

# Multi-Objective approach to sensor placement in IGCC power plants



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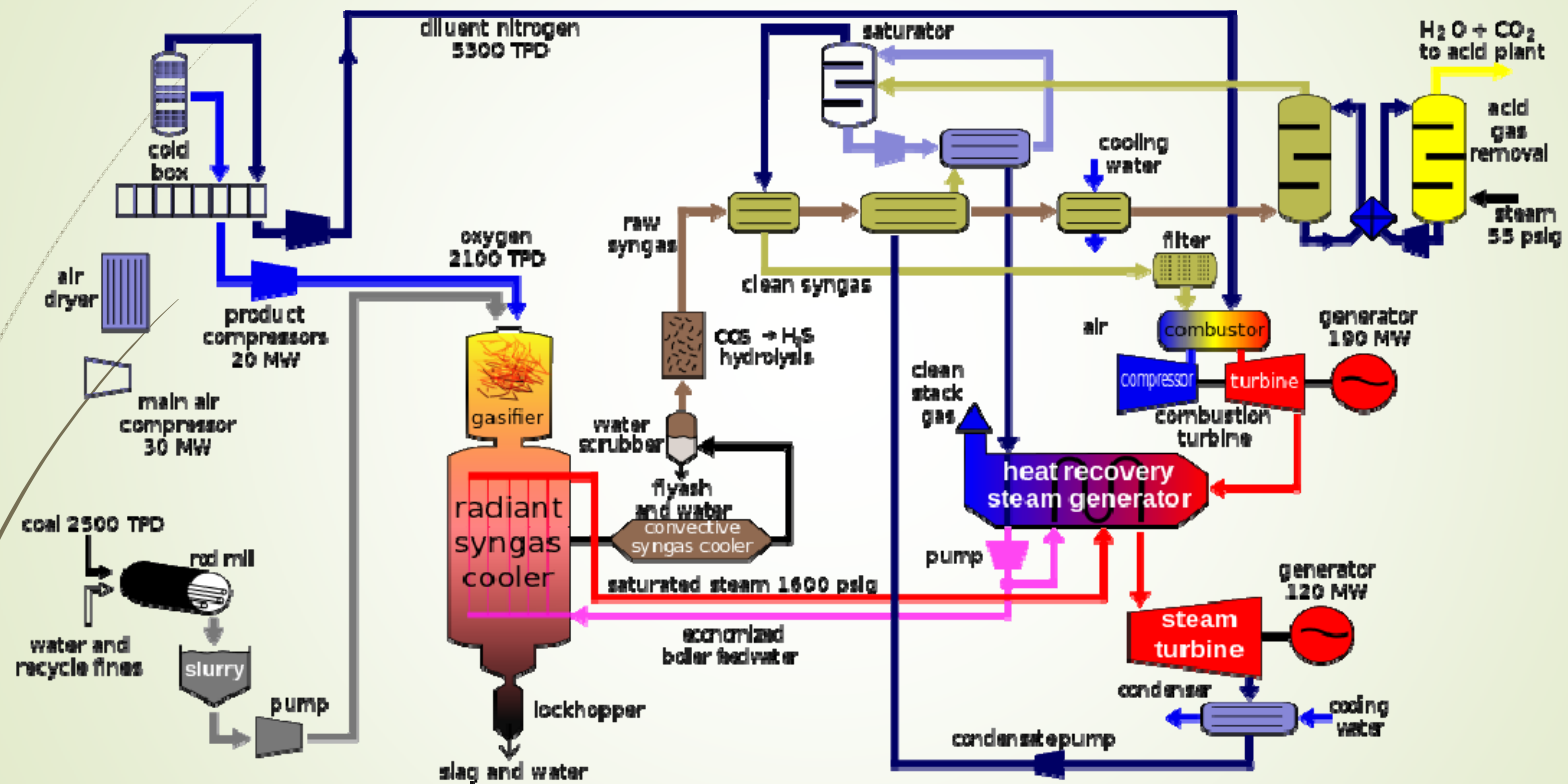
# MOTIVATION & BACKGROUND

## Motivation

- ▶ The U.S. Energy Information Administration (EIA) predicts global demand of energy will rise by 56 % from the year 2010 to 2040.
- ▶ Renewable energy and nuclear power are fastest growing energy sources.
- ▶ Yet, 80% of the world's power is still generated from conventional sources.
- ▶ Conventional fossil fuel based power plants have low efficiency, high environmental impact.
- ▶ IGCC plants are better on both fronts.
- ▶ Hence, it makes sense to invest in research for improving performance of IGCC plants.

## IGCC Power Plant

- More than 80 unit operations
- Over 200 streams



Picture source: Wikipedia

# VIRTUAL SENSING IN IGCC PLANTS

- ▶ The process of estimating value of a variable through mathematical modeling.
  - ▶ *Eliminates need of placing direct physical means of measurement such as a sensor.*
  - ▶ *Two types – analytical and empirical*
- ▶ Advantage - Economical and less-invasive.
  - ▶ *Appropriate choice for IGCC plant due to harsh operating conditions and hundreds of process variables.*
- ▶ Disadvantage - lower measurement accuracy than actual sensing
  - ▶ *High measurement error gives rise to uncertainty in the system.*
  - ▶ *Only variables that are expensive or difficult to measure directly are measured virtually.*

## SENSOR NETWORK – WHY DO WE NEED IT?

### ➤ OBSERVABILITY

- Monitoring and controlling the process variables in real time.
- To maintain all process variables within a safe range of operation at all times.
- Ensures smooth, safe and reliable operation.

### ➤ EFFICIENCY

- Certain variables that directly impact efficiency should be close to target value.
  - *Gasifier temperature*
  - *Steam to air ratio in gasifier*
  - *Air to fuel ratio in gas turbine.*
- If these variables are above or below their optimal values, the plant will run at a sub-optimal level.

# OBJECTIVES & PROBLEM STATEMENT

# OBJECTIVES

## ➤ **METHODOLOGY**

- *Develop sensor deployment methodologies applicable to IGCC power plant systems.*
- *Incorporate measurement error (uncertainty) and non-linear nature of the system in the formulation and solution of the optimal sensor deployment problem.*

## ➤ **ALGORITHM**

- *Develop a new algorithmic framework that can improve the computational efficiency significantly.*

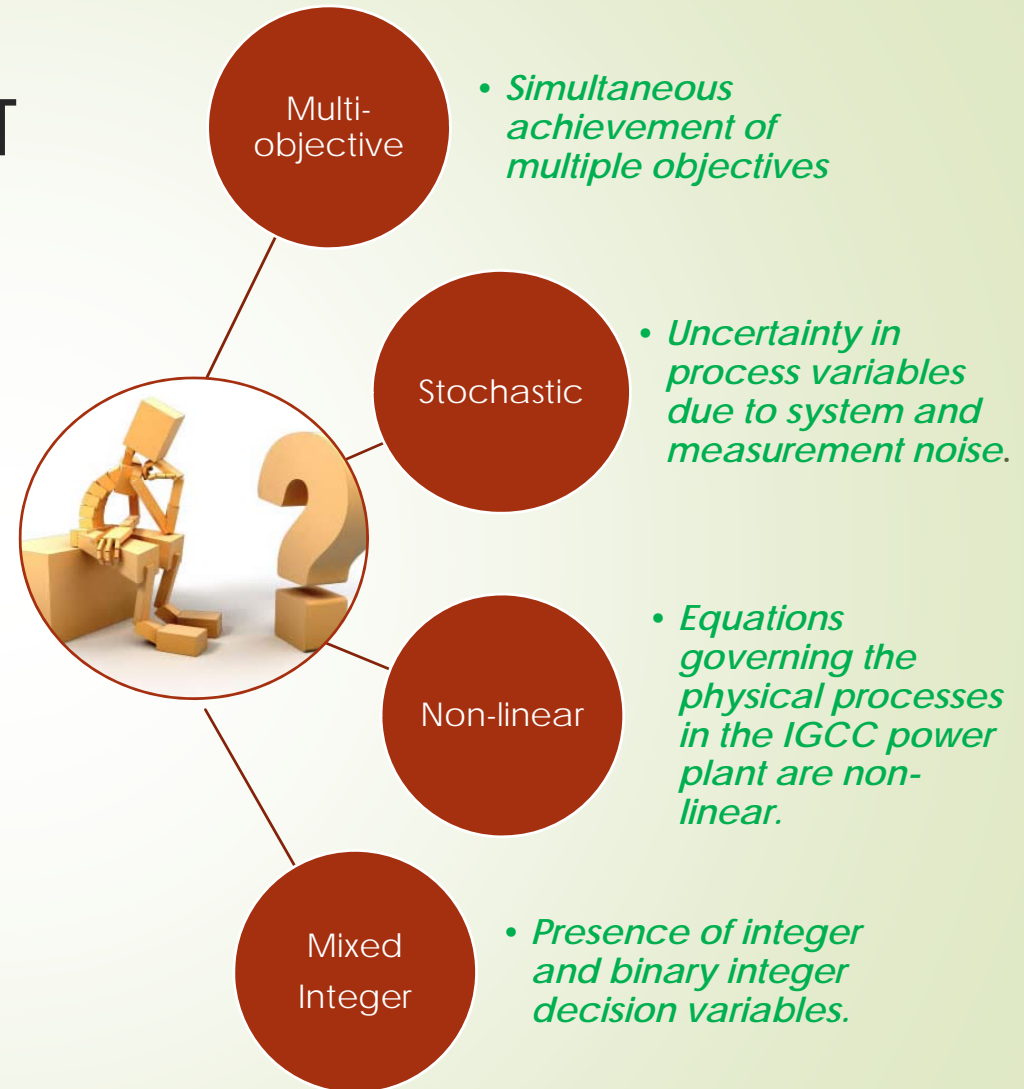
## ➤ **MULTI-OBJECTIVE APPROACH**

- *Develop multi-objective optimal sensor deployment algorithms to provide trade-off designs between various objectives – maximizing observability & maximizing efficiency.*



# PROBLEM STATEMENT

- ▶ Decision variables - *number & location of sensors in the plant and the type of sensors.*
- ▶ Objective functions – *maximizing observability (using FI), maximizing efficiency, minimizing cost.*
- ▶ Constraint – *budget, mass & energy balances.*



