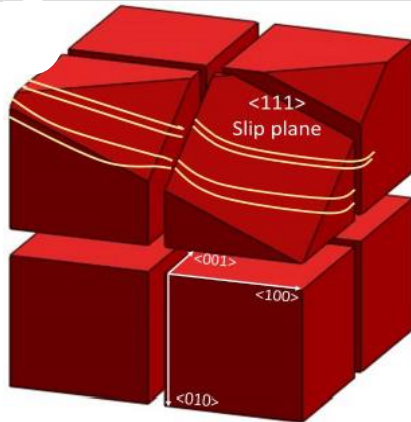


Removal of Oxide and  $\gamma'$  depleted zone

Removal of Oxide and  $\gamma'$  depleted zone

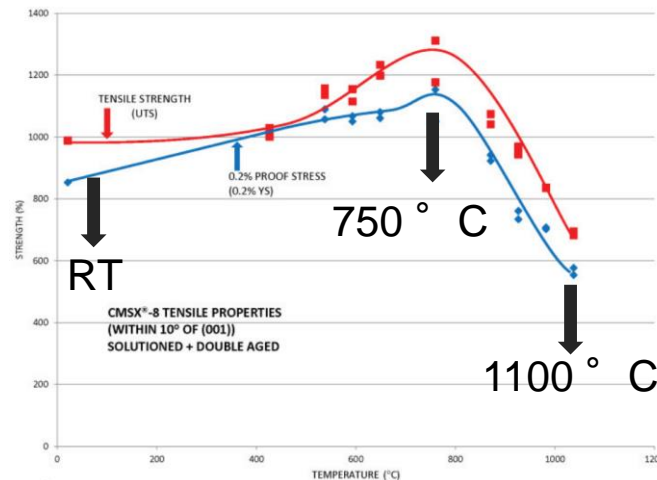
## Room Temperature

- The primary mechanism is the dislocation ribbons shearing through the  $\gamma$  precipitates



## 750 ° C

- Material exhibits its highest strength at this temperature

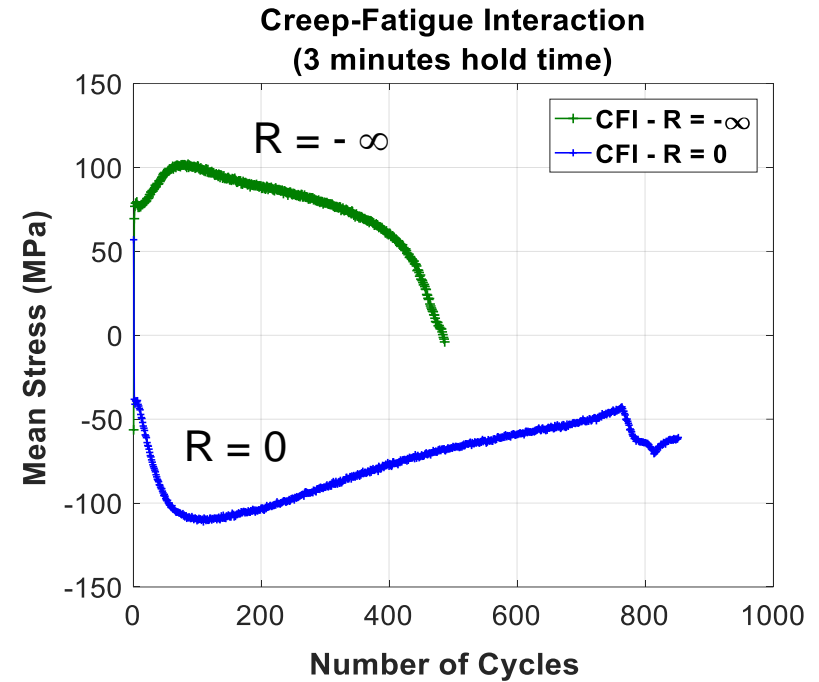
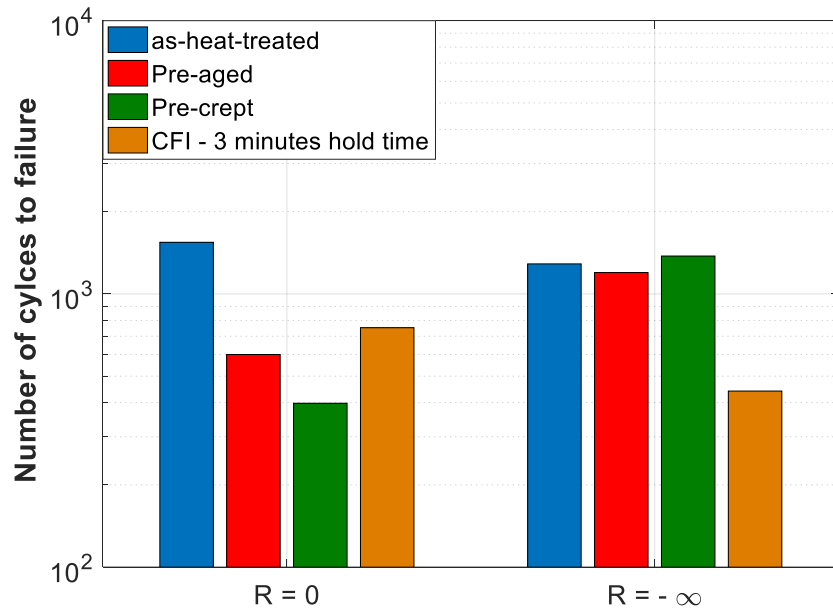


## 1100 ° C

- The dominated mechanism is cross slip and thermally assisted glide and climb of dislocations in  $\gamma$  channels







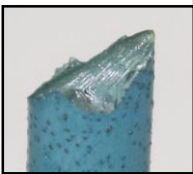
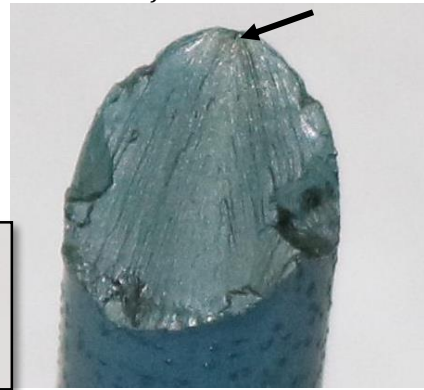
No notable microstructure influence when  $R_\epsilon = -\infty$ .

Fatigue-environment interaction likely explanation when  $R_\epsilon = -\infty$ .

