



# **Large Scale Screening** of Low cost **Ferritic Steel** Designs for **Advanced Ultra-SuperCritical** Boiler Using **First Principles** **Methods**

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# Outline

**Background**

**Goal**

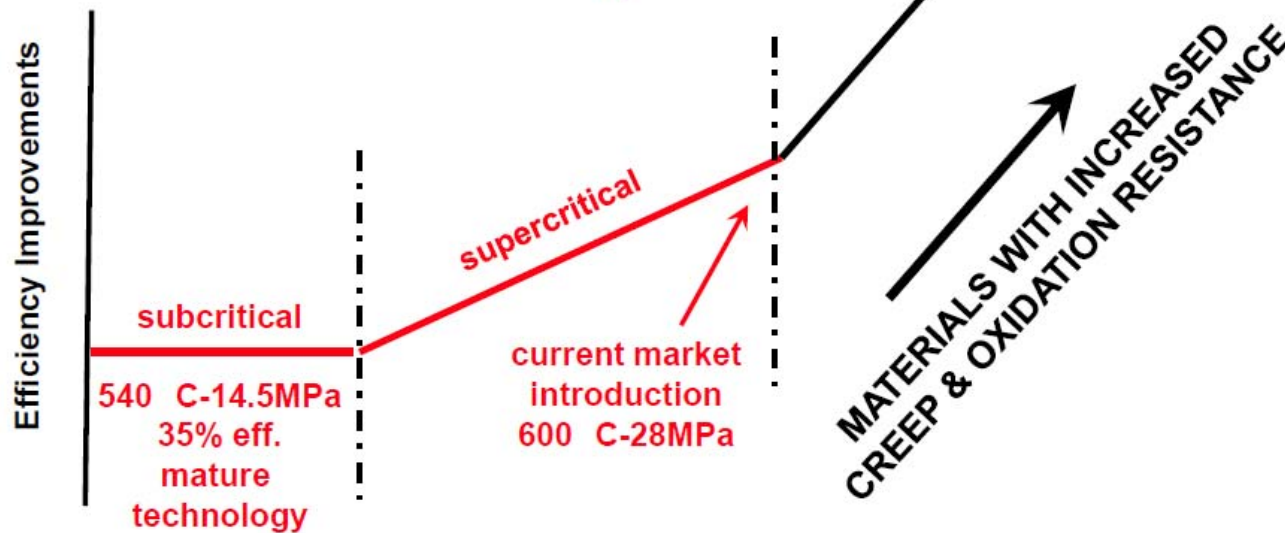
**Approach**

**Project status**

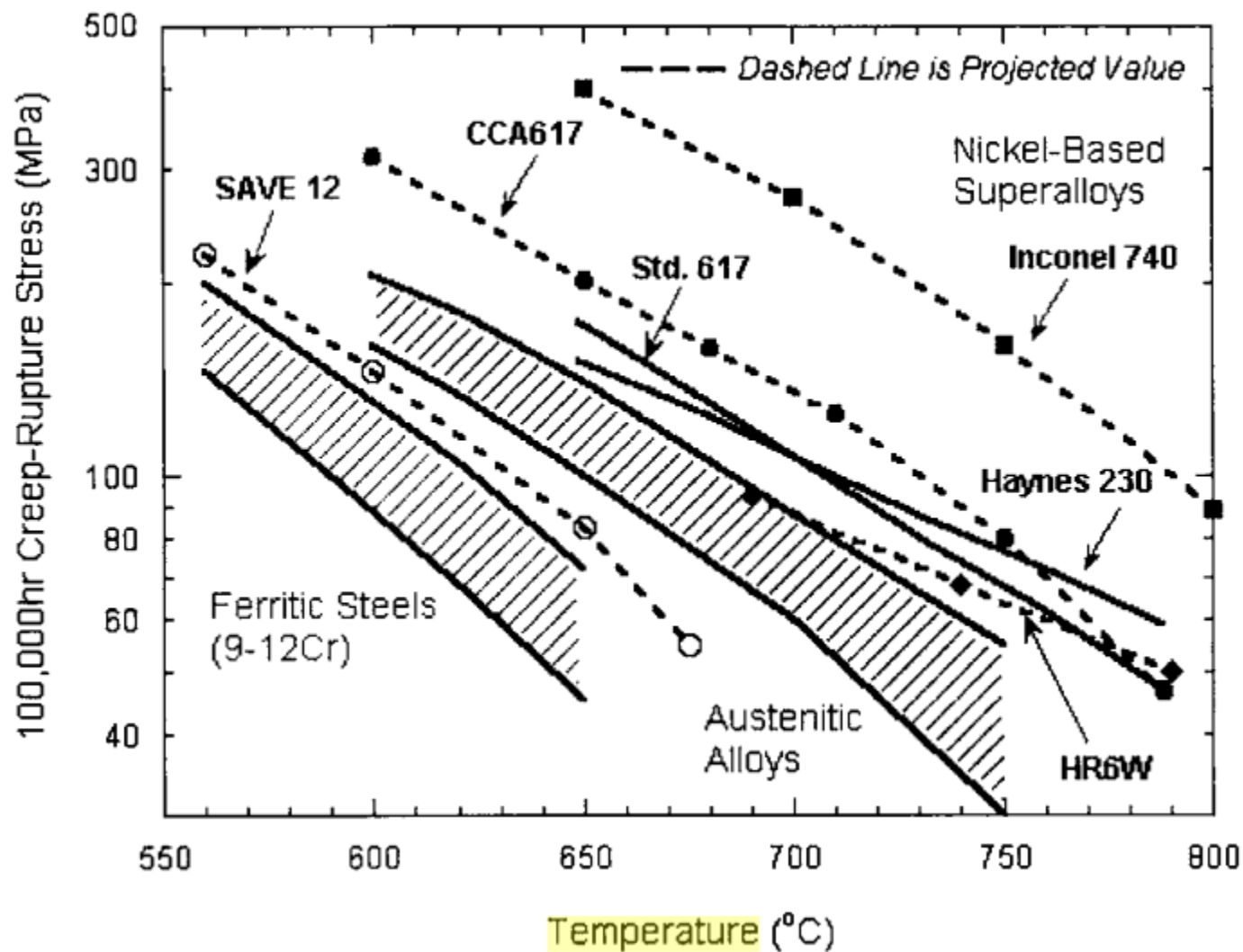
## Increasing Efficiency

Each 1% increase in efficiency eliminates ~1,000,000 tons of CO<sub>2</sub> emissions over the lifetime of an 800-MW plant

US-DOE Advanced Power Systems:  
46%-48% efficiency from coal generation  
Steam condition: 760 C - 35MPa  
~ 5ksi



100,000hr Creep-Rupture for USC Boiler Materials



## ❑ Material requirements for Advanced Ultra-SuperCritical (AUSC) boiler:

- **Low cost** metal
- Compatible thermal properties
- Sufficient high temperature performance
  - Sufficient mechanical strength
  - Creeping resistance
  - Corrosion resistance
- *Low temperature ductility*

## □ Ferritic steel

- BCC matrix with low Ni content (low cost)
- Low temperature brittleness