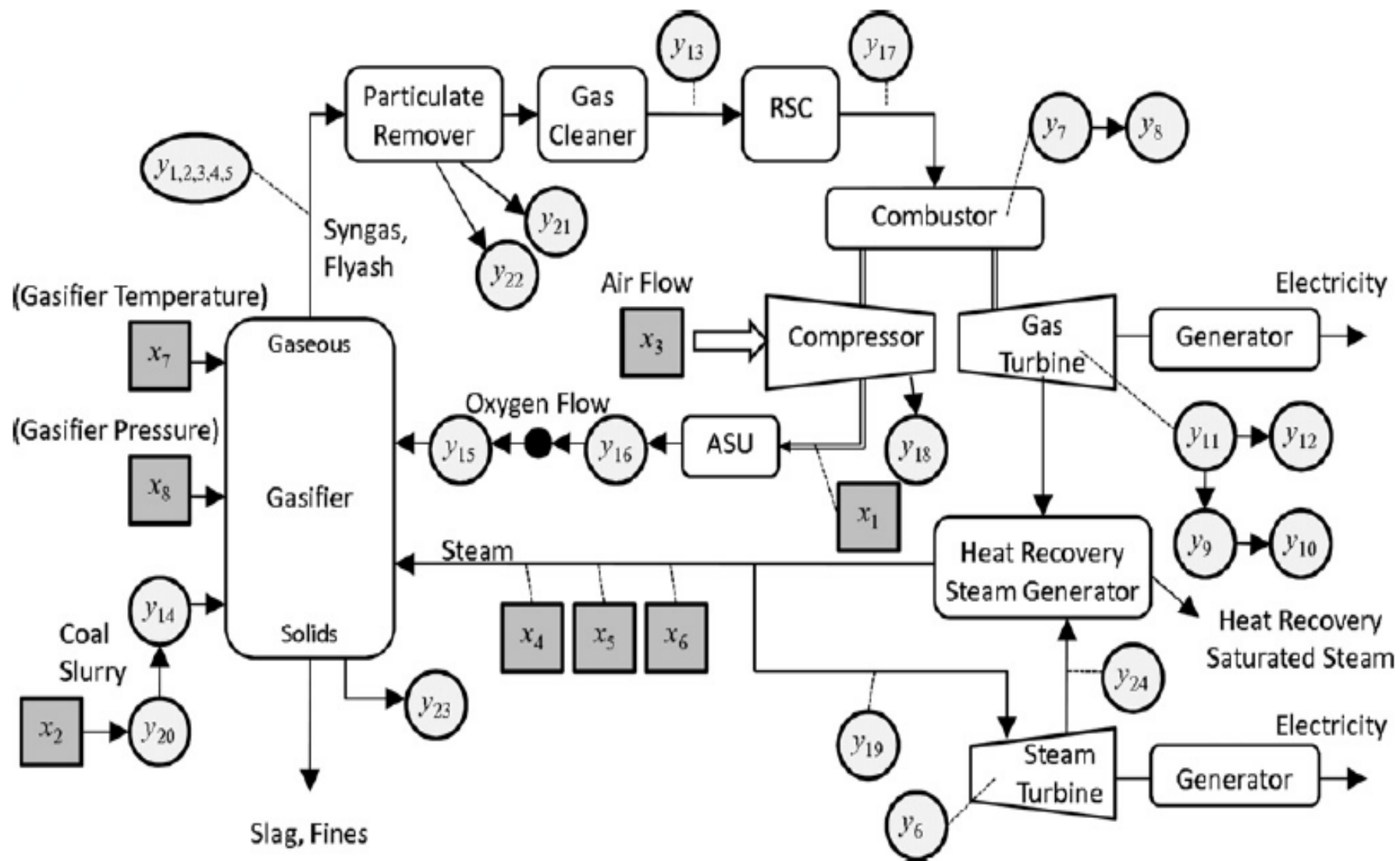
## Variables & Control

- ▶ 24 intermediate variables selected
  - ▶ They have effect on output variables and plant performance.
  - ▶ Sensors are to be installed in these locations
  - ▶ Selected based upon experience
  - ▶ Placing actual sensors reduce measurement error.
  - ▶ Place sensors strategically to gain as accurate information as possible for all these process variables.
- ▶ Without sensor – measurement error is  $\pm 20\%$
- ▶ With sensor
  - ▶ Low cost sensors, error =  $\pm 5\%$
  - ▶ Medium cost sensors, error =  $\pm 2.5\%$
  - ▶ High cost sensors, error =  $\pm 1\%$

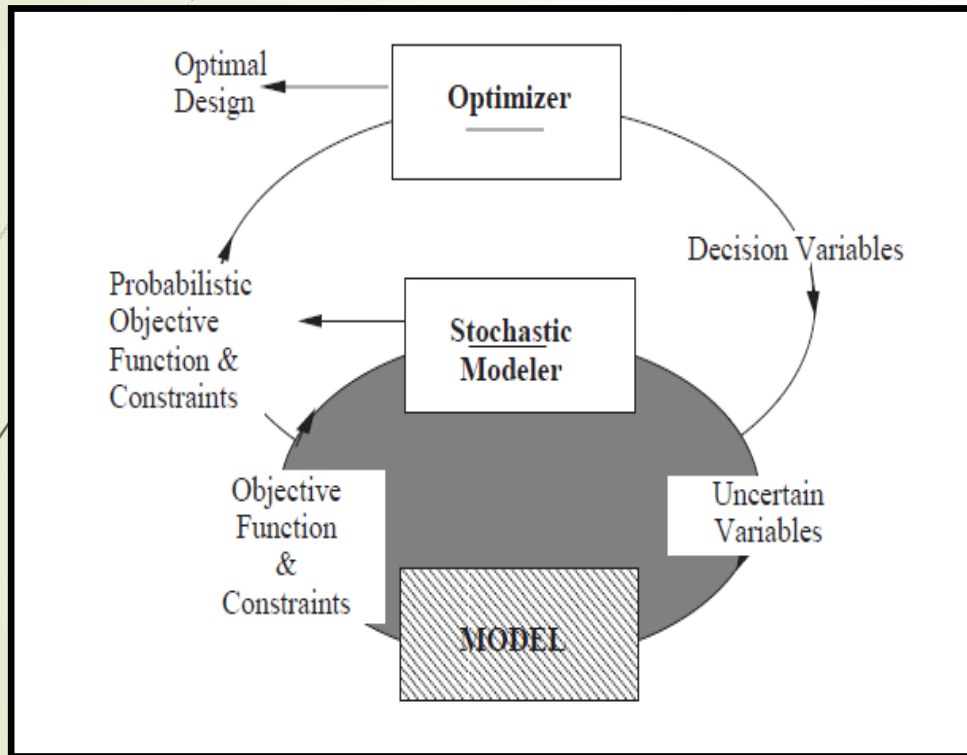
**Table 2**  
Intermediate and output process variables.

$y_j$	Description	Stream <sup>a</sup>	Nominal	Units
1	Gasifier syngas flow rate	RXROUT	393,475	kg/h
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24	Recycled HRSG steam heat output	QRDEA	3.27e8	Btu/h

<sup>a</sup> Stream notation refers to DOE/NETL model [11].



# GENERALIZED STOCHASTIC PROGRAMMING FRAMEWORK



- Specify uncertainties in key input parameters in terms of probability distributions.
- Sample the distribution of the specified parameter in an iterative fashion.
- The model is evaluated for each of these sample points to determine the probabilistic value of objective function & constraints.
- Derivative estimation through perturbation analysis

*Ref: BONUS Algorithm for Large Scale Stochastic Non-linear Stochastic Algorithm Problems, U. Diwekar, A., David, Springer 2013*