$R_\epsilon = 0$

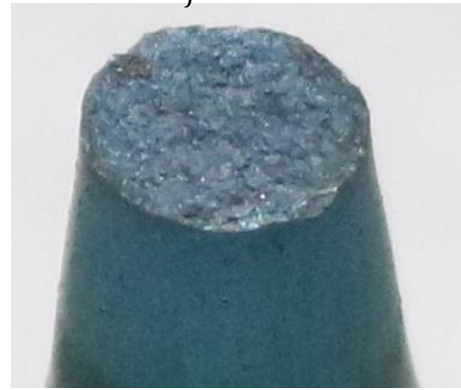
As-heat-treated

$N_f = 1545$



Pre-aged

$N_f = 600$



**Necking:** 20% reduction in area at fractured point

Pre-crept

$N_f = 398$

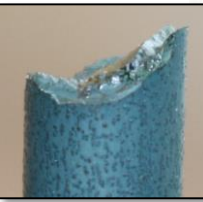


Crack propagation



$R_\epsilon = -\infty$

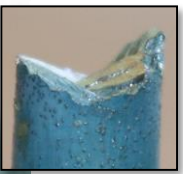
$N_f = 1288$

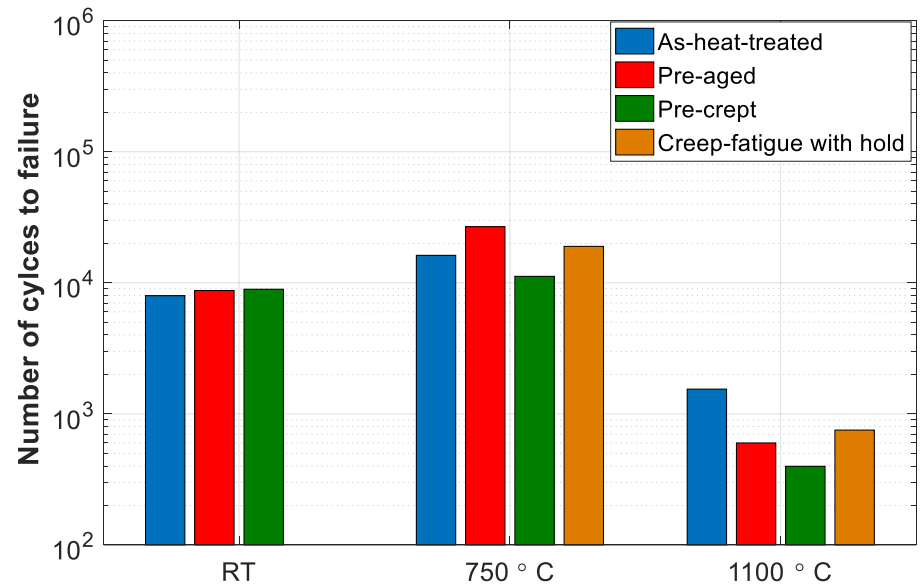
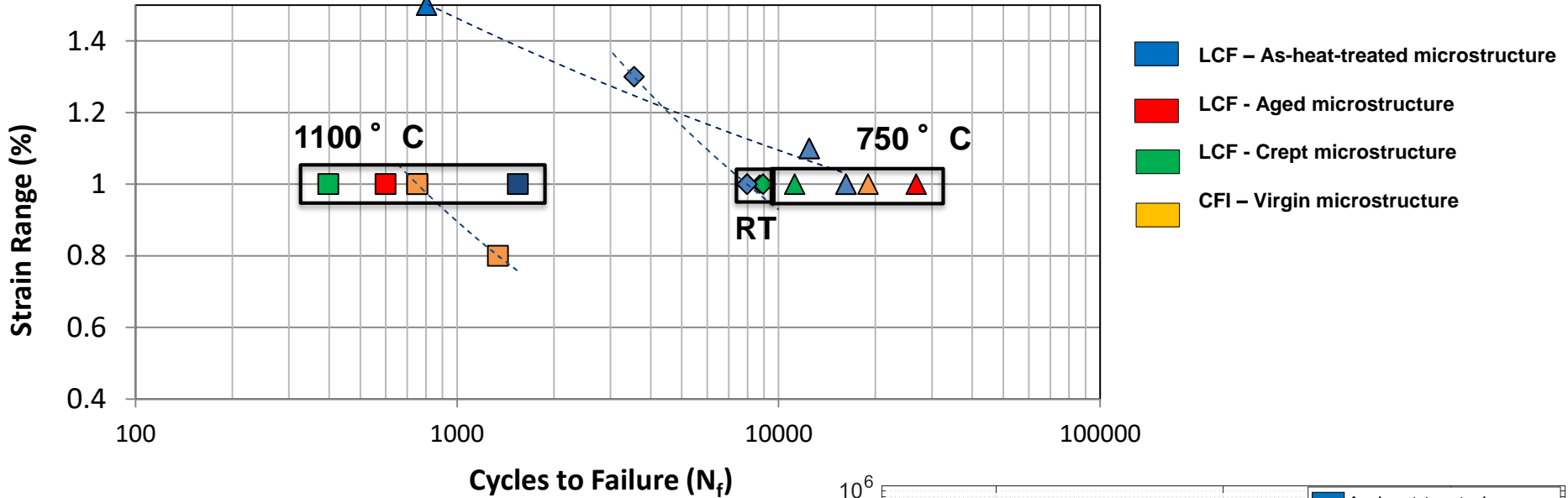


$N_f = 1197$



$N_f = 1376$





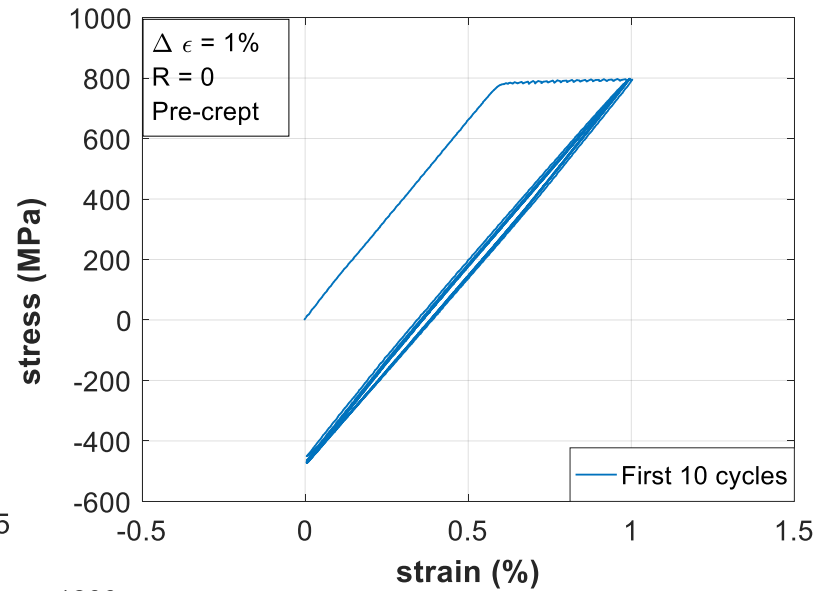
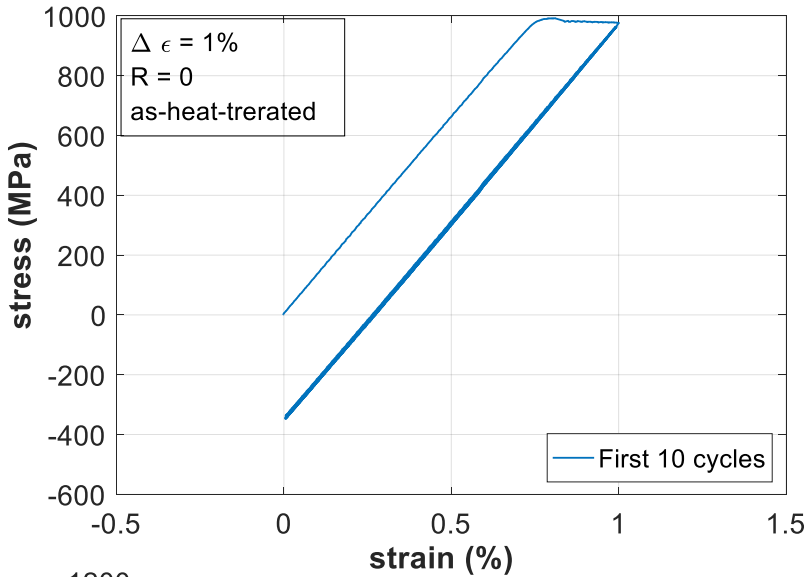
Only observe significant influence of microstructure on LCF at 1100 ° C

The George W. Woodruff School of Mechanical Engineering

School of Materials Science and Engineering

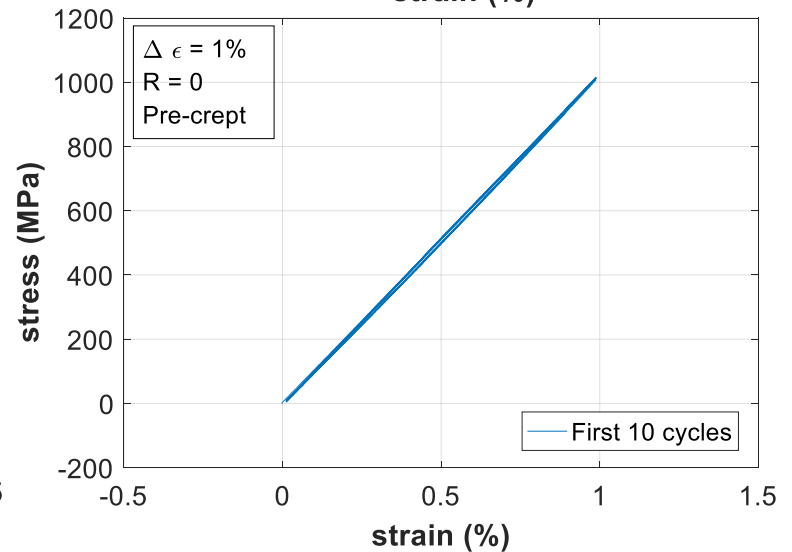
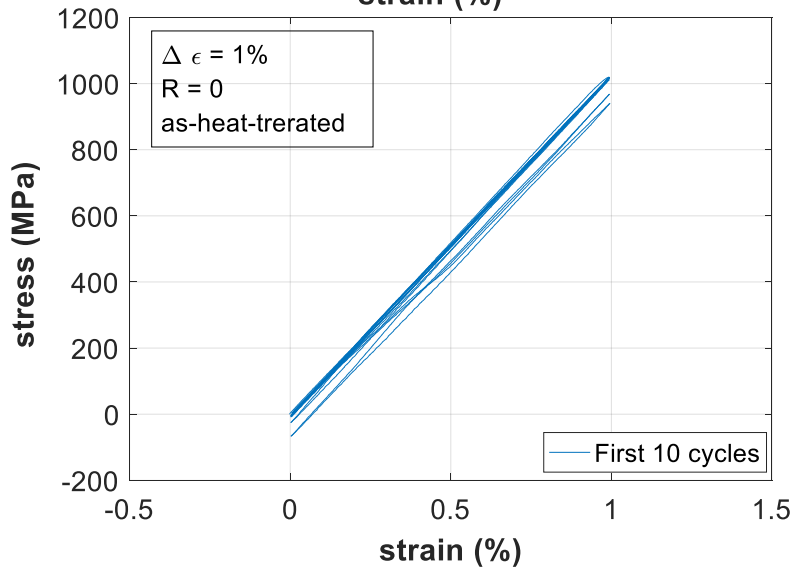
RT