# ALGORITHMIC FRAMEWORK BASED ON BONUS

B- Better

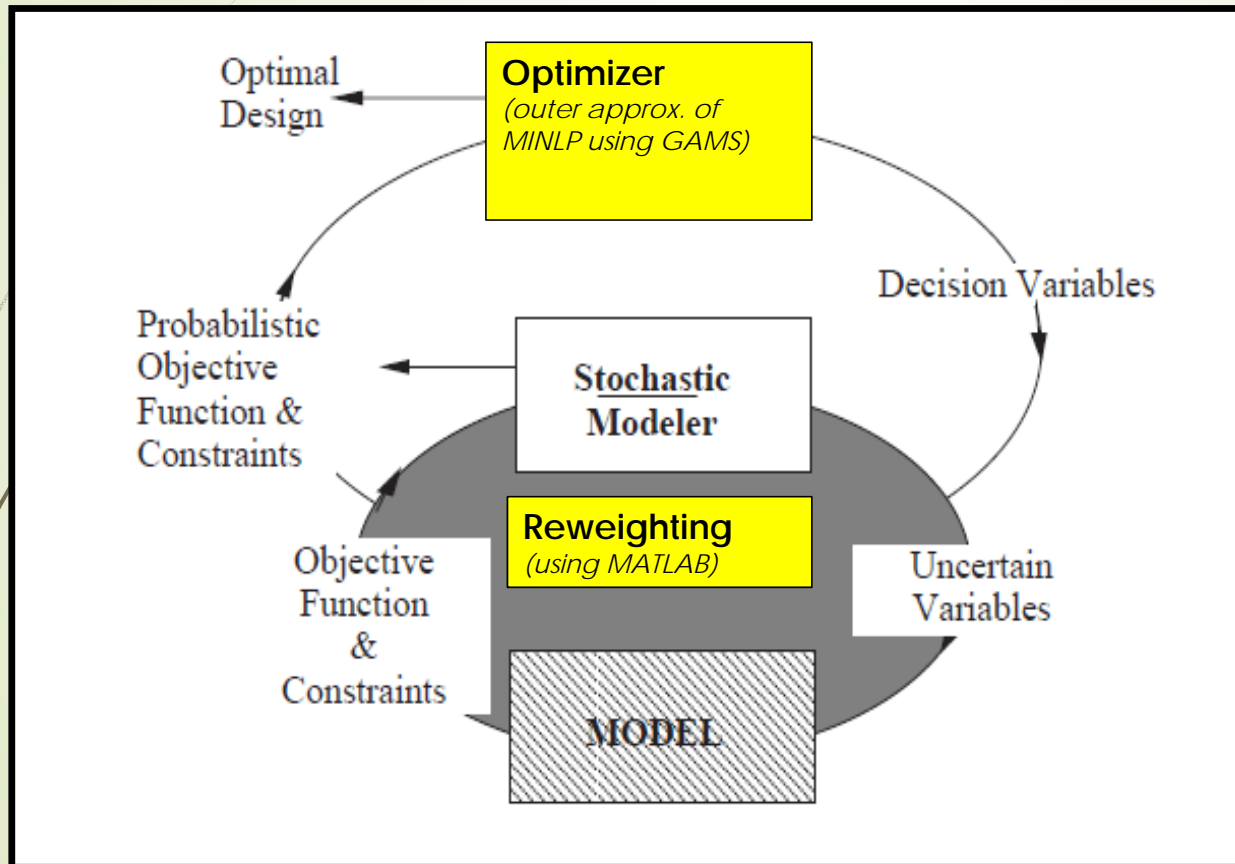
O- Optimization for

N- Non-Linear

U- Uncertain

S- Systems

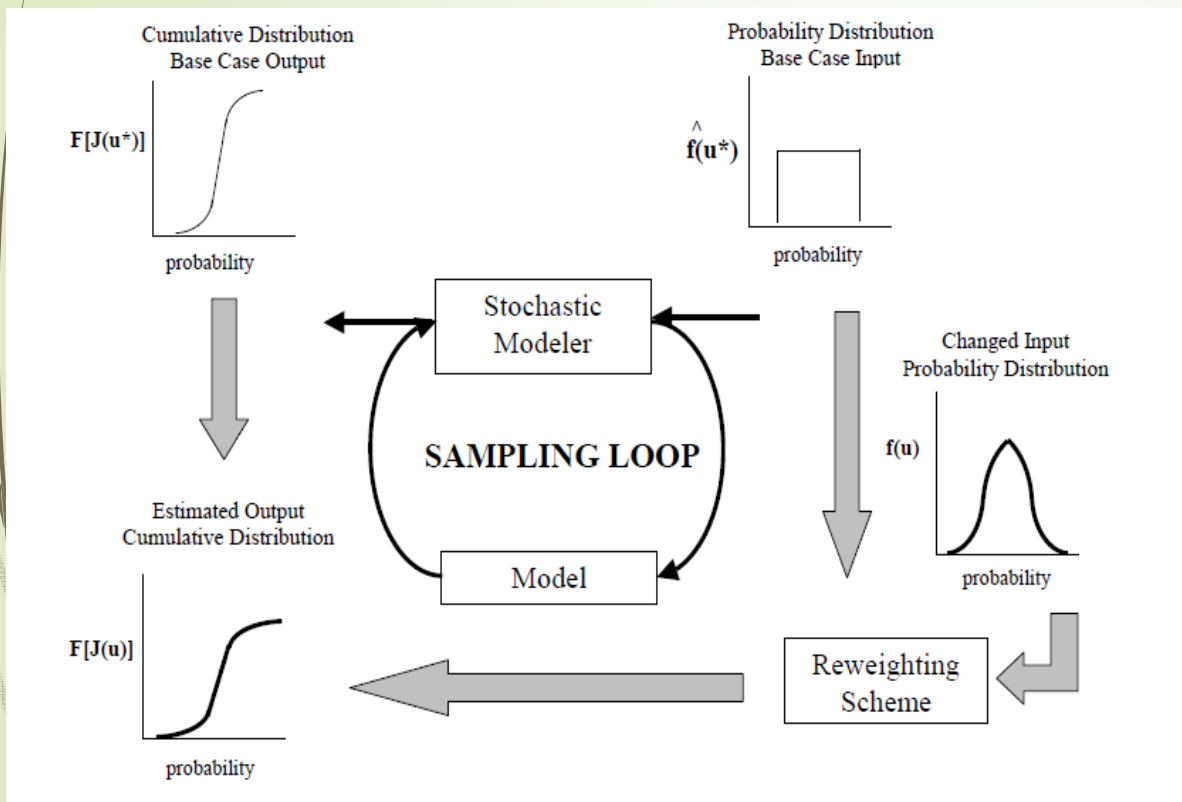
# STOCHASTIC PROGRAMMING FRAMEWORK



*Computational time for 800 samples reduced from 18 hours (ASPEN) to less than a minute (BONUS).*

*Ref: BONUS Algorithm for Large Scale Stochastic Non-linear Stochastic Algorithm Problems, U. Diwekar, A., David, Springer 2013*

# BONUS & Reweighting



Ref: *BONUS Algorithm for Large Scale Stochastic Non-linear Stochastic Algorithm Problems*, U. Diwekar, A., David, Springer 2013

- Initial uniform distributions (lower & upper bound) assumed for decision variables.
- PDFs of Decision & uncertain variables form base distributions.
- BONUS samples solution space of objective function using base distributions.
- As decision variables change, the distributions for the objective function & constraints also change.
- BONUS algorithm estimates objective function & constraints based on ratios of the probabilities for the current and the base distributions.
- Thus, BONUS avoids sample model runs in subsequent iterations.



# MULTI-OBJECTIVE OPTIMIZATION

## Multi-objective approach

- Objectives: maximize fisher information, efficiency, minimize cost
- Constraint method, a posterior method for generating pareto set where
  - *The multi-objective problem is transformed into a series of single objective problems.*
  - *Any single objective is optimized while the rest are converted into constraints with lower & upper bounds.*
- Lower bound to cost corresponds to using no sensors, i.e., zero (0).
- Upper bound to cost corresponds to using high accuracy sensors for all 24 locations.

## STEPS IN OUR SOLUTION

- ▶ 2-tier constraint method
- ▶ To derive only feasible solutions, Divide cost values into 10 bins between upper and lower bound.
- ▶ For each cost, solve single optimization problem to maximize efficiency and calculate the corresponding FI.
- ▶ Similarly, for each cost, solve single optimization problem to maximize FI and calculate the corresponding efficiency.

## STEPS (contd..)

- ▶ Derive upper & lower bounds of efficiency & FI & generate pay-off tables for each cost,
- ▶ For each pay-off table, select feasible values of efficiency in small increments and solve single optimization problems to find maximum FI for each of these values.
- ▶ Generate the complete pareto surface (trade-offs) by solving multiple single objective problems.
- ▶ Plot the complete pareto surface and analyze.

# MAXIMIZING FISHER INFORMATION

$$\max_{\mathbf{w}, \tau \in \mathcal{W}} \sum_{\tau=1}^3 \sum_{j=1}^{Sout} f_{j, \tau}(\mathbf{w}, \mathbf{Y}) w_{j, \tau}$$

Subject to

$$\sum_{\tau=1}^3 \sum_{j=1}^{Sout} C_{j, \tau} w_{j, \tau} \leq B \quad j=1, 2, \dots, Sout.$$

$$\sum_{\tau=1}^3 w_{j, \tau} \leq 1,$$

Mass & Energy Balances

$$f_j^A(\mathbf{w}, \mathbf{Y}) = 1 - I_{Y_j}^{ns}(\theta_{y_j}) / I_{Y_j}^s(\theta_{y_j} | \mathbf{w}_j = \mathbf{1}),$$

- Fisher information: a probabilistic nonlinear function
- Constraint on cost
- Stochastic Mixed integer nonlinear programming problem

# MAXIMIZING EFFICIENCY

$$\max_{w_{j,\tau} \in W} \sum_{\tau=1}^3 \sum_{j=1}^{S_{out}} E_{j,\tau}(w, Y) w_{j,\tau}$$

$$\sum_{\tau=1}^3 \sum_{j=1}^{S_{out}} C_{j,\tau} w_{j,\tau} \leq B$$

$$\sum_{\tau=1}^3 w_{j,\tau} \leq 1, \quad j = 1, 2, \dots, S_{out}$$

Mass & Energy Balances

- Second Objective – maximize expected value of plant thermal Efficiency
- Constraint – budget
- Efficiency depends upon only certain variables – coal feed rate, gas turbine electric power, steam turbine electric power etc.

$$E = \frac{P_{wrnet}}{F_{coalc} * F_{mf} * H_{OC}}$$

# Mass & Energy balance equations:

The mass balance equation is given by:

$$\frac{dM_i}{dt} = \sum Y_{i,\text{in}} \dot{M}_{\text{in}} - \sum Y_{i,\text{out}} \dot{M}_{\text{out}} + \sum R_i$$

The energy balance equation is given by:

$$\frac{dU}{dt} = \sum \dot{H}_{i,\text{in}} - \sum \dot{H}_{j,\text{out}} + \sum \dot{Q}_k + \sum P_m$$

Where

- $Y_{i,\text{in}}$  = mass concentration of content  $i$  in inlet flow
- $\dot{M}_{\text{in}}$  = inlet mass flow rate
- $Y_{i,\text{out}}$  = mass concentration of content  $i$  in outlet flow
- $\dot{M}_{\text{out}}$  = outlet mass flow rate
- $R_i$  = net production rate of  $i$  by chemical reactions.

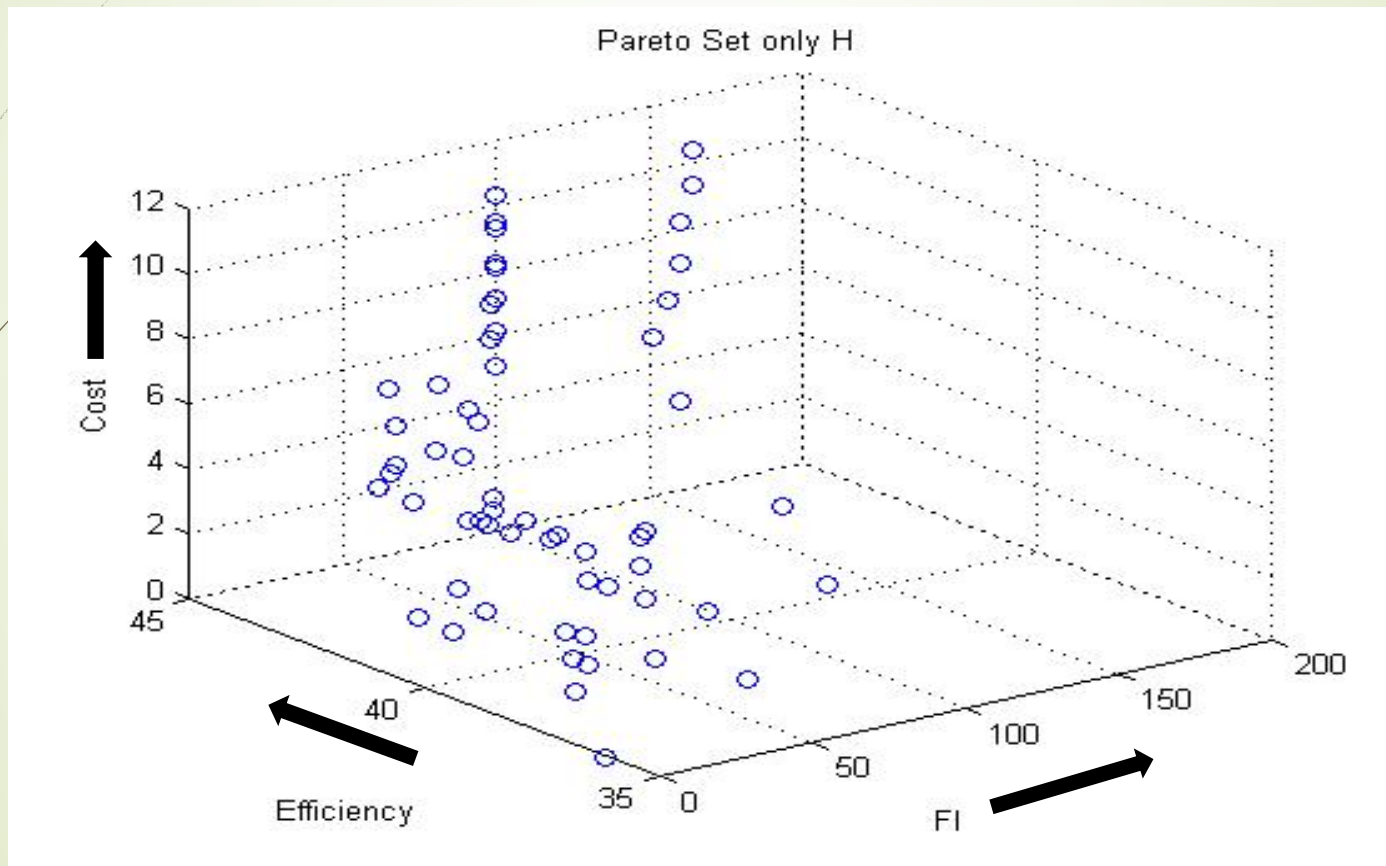
Where

- $U$  = internal energy in block
- $\dot{H}_{i,\text{in}}$  = enthalpy flow rate of content  $i$  in the inlet flow
- $\dot{H}_{j,\text{out}}$  = enthalpy flow rate of content  $j$  in the outlet flow
- $\dot{Q}_k$  = heat flow
- $P_m$  = mechanical power.

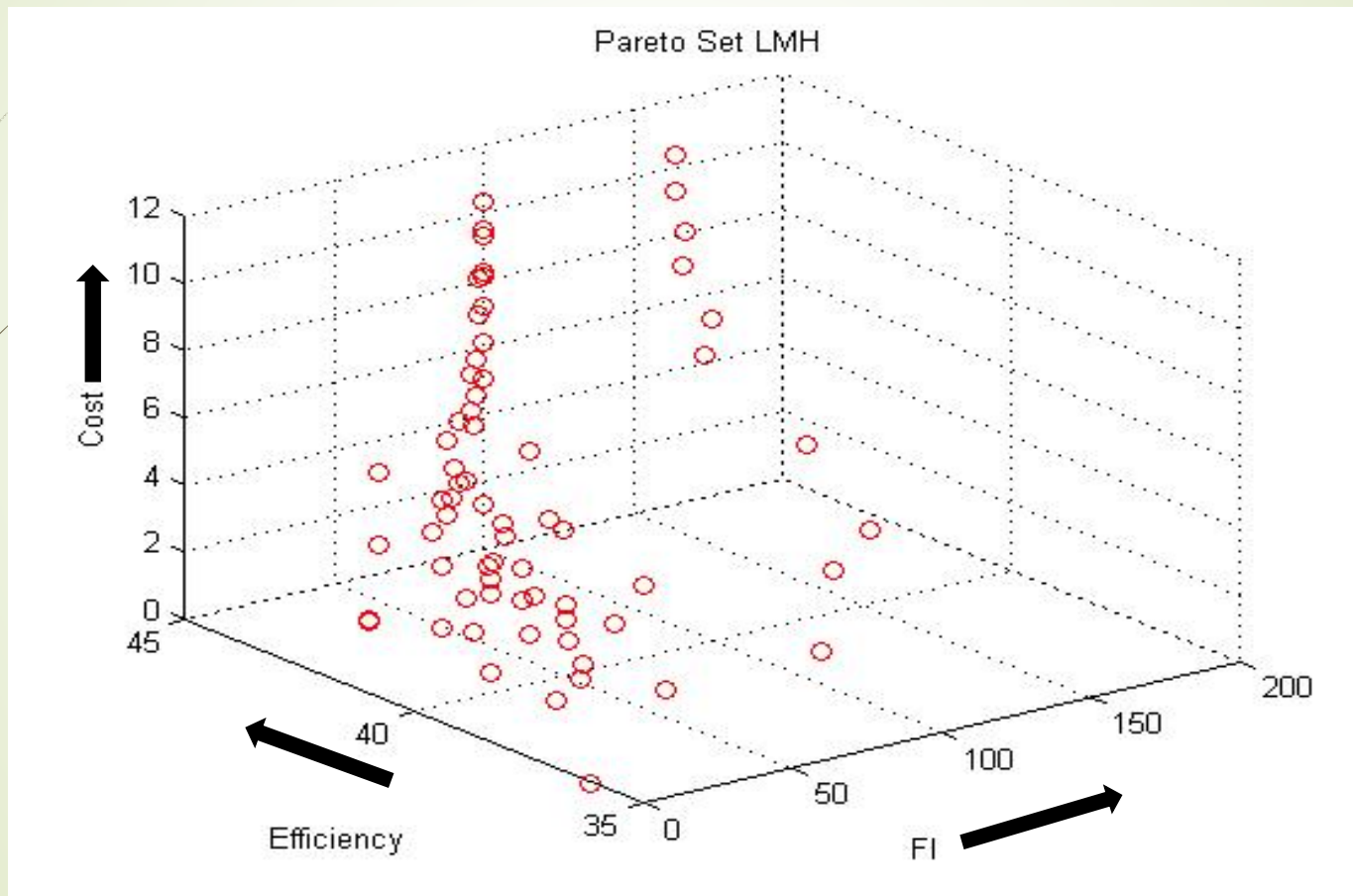
# RESULTS & DISCUSSIONS



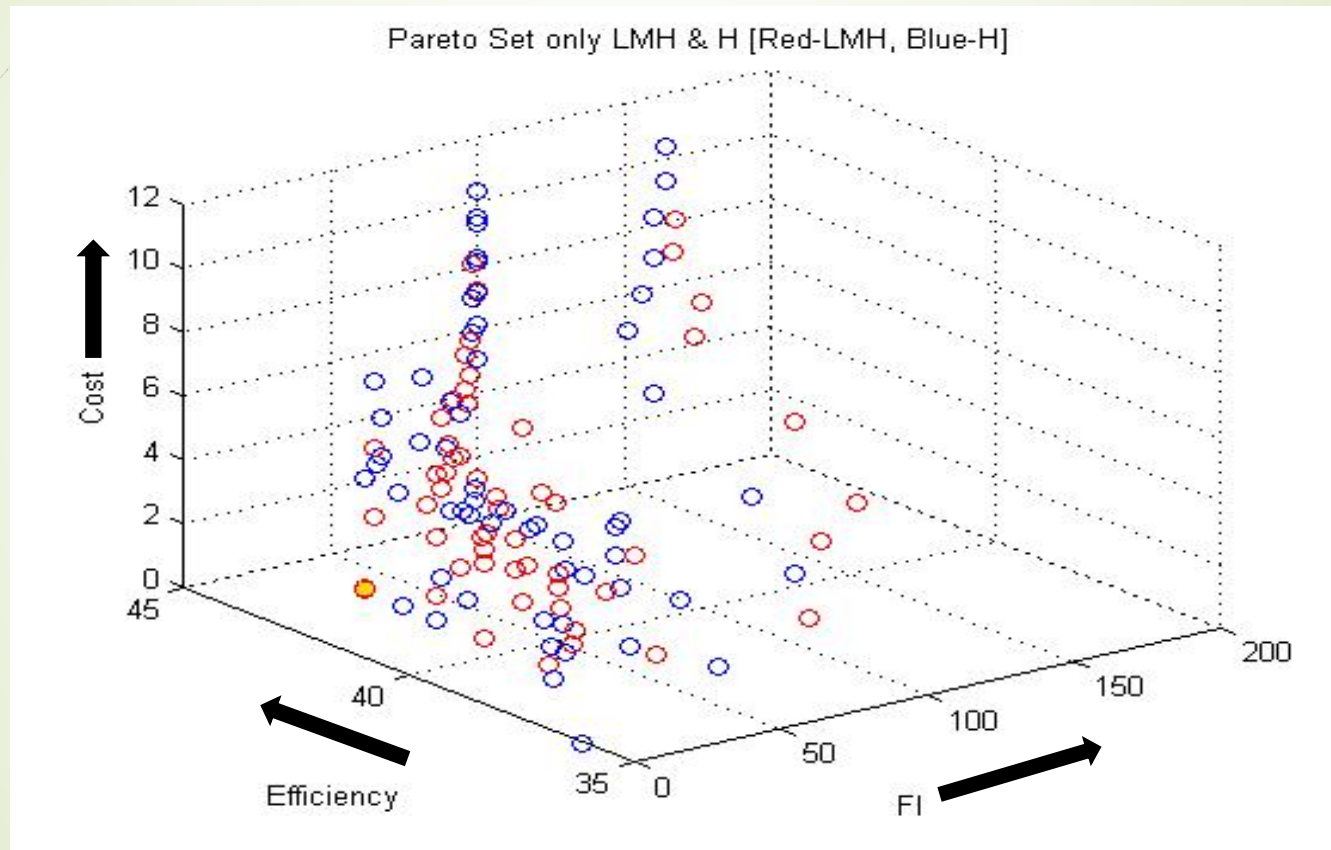
## Pareto set using only High Accuracy Sensors



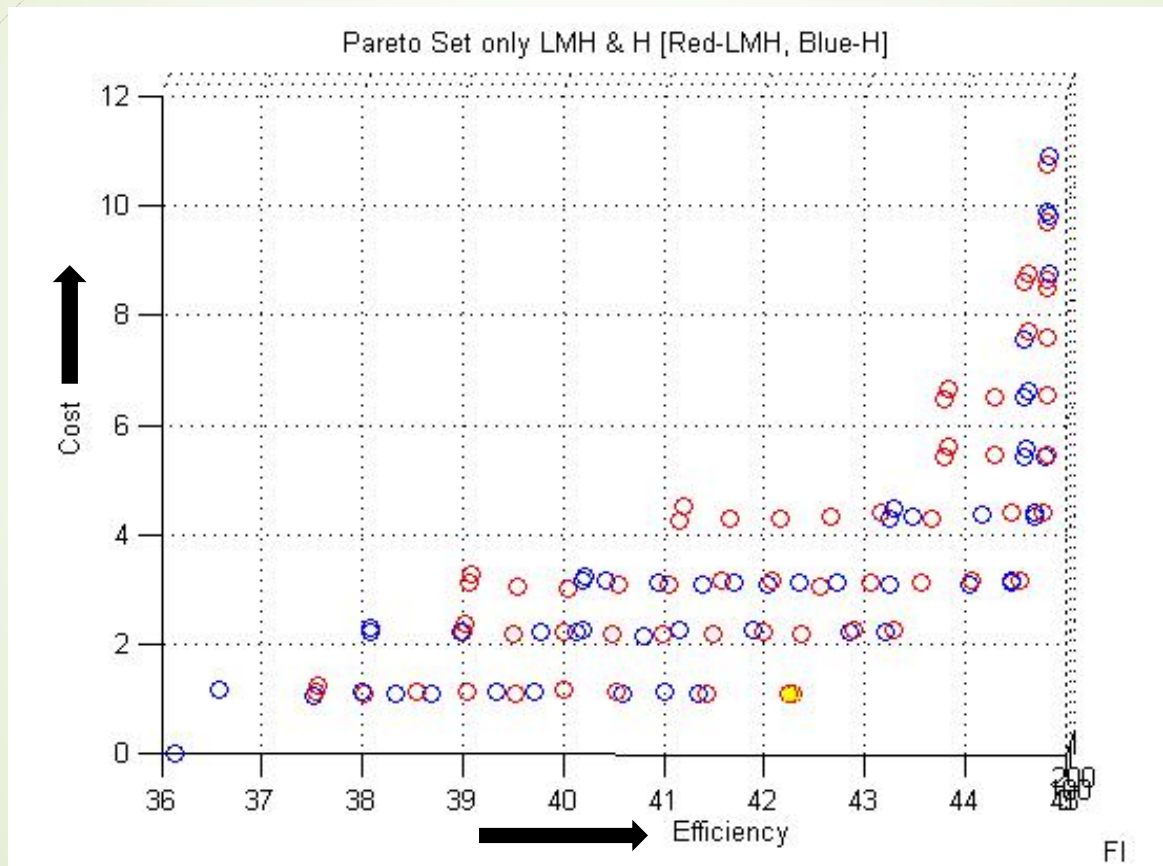
## Pareto set using Low, Medium & High Accuracy Sensors