Elastic dominated cyclic response



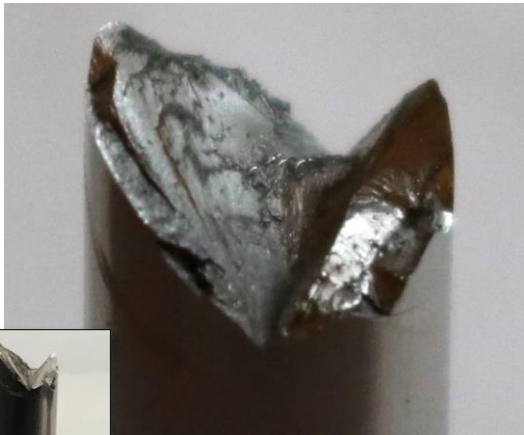
750 ° C

Elastic dominated cyclic response - Peak strength



## Low Cycle Fatigue at Room Temperature

As-heat-treated

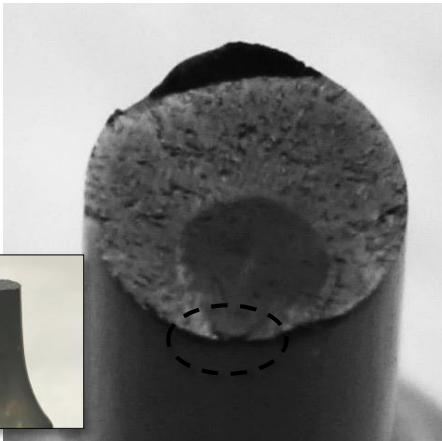


Pre-crept

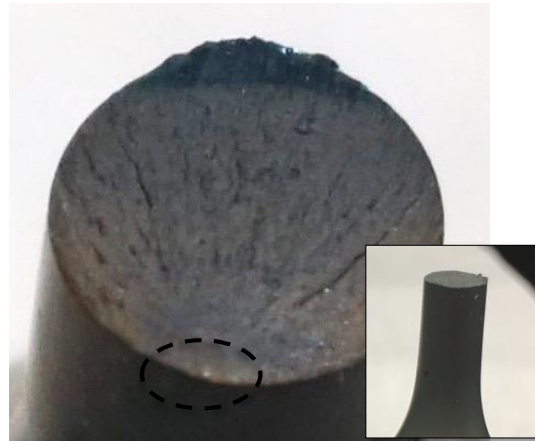


## Low Cycle Fatigue at 750 ° C

As-heat-treated



Pre-aged

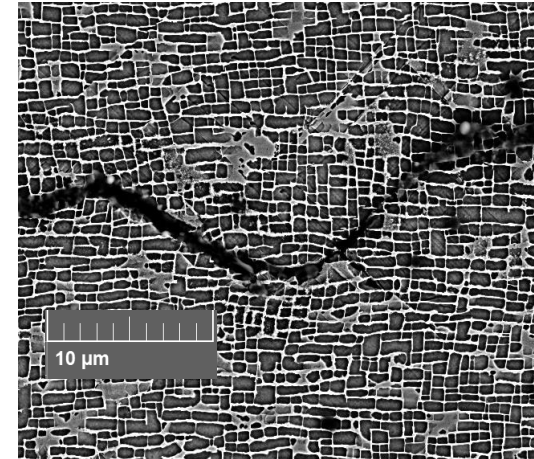
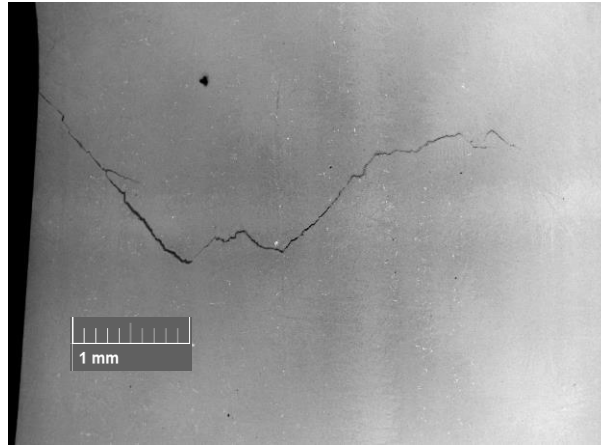


Pre-crept



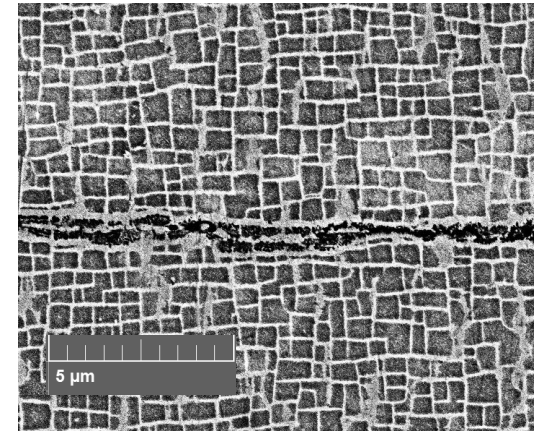
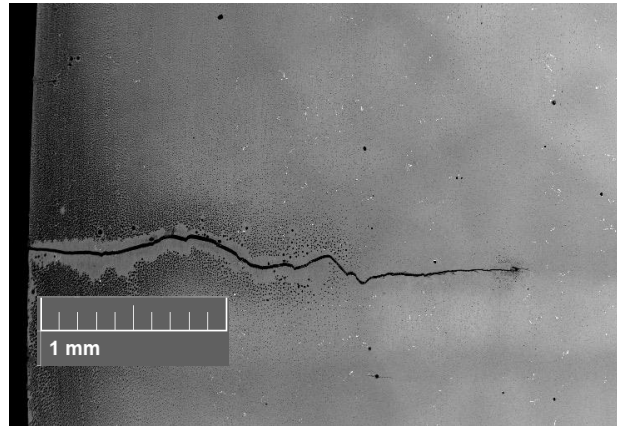
LCF at Room temperature

*Pre-aged  
microstructure*

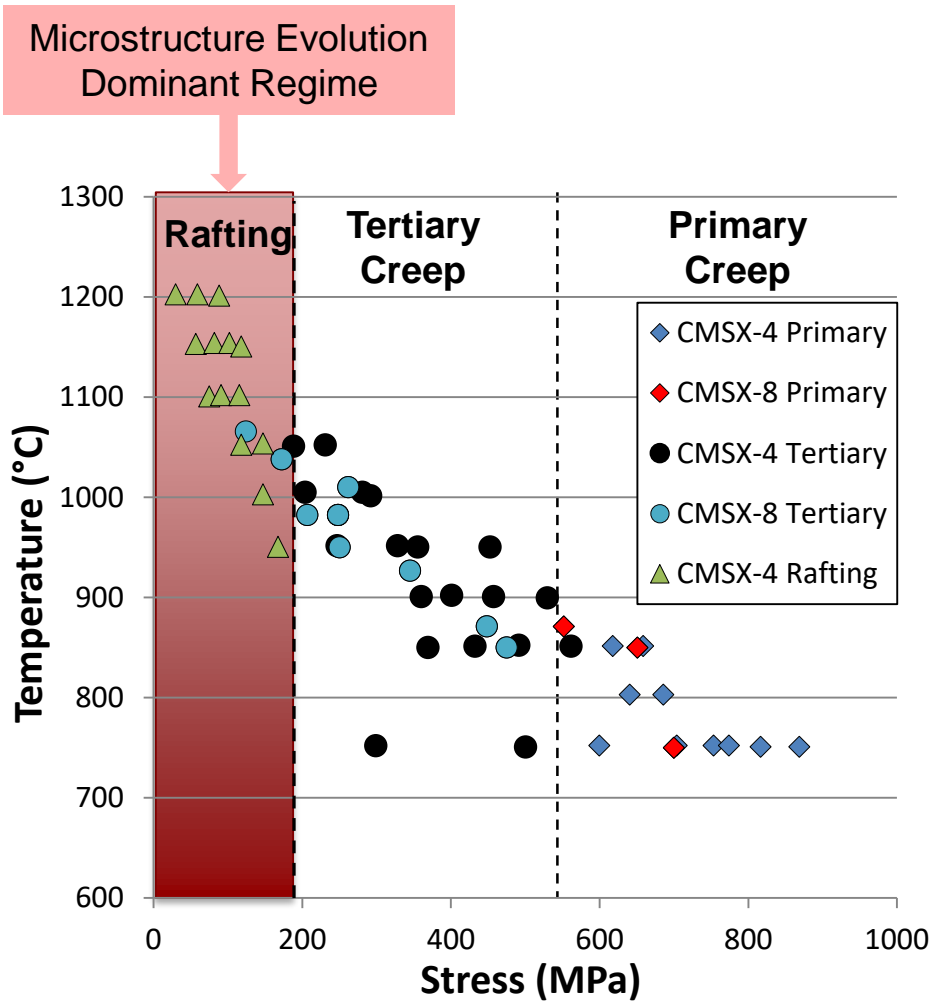


CFI at 750 °C

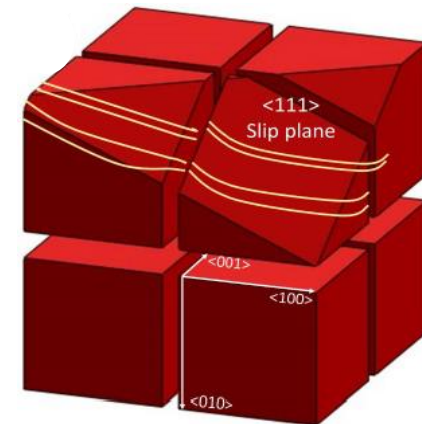
*As-heat-treated  
microstructure*



- Creep-fatigue interaction experiments on CMSX-8
- Influence of aging on microstructure and creep-fatigue interactions
- **Microstructure-sensitive, temperature-dependent crystal viscoplasticity to capture the creep and cyclic deformation response**



**Tertiary** – dislocation activity restricted to  $a/2\langle 110 \rangle$  form operating on  $\{111\}$  slip planes in the  $\gamma$  channels

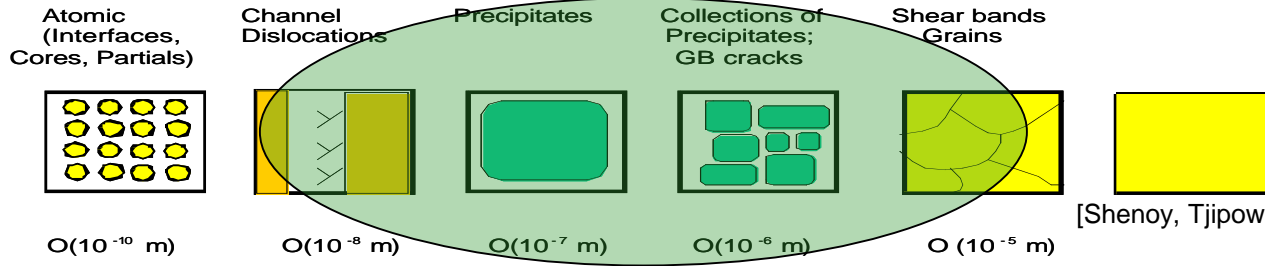


**Primary** –  $\gamma'$  particles are sheared by dislocation ribbons of overall Burgers vector  $a\langle 112 \rangle$  dissociated into superlattice partial dislocations separated by a stacking fault; shear stress must above threshold stress (about 550 MPa)