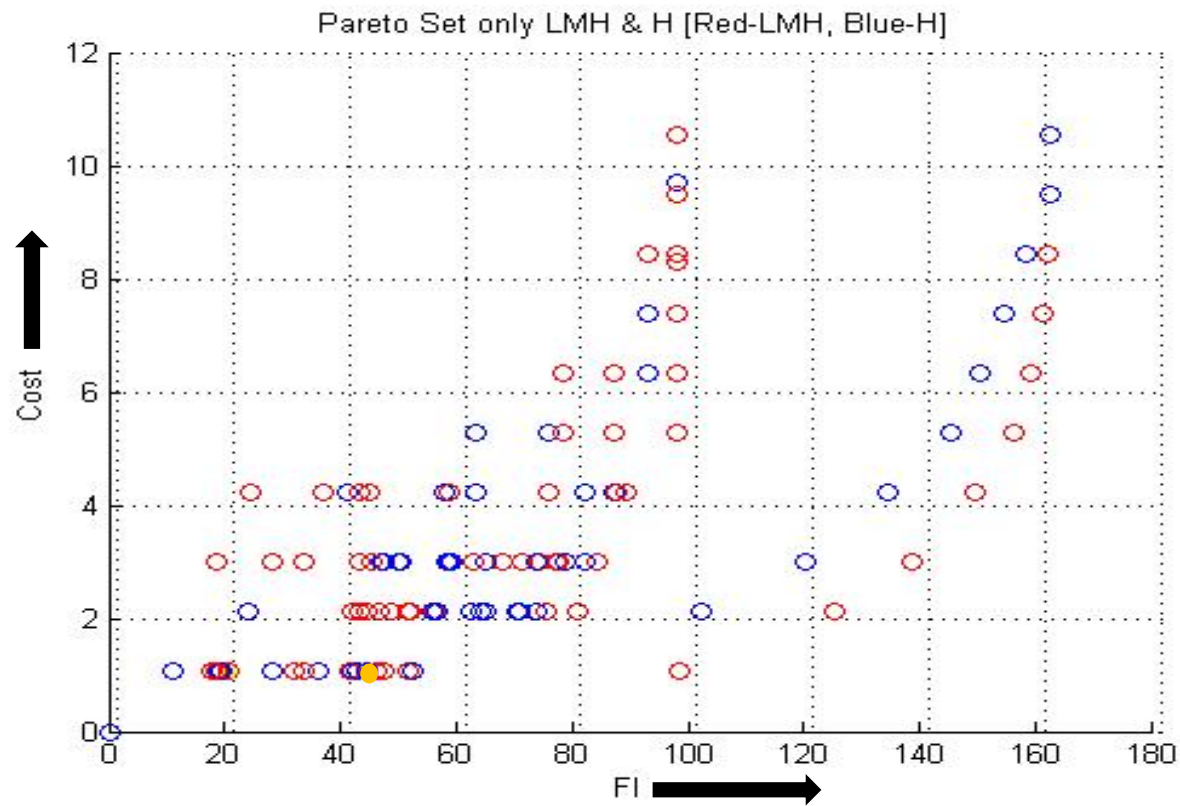
## Low Cost – High efficiency



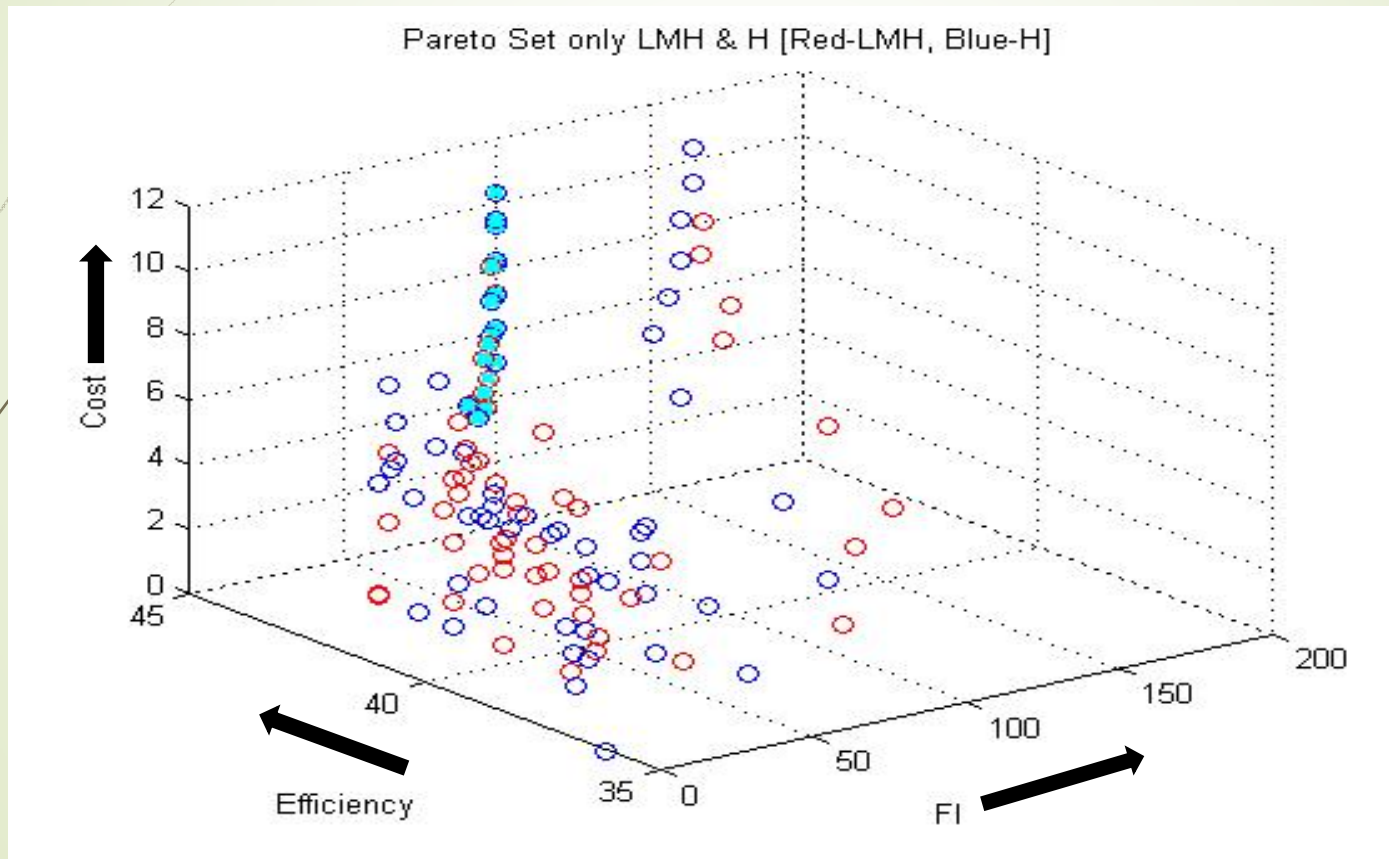
# Low Cost – High efficiency



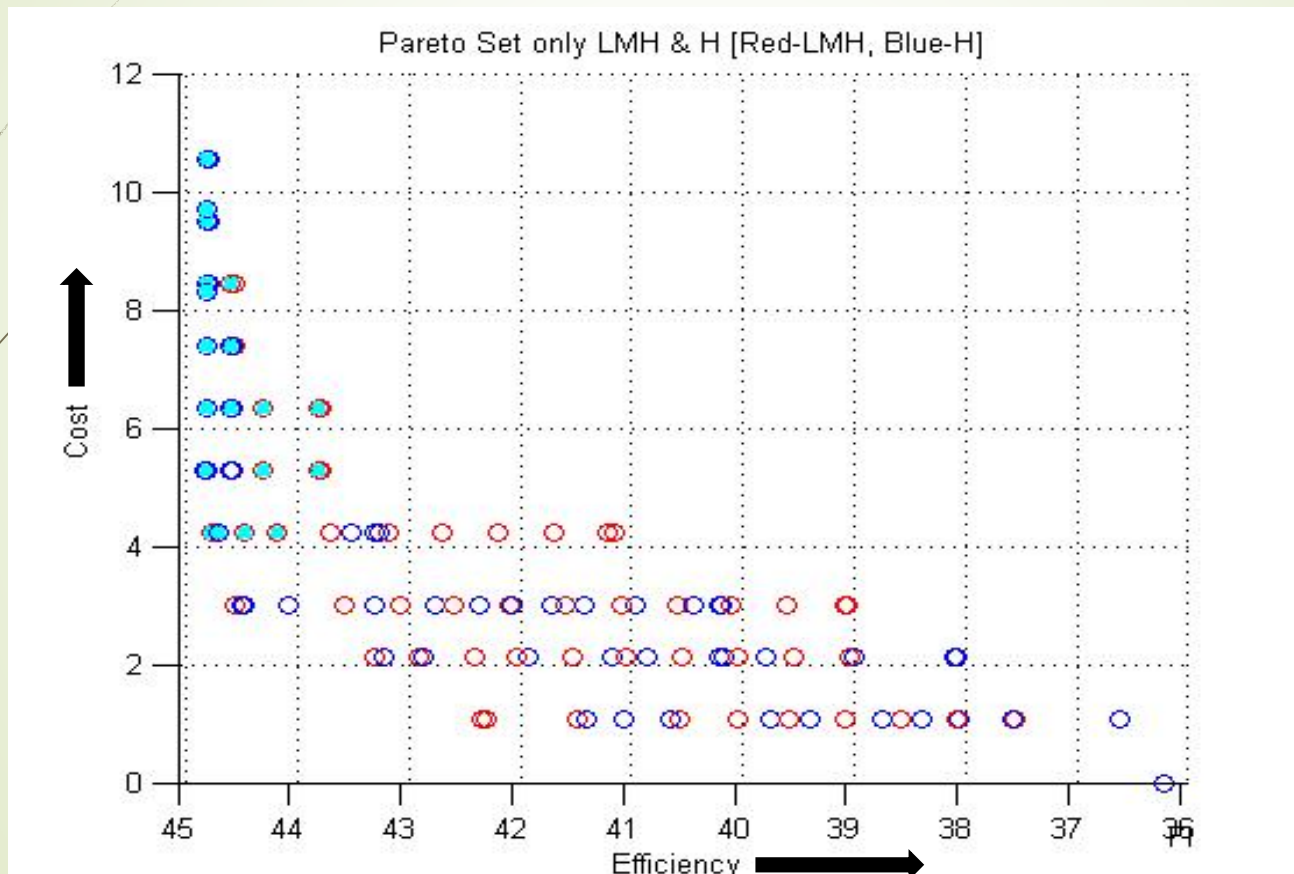
# Low Cost – Low FI – High Efficiency



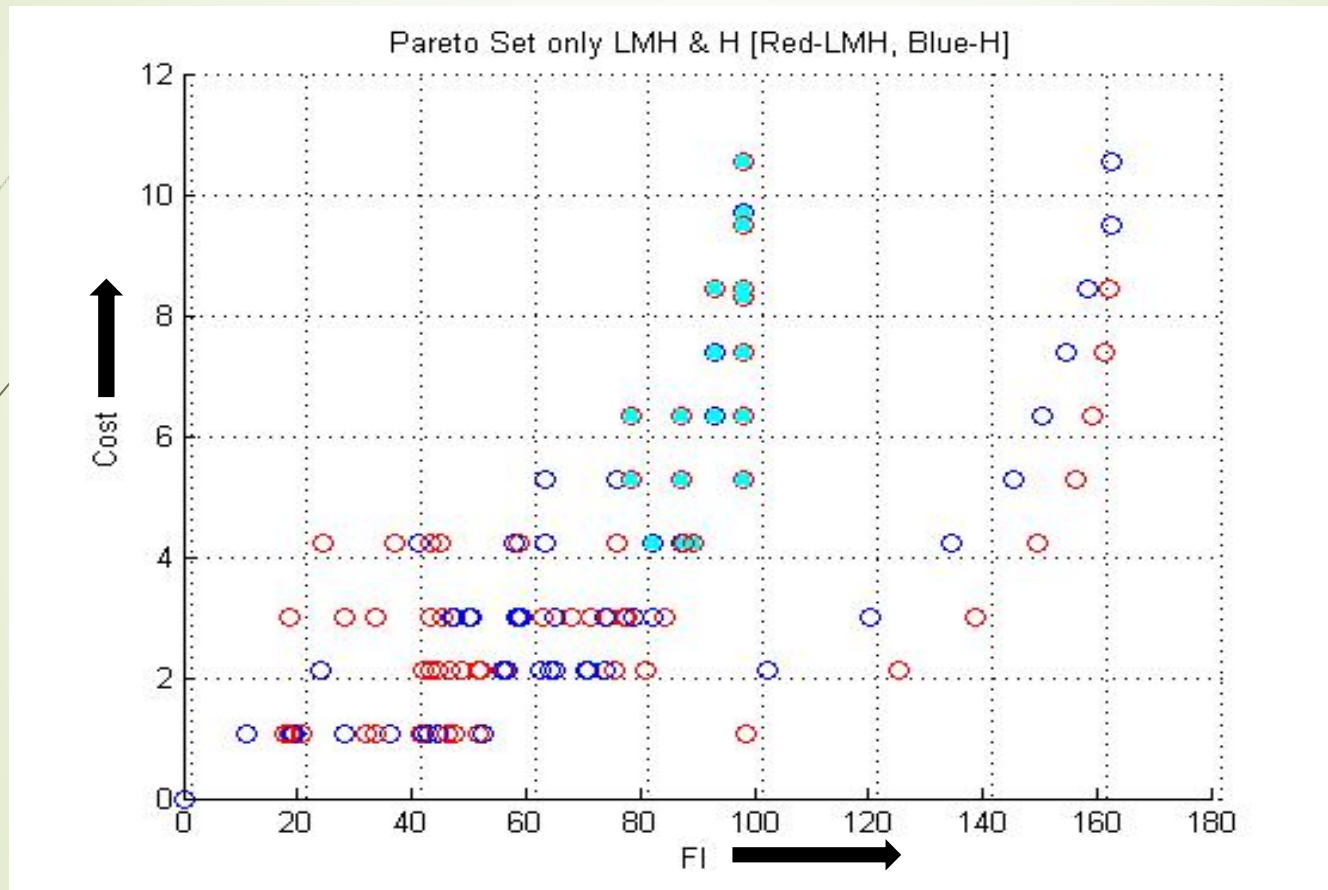
## High Cost – High Efficiency – low FI



# High Cost – High Efficiency – low FI

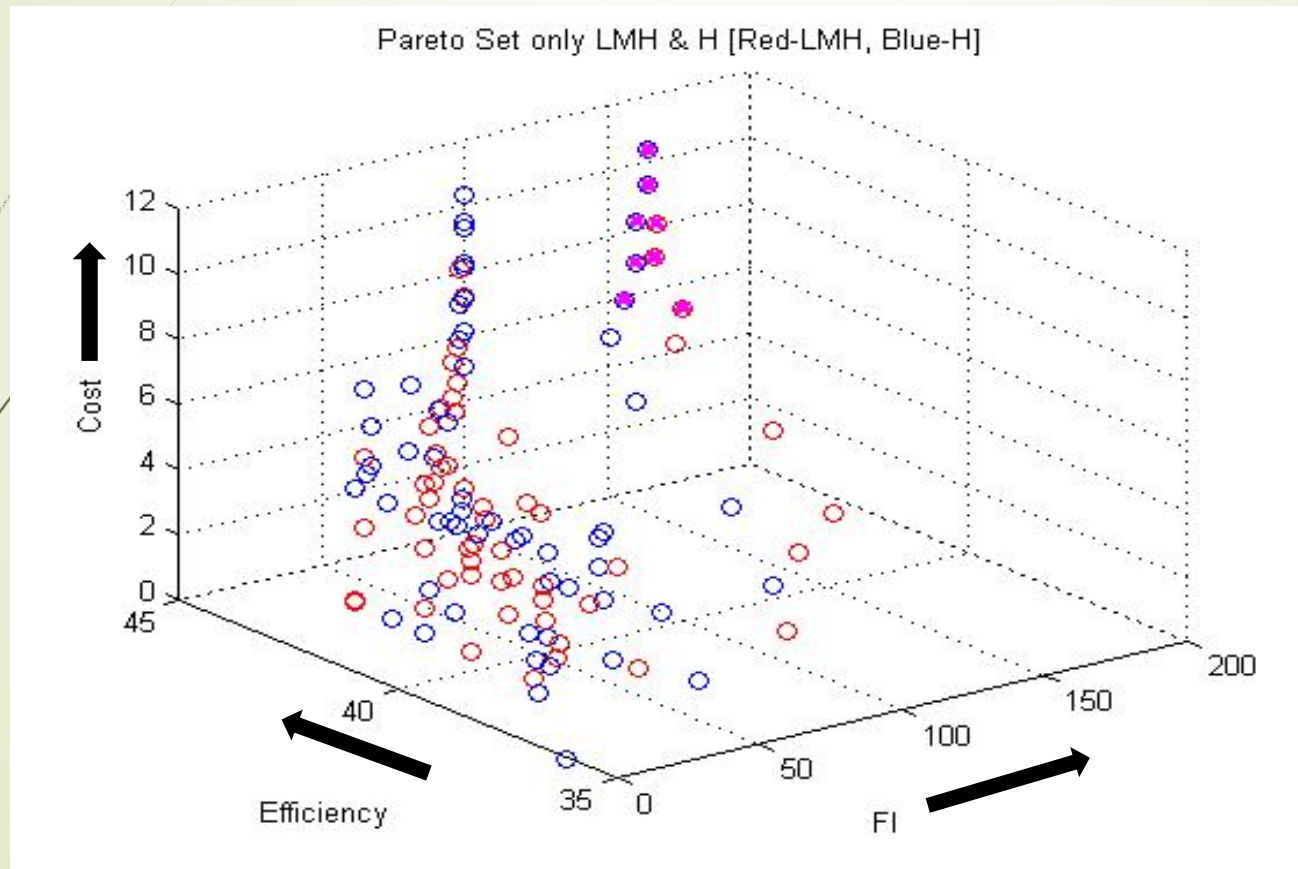


# High Cost – High efficiency – low FI

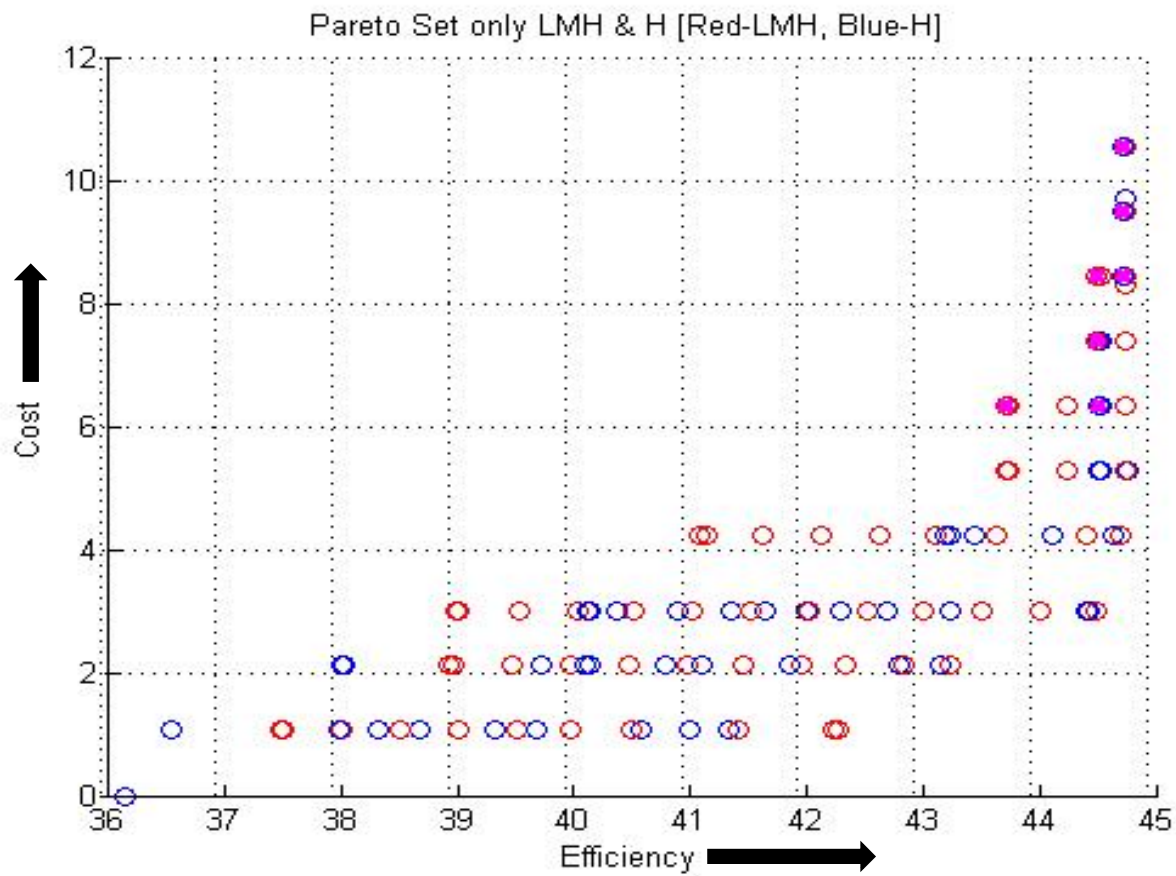




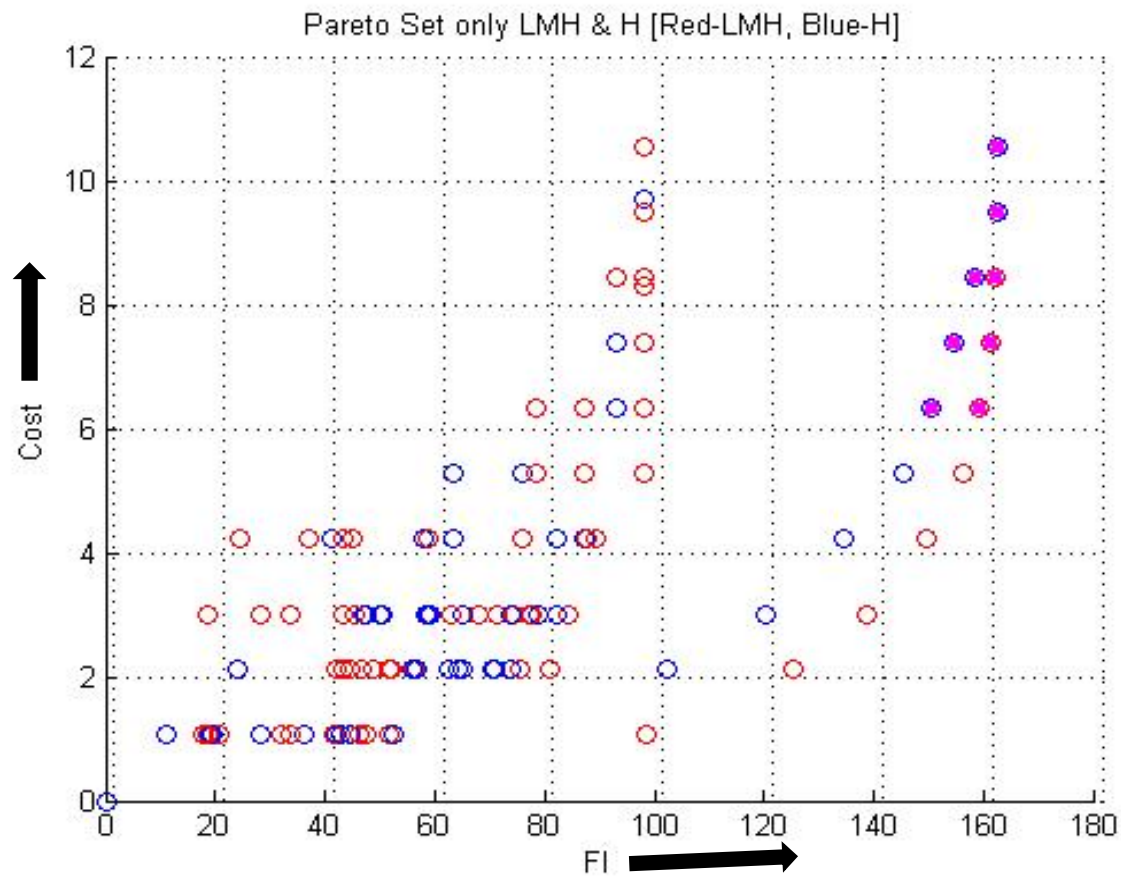
# High Cost – High efficiency – High FI



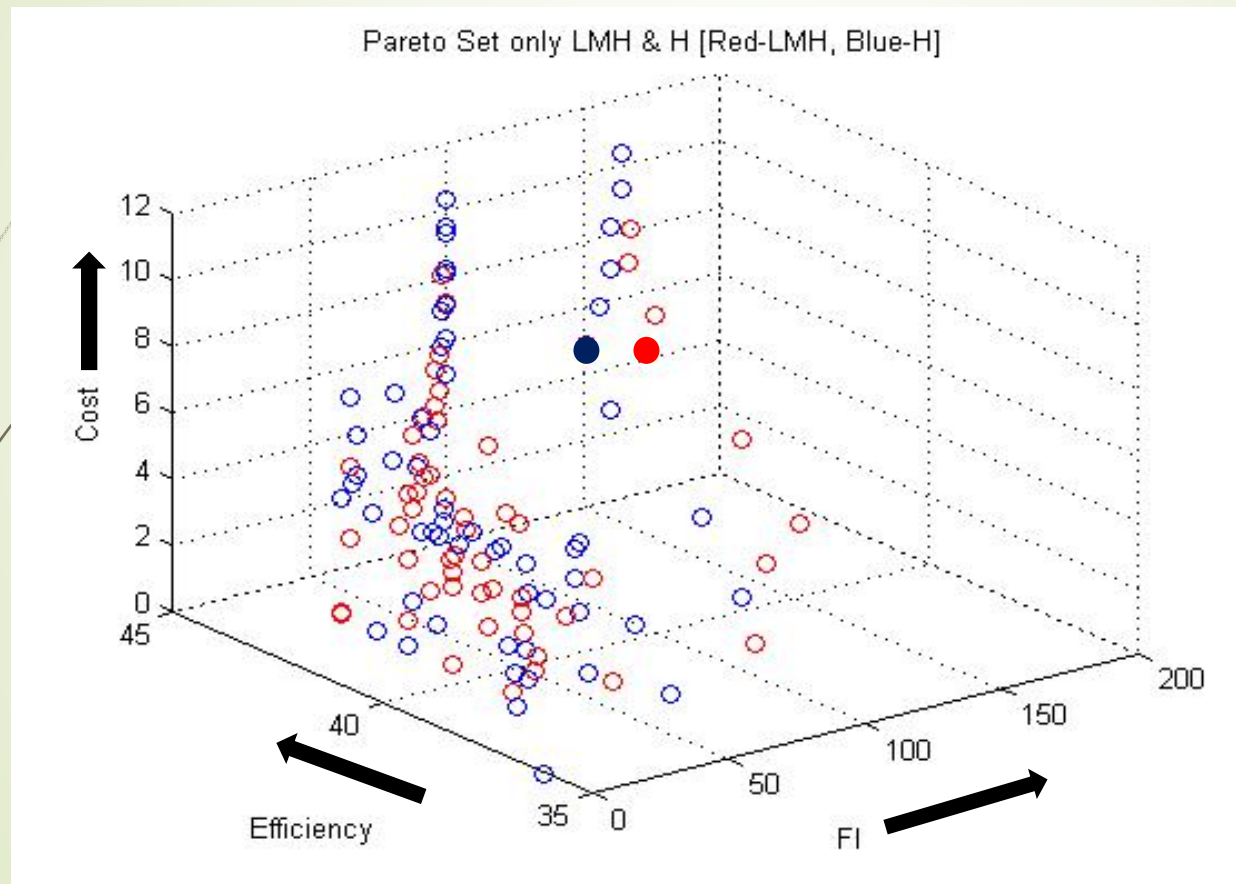
# High Cost – High efficiency – High FI



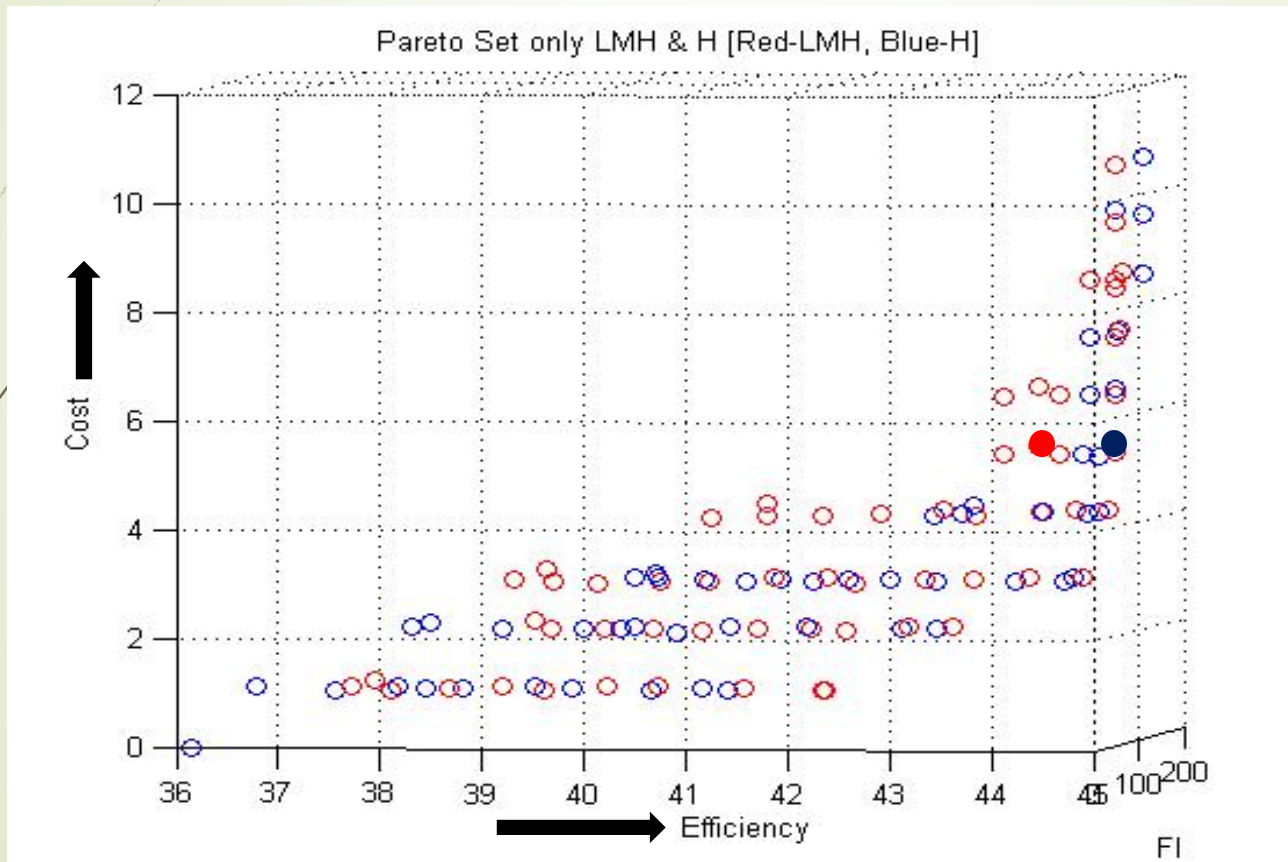
# High Cost – High efficiency – High FI



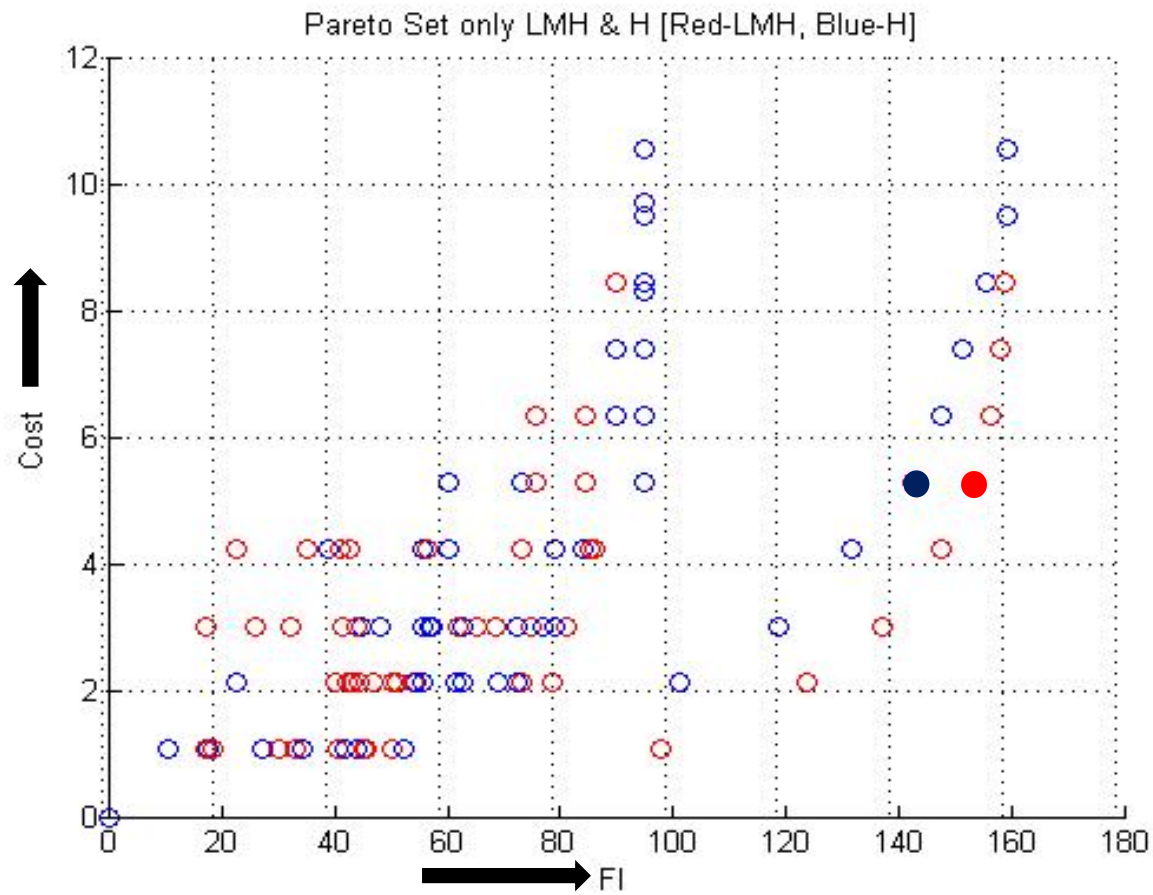