[Reed, 2006; Ma, Dye, and Reed, 2008; our CMSX-8 Data]



## Alloy structure



[Shenoy, Tjipowidjojo, and McDowell, 2008]

+

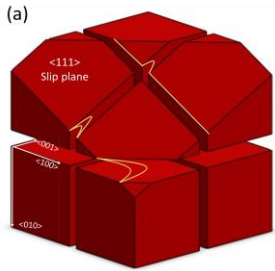
Distinct deformation in the  $\gamma$  and  $\gamma'$  phases

$$\mathbf{L}^{in} = f_{\gamma} \left( \sum_{\alpha=1}^{12} \dot{\gamma}_{\gamma}^{in(\alpha)} (\hat{\mathbf{d}}^{(\alpha)} \otimes \hat{\mathbf{n}}^{(\alpha)}) \right) + f_{\gamma'} \left( \sum_{\alpha=13}^{24} \dot{\gamma}_{L1_2}^{in(\alpha)} (\hat{\mathbf{d}}^{(\alpha)} \otimes \hat{\mathbf{n}}^{(\alpha)}) \right)$$

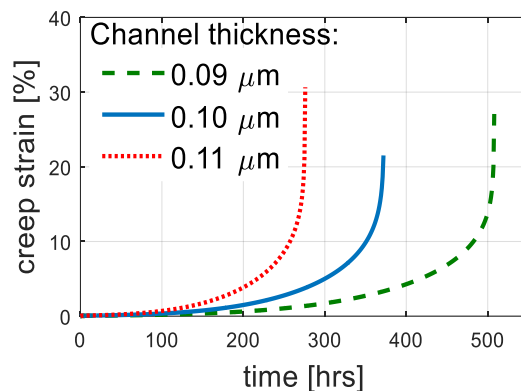
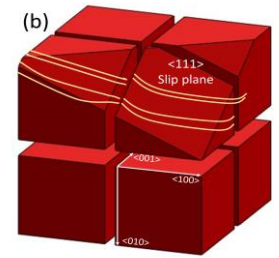
+

Deformation predictions sensitive to the  $\gamma$  and  $\gamma'$  phase attributes

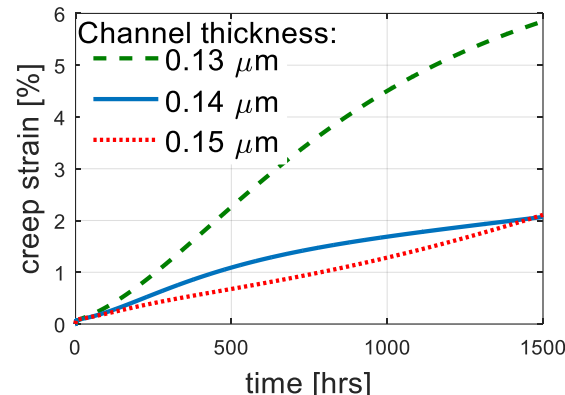
$\gamma$  deformation  
In  $\gamma$ : 12 octahedral slip systems active



$\gamma'$  deformation  
In  $\gamma'$ : 12 octahedral slip systems moving as dislocation ribbons



Tertiary creep: 950 °C, Stress = 400 MPa



Primary creep: 750 °C, Stress = 680 MPa

Kinematic relations including temperature dependence

Deformation gradient

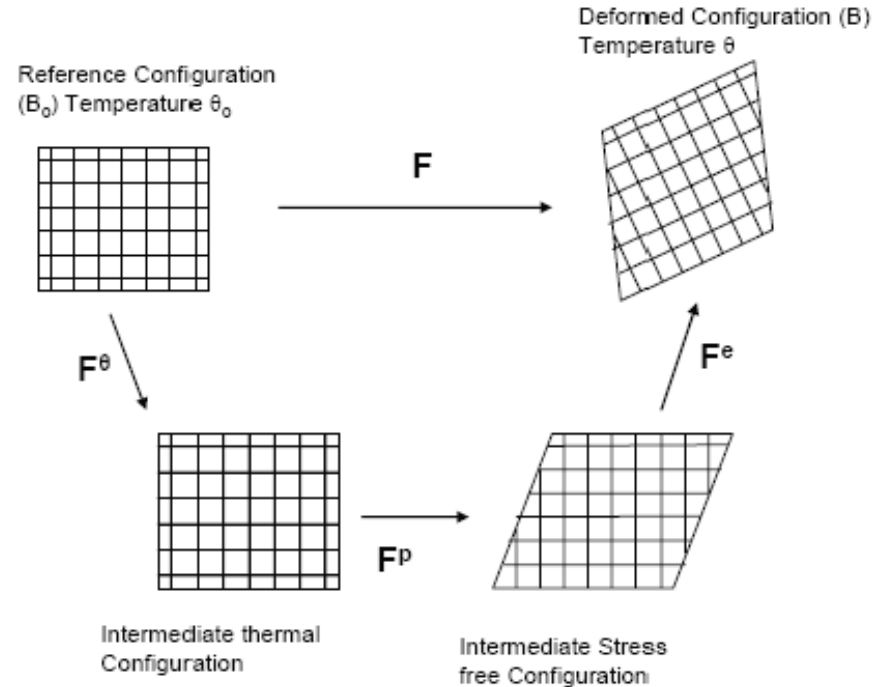
$$\mathbf{F} = \frac{\mathbf{dx}}{\mathbf{dX}} = \mathbf{F}^e \times \mathbf{F}^p \times \mathbf{F}^\theta$$

Velocity gradient

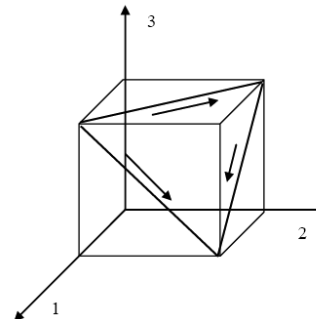
$$\mathbf{L} = \dot{\mathbf{F}} \times \mathbf{F}^{-1}$$

Macroscopic plastic velocity gradient

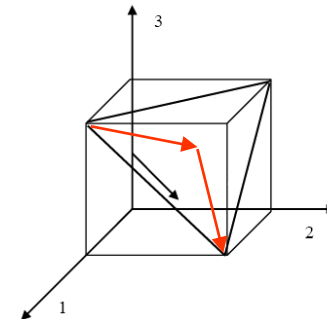
$$\mathbf{L}^p = \dot{\mathbf{F}}^p \mathbf{F}^{p-1} = \sum_{a=1}^{N_{slip}} \dot{\gamma}^{(a)} (\mathbf{s}_o^{(a)} \otimes \mathbf{n}_o^{(a)})$$



In  $\gamma$ : 12 octahedral slip systems active



In  $\gamma'$ : 12 octahedral slip systems moving as dislocation ribbons



## Inelastic Velocity Gradient

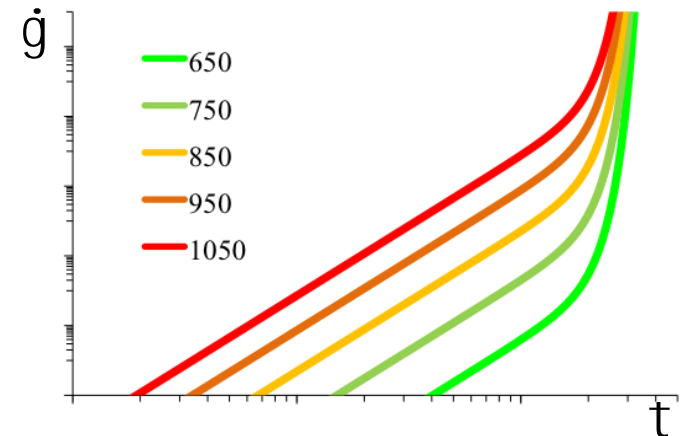
$$\mathbf{L}^{in} = \dot{\mathbf{F}}^{in} \mathbf{F}^{in-1} = f_{\gamma} \left( \sum_{\alpha=1}^{12} \dot{\gamma}_{\gamma}^{in(\alpha)} \left( \hat{\mathbf{d}}^{(\alpha)} \otimes \hat{\mathbf{n}}^{(\alpha)} \right) \right) + f_{\gamma'} \left( \sum_{\alpha=13}^{24} \dot{\gamma}_{L1_2}^{in(\alpha)} \left( \hat{\mathbf{d}}^{(\alpha)} \otimes \hat{\mathbf{n}}^{(\alpha)} \right) \right)$$