# Moderate Cost – High efficiency – High FI



# Moderate Cost – High efficiency – High FI



# Moderate Cost – High efficiency – High FI



## Sensor Locations – L, M, H sensors

Sensor Locations																							
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
H	M	L	M	H	M	L	L	L	L	L	-	H	H	H	H	H	L	-	H	L	L	L	-

Cost - \$5275000, FI - 154.81, Efficiency - 0.4377

L- 10, M-3, H-8, Nil - 3

## Sensor Locations – only H sensors

Sensor Locations																							
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
H	H	H	H	H	-	-	-	H	H	H	-	H	H	H	H	H	-	-	H	-	-	-	-

Cost - \$5275000, FI - 144.04, Efficiency - 0.4456

H-13, Nil - 11

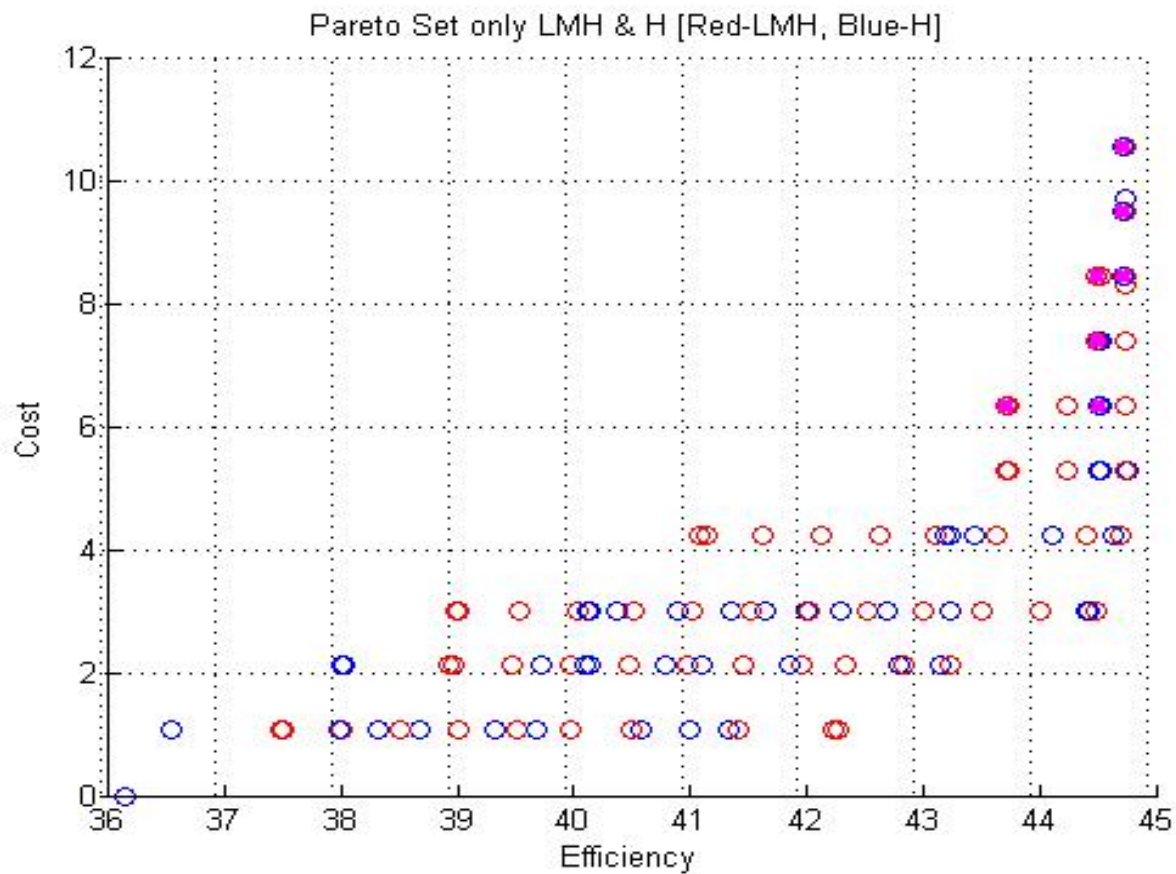
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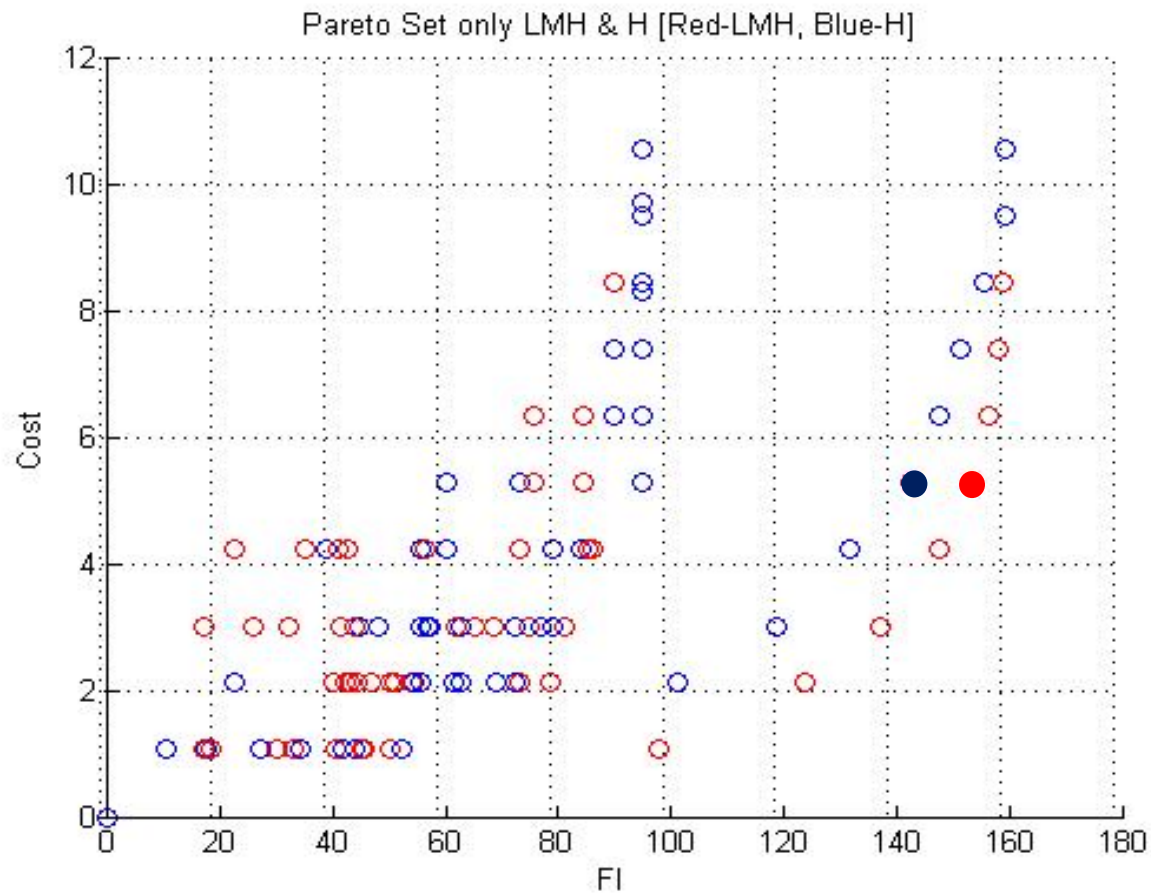
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# High Cost – High efficiency – High FI