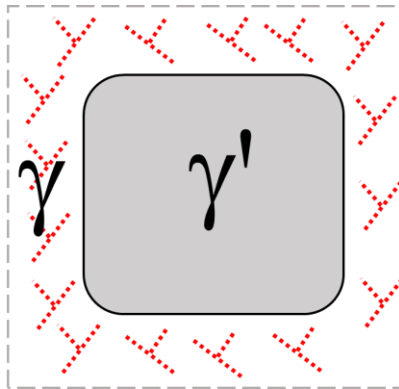
## Inelastic Shear Strain Rate

$$\left\{ \begin{aligned} \dot{\gamma}_{\gamma}^{in(\alpha)} &= \rho_{\gamma}^{(\alpha)} b \lambda_{\gamma}^{(\alpha)} F_{attack} \text{sign} \left( \tau^{(\alpha)} + \tau_{mis}^{(\alpha)} - \chi^{(\alpha)} \right) \exp \left\{ \frac{-Q_{slip}^{110} + \left( \left| \tau^{(\alpha)} + \tau_{mis}^{(\alpha)} - \chi^{(\alpha)} \right| - \tau_{\gamma pass}^{(\alpha)} - \tau_{oro}^{(\alpha)} \right) V_{c1}^{(\alpha)}}{kT} \right\} \\ \dot{\gamma}_{L1_2}^{in(\alpha)} &= \rho_{L1_2}^{(\alpha)} b \lambda_{L1_2}^{(\alpha)} F_{attack} \text{sign} \left( \tau^{(\alpha)} - \chi^{(\alpha)} \right) \exp \left\{ \frac{-Q_{slip}^{112} + \left( \left| \tau^{(\alpha)} - \chi^{(\alpha)} \right| - \tau_{L1_2 pass}^{(\alpha)} - \tau_{APB} \right) V_{c2}^{(\alpha)}}{kT} \right\} \end{aligned} \right.$$

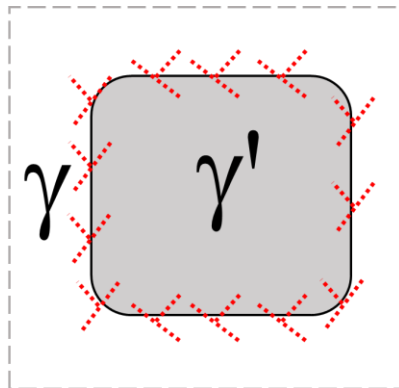
## Dislocation Density Evolution Equations

$$\left\{ \begin{aligned} \dot{\rho}_{\gamma}^{(\alpha)} &= \frac{1}{b} \left( \frac{c_{mult1}}{\lambda_{\gamma}^{(\alpha)}} - c_{annh1} \rho_{\gamma}^{(\alpha)} \right) \left| \dot{\gamma}_{\gamma}^{in(\alpha)} \right| \\ \dot{\rho}_{L1_2}^{(\alpha)} &= c_{mult21} \rho_{pb}^{(\alpha)} \Gamma + \frac{c_{mult22}}{b \lambda_{\gamma'}^{(\alpha)}} \left| \dot{\gamma}_{\gamma'}^{(\alpha)} \right| - c_{annh2} \rho_{\gamma'}^{(\alpha)} \left| \dot{\gamma}_{\gamma'}^{(\alpha)} \right| \\ \dot{\rho}_{pb}^{(\alpha)} &= \frac{c_{mult}^{pb}}{b L_{\gamma}} \left| \dot{\gamma}_{\gamma}^{in(\alpha)} \right| - c_{annh}^{pb} \rho_{pb}^{(\alpha)} \left| \dot{\gamma}_{\gamma}^{in(\alpha)} \right| \end{aligned} \right.$$

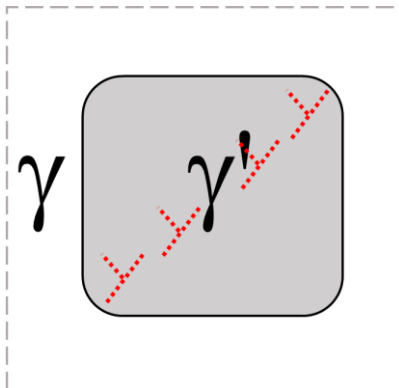




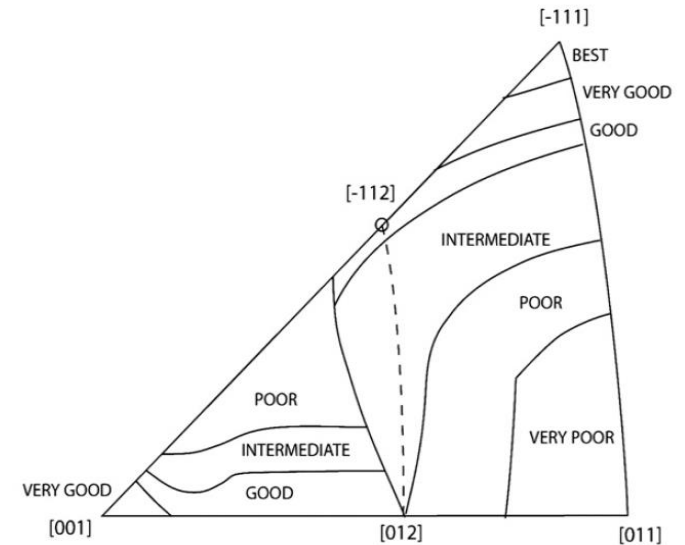
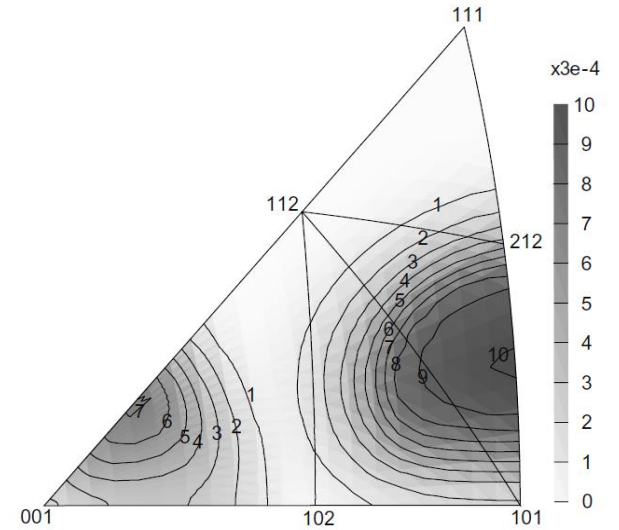
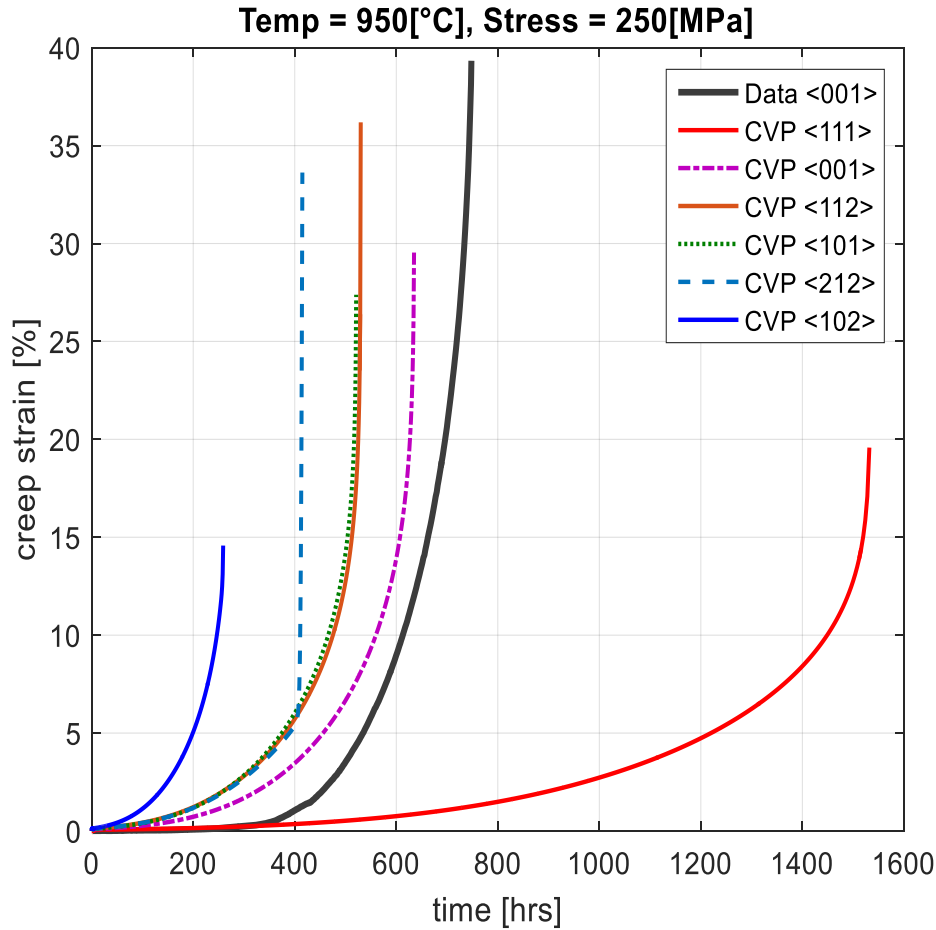
$$\dot{\rho}_{\gamma}^{(\alpha)} = \frac{1}{b} \left( \overbrace{\frac{c_{mult1}}{\lambda_{\gamma}^{(\alpha)}}}_{\text{multiplication}} - \overbrace{c_{annh1}}_{\text{annihilation}} \rho_{\gamma}^{(\alpha)} \right) \left| \dot{\gamma}_{\gamma}^{in(\alpha)} \right|$$

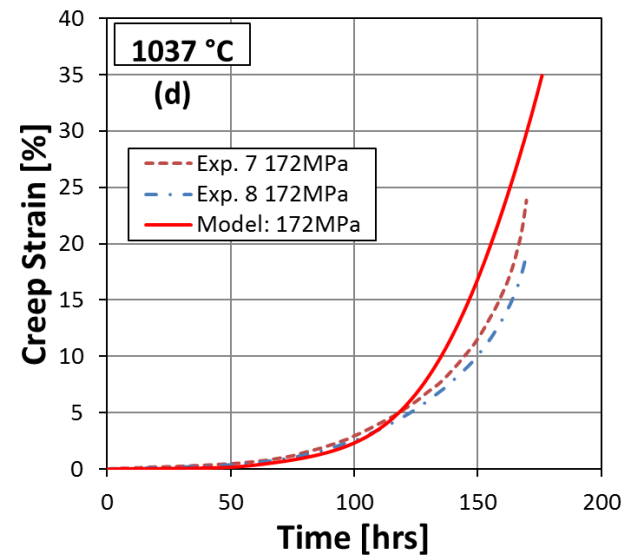
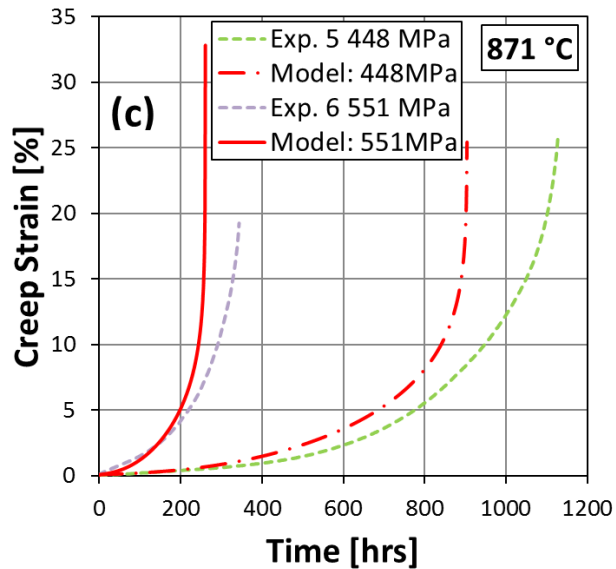
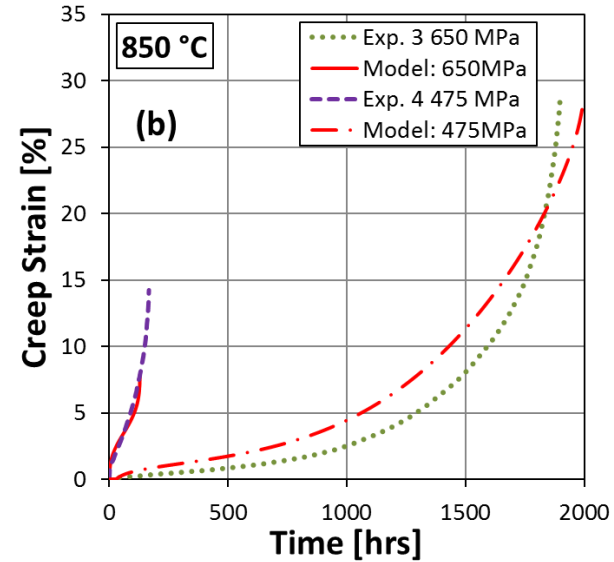
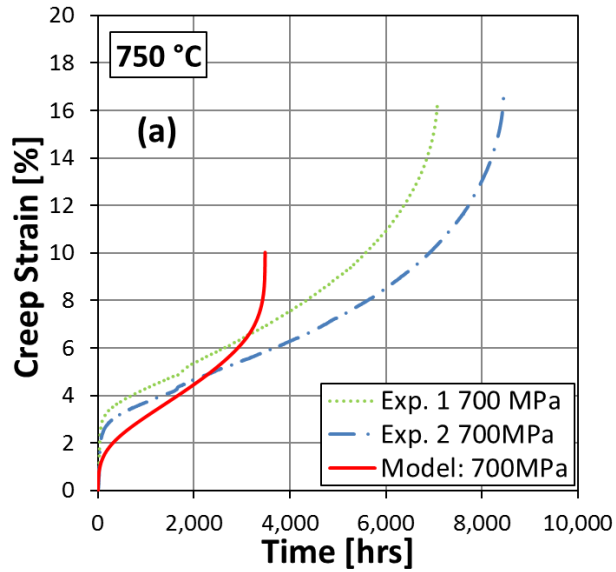


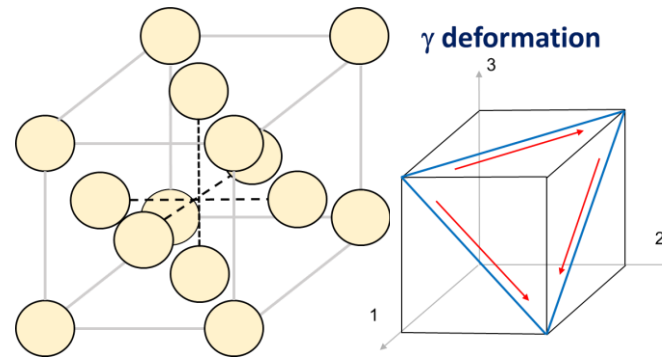
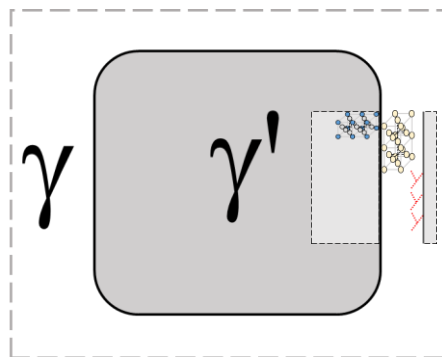
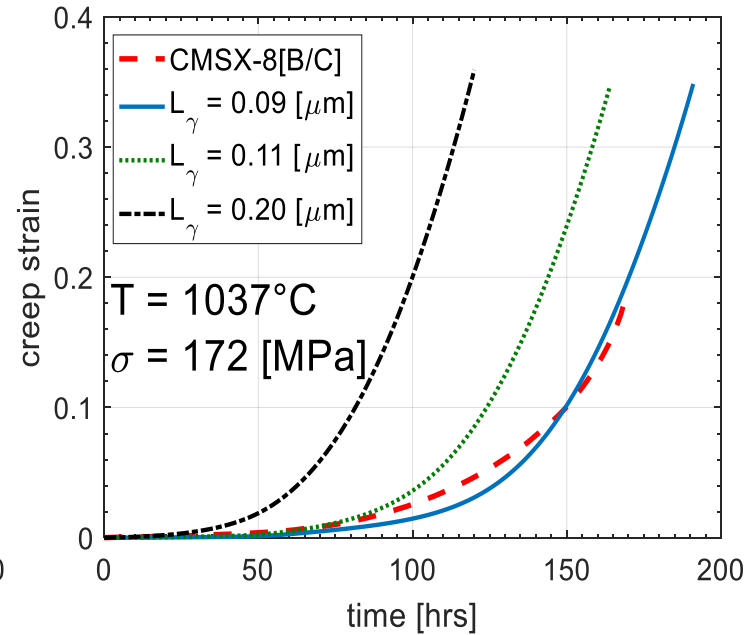
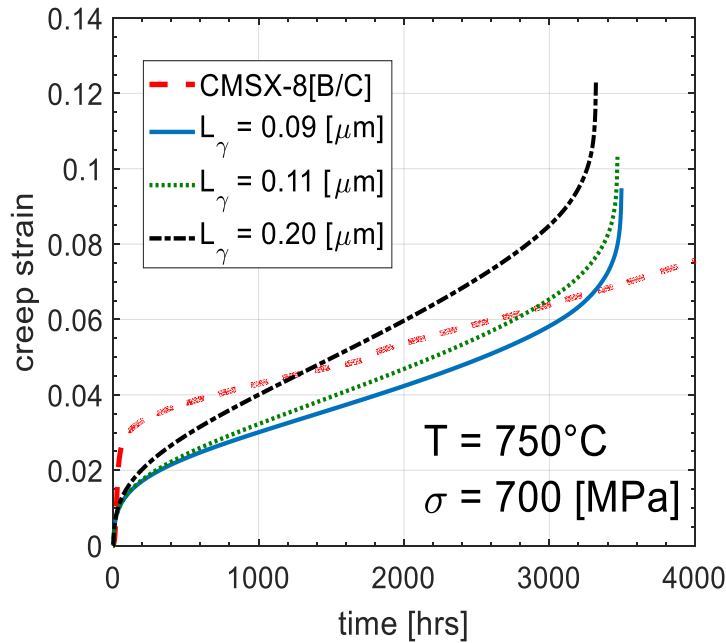
$$\dot{\rho}_{pb}^{(\alpha)} = \frac{c_{mult}^{pb}}{bL_{\gamma}} \left| \dot{\gamma}_{\gamma}^{in(\alpha)} \right| - c_{annh}^{pb} \rho_{pb}^{(\alpha)} \left| \dot{\gamma}_{\gamma}^{in(\alpha)} \right|$$