## Moderate Cost – High efficiency – High FI



# INFERENCES

- ▶ Maximizing efficiency is cheaper than maximizing FI.
- ▶ Even if we are trying to maximize efficiency, a budget of \$5.27 million is sufficient.
- ▶ Even if we are trying to maximize both, a budget of \$ 7.38 million is sufficient.

## SUMMARY

- ▶ Initial sample generated from ASPEN
- ▶ Off-line APSEN simulations for the fixed number of samples
- ▶ Algorithmic framework based on BONUS for single objective optimization
- ▶ Feasible solutions by fixing cost bins apriori
- ▶ 2-tier constraint method for solving multi-objective optimization.
- ▶ Pareto surface generation for decision makers
- ▶ Analysis of pareto surface can help determine the solution for desired trade-off.

## KEY CONTRIBUTIONS

Objectives satisfied

- Developed sensor deployment methodology which incorporates non-linearity and uncertainty - a framework for virtual sensing and hybrid hardware and virtual sensing in power plants.
- Developed computationally efficient algorithm -significant reduction in the number of model runs to be solved for optimization and the number of samples for the uncertainty analysis
- Obtained tradeoffs between multiple objectives.

## FUTURE WORK

- Comparison of stochastic approach to SND with dynamic simulation approach to determine which is more computationally efficient.
- Include other objective functions, e.g., CO<sub>2</sub> capture efficiency.
- Application of this methodology to dynamic sensor problems.
- Extension of this methodology to other systems which have a black box model.

Thank  
You