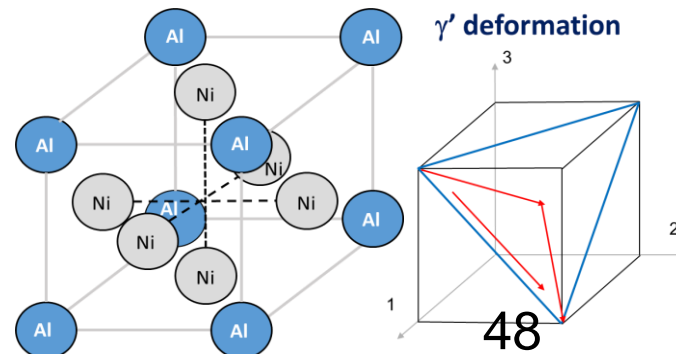
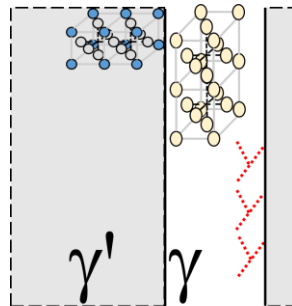
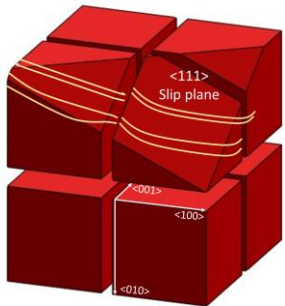
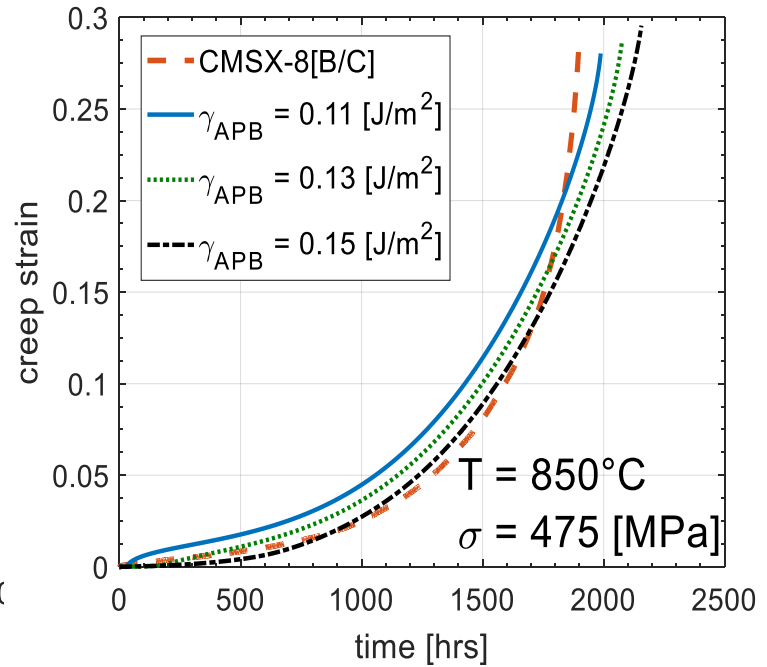
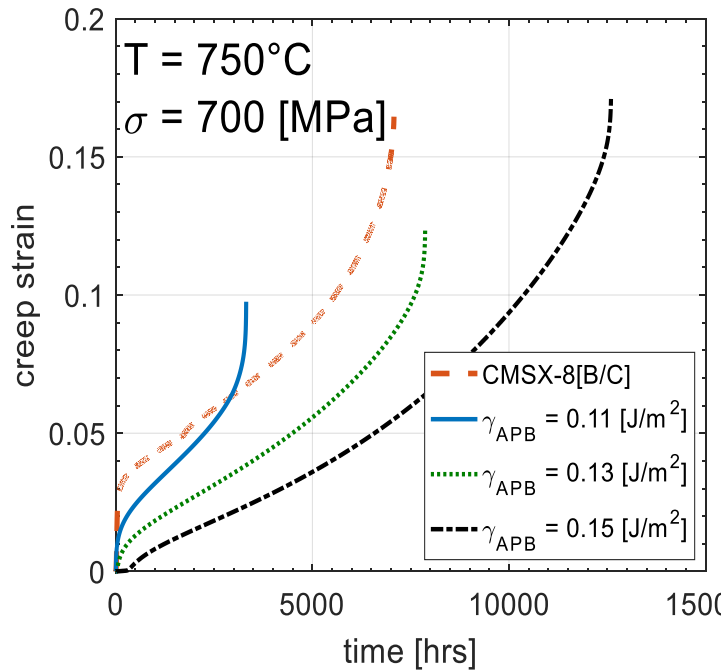


$$\dot{\rho}_{L12}^{(\alpha)} = c_{mult21} \rho_{pb}^{(\alpha)} \Gamma + \frac{c_{mult22}}{b\lambda_{\gamma'}^{(\alpha)}} \left| \dot{\gamma}_{\gamma'}^{(\alpha)} \right| - c_{annh2} \rho_{\gamma'}^{(\alpha)} \left| \dot{\gamma}_{\gamma'}^{(\alpha)} \right|$$



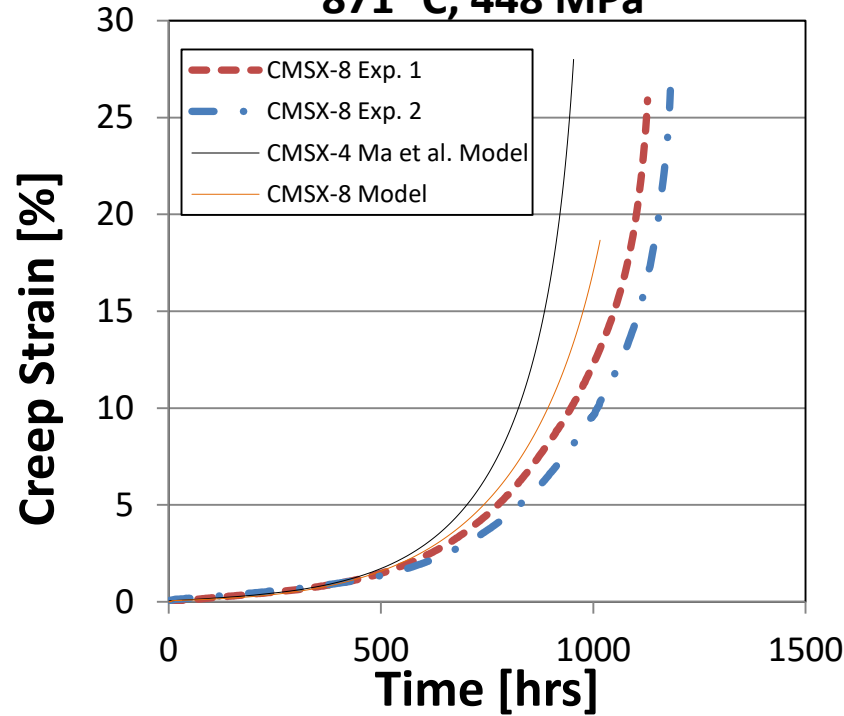




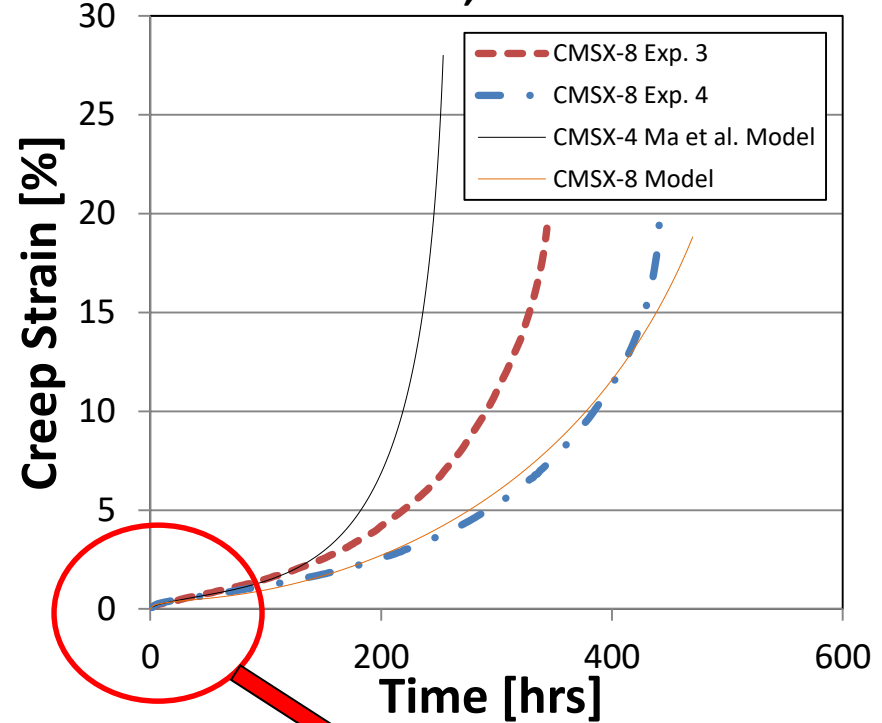




871 °C, 448 MPa

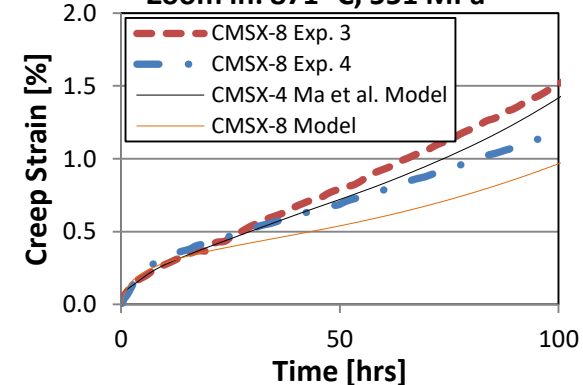


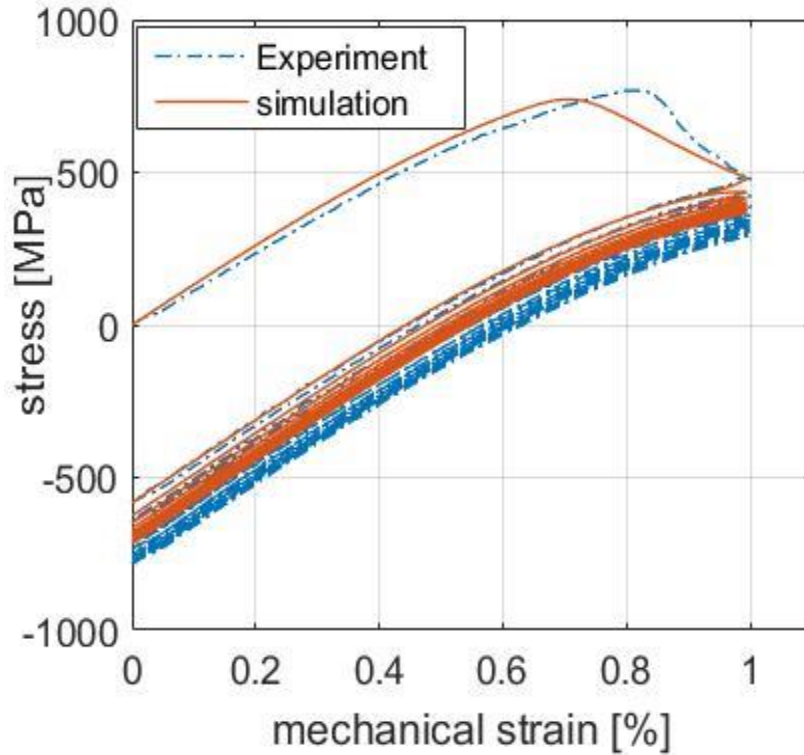
871 °C, 551 MPa



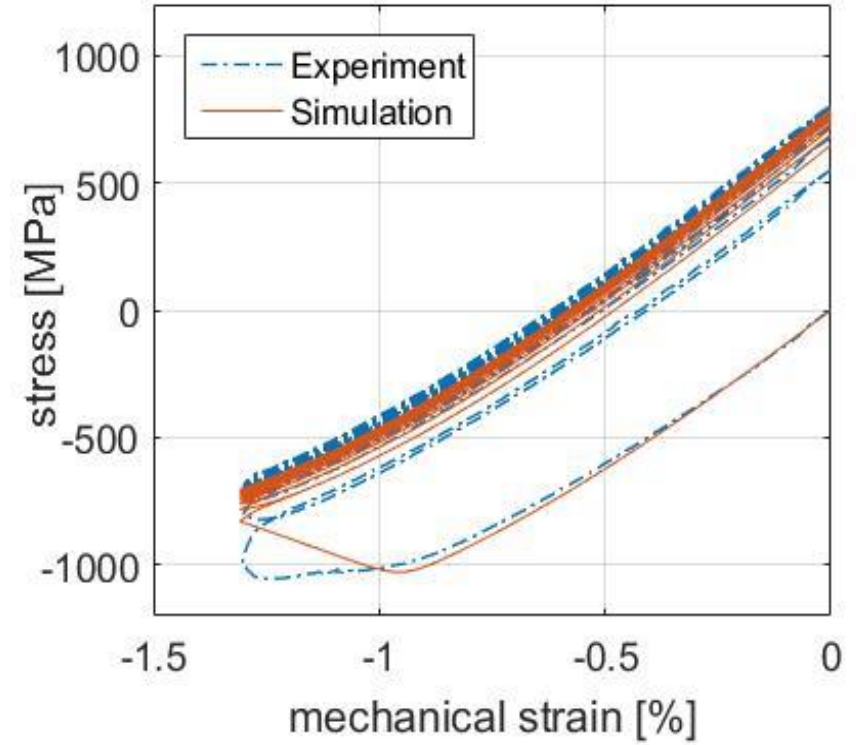
Primary, secondary and tertiary creep can be captured with the model

Zoom in: 871 °C, 551 MPa





First 10 cycles: IP-TMF  
 [100-1100-100] °C,  $R = 0$ ,  $\dot{T} = 2.83$  [°K/s]



Stabilized hysteresis: OP-TMF  
 [100-850-100] °C,  $R = -\infty$ ,  $\dot{T} = 2.83$  [°K/s]

Very good agreement predicting TMF

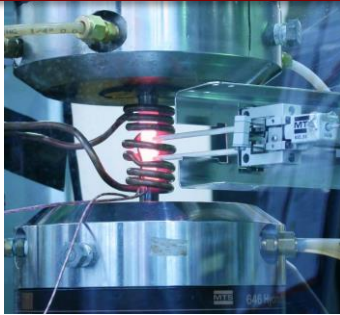
Since Re segregates almost exclusively in the  $\gamma$  channels, the Activation energy in the  $\gamma$  phase can be modified to account for Re content as follows:

$$\left\{ \begin{array}{l} \dot{\gamma}_{\gamma}^{in(\alpha)} = \Theta(T) \rho_{\gamma}^{(\alpha)} b \lambda_{\gamma}^{(\alpha)} F_{attack} \text{sign}(\tau^{(\alpha)} + \tau_{mis}^{(\alpha)} - \chi^{(\alpha)}) \exp \left\{ \frac{-Q_{slip}^{110} + \left( \left| \tau^{(\alpha)} + \tau_{mis}^{(\alpha)} - \chi^{(\alpha)} \right| - \tau_{\gamma pass}^{(\alpha)} - \tau_{oro}^{(\alpha)} \right) V_{c1}^{(\alpha)}}{kT} \right\} \\ \dot{\gamma}_{Li_2}^{in(\alpha)} = \rho_{Li_2}^{(\alpha)} b \lambda_{Li_2}^{(\alpha)} F_{attack} \text{sign}(\tau^{(\alpha)} - \chi^{(\alpha)}) \exp \left\{ \frac{-Q_{slip}^{112} + \left( \left| \tau^{(\alpha)} - \chi^{(\alpha)} \right| - \tau_{Li_2 pass}^{(\alpha)} - \tau_{APB} \right) V_{c2}^{(\alpha)}}{kT} \right\} \end{array} \right.$$

If we considering activation energy for plastic flow  $Q_o$  a function of %Re, the diffusivity parameter could take the form of:

$$\Theta(T) = \exp\left(-\frac{Q_o}{RT}\right) \quad \text{for } T \geq \frac{T_m}{2} \qquad Q(T) = \exp\left(-\frac{2Q_o}{RT} \left[ \ln\left(\frac{T_m}{2T}\right) + 1 \right]\right) \quad \text{for } T \leq \frac{T_m}{2}$$

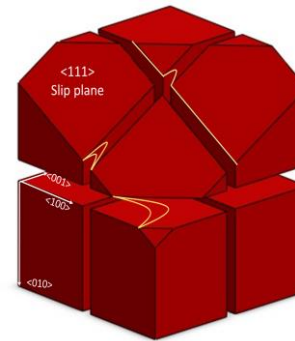
## Creep-Fatigue Interaction Experiments and Lifetime Models



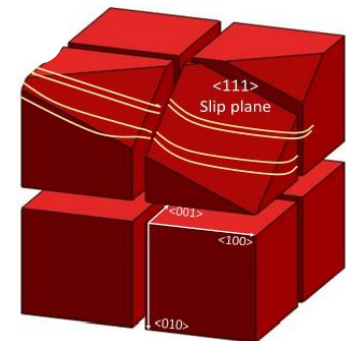
## Microstructure-sensitive Crystal Viscoplasticity (CVP) Model to Determine Service “Process”-Structure-Property Linkages

$$\mathbf{L}^{in} = \dot{\mathbf{F}}^{in} \mathbf{F}^{in-1} = f_{\gamma} \left( \sum_{\alpha=1}^{12} \dot{\gamma}_{\gamma}^{in(\alpha)} (\hat{\mathbf{d}}^{(\alpha)} \otimes \hat{\mathbf{n}}^{(\alpha)}) \right) + f_{\gamma'} \left( \sum_{\alpha=13}^{24} \dot{\gamma}_{L1_2}^{in(\alpha)} (\hat{\mathbf{d}}^{(\alpha)} \otimes \hat{\mathbf{n}}^{(\alpha)}) \right)$$

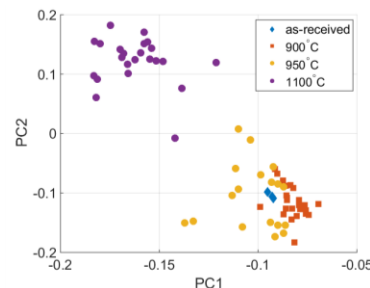
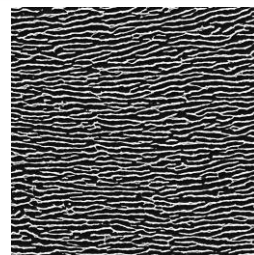
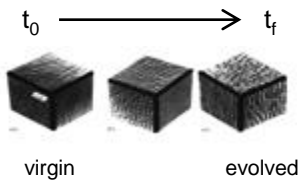
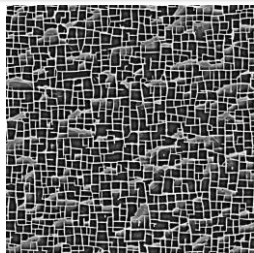
$\gamma$  deformation



$\gamma'$  deformation



## Experiments & Models (both physically-based and data analytics) to Predict Current State of Microstructure (Service Process-Structure Linkages)



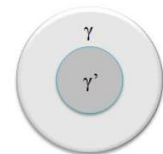
## Established Method to Determine Sensitivity of Local Composition on Diffusivity for Input in Aging and Viscoplasticity Models

Thermo-Calc  
DICTRA

Databases: TCNi5 / MOBNI2



- Composition segregation in  $\gamma$  and  $\gamma'$  phase
- Determination of composition sensitive effective diffusivity to characterize aging activation energy and diffusivity parameter in viscoplasticity models



- Stress-free and stress-assisted (rafting) aging experiments under tensile and compressive stresses
- Establishing process-structure linkages using physical models, 2-point statistics and PCA

This work is supported by



Grant DE-FE0011722