- Weldability

## □ New design of ferritic steel

- Composition modulation
- Microstructure engineering



# Complexity of the Alloy Strategy

## ❑ Many structural factors:

### ➤ **Matrix**

➤ Precipitation

➤ Grain boundary

➤ Interphase

## ❑ Correlated problem

➤ Doping may solve a problem but bring in more problems

➤ Difficult to assess the effect of alloying

# Known 9-12% Cr Ferritic Steels

**Table 1. Precipitate Phases in Different Steel Phases. PT Represent for Prototype Structure and SG for Space Group Number.**

Precipitate Phase	PT	SG	Steel Phases											
			P91	P92	E911	AXM	HCM12	P122	T122	NF1 2	FN5	TB12	VM12	X20
<b>BCC_A2</b>	W	229	X	x	x	x	x	x	x	x	x	x	x	x
<b>M23C6</b>	Cr23C6	225	X	x	x	x	x	x	x	x	x	x	x	x
<b>LAVES</b>	MgZn2	194	X	x	x			x	x	x	x	x	x	x
<b>Z_PHASE</b>	NaCl	225	X	x	x	x	x	x	x	x	x	x	x	x
<b>NbNi<sub>3</sub></b>	Al3Ti	139	X			x	x	x	x	x	x			
<b>AlN</b>	ZnO	194	X	x	x	x		x	x			x		
<b>SIGMA</b>	CrFe	136		x	x							x		
<b>FCC_A1</b>	Cu	225		x	x	x	x	x	x	x		x	x	x
<b>HCP_A3</b>	Mg	194		x	x							x		
<b>M<sub>2</sub>B<sub>Tetr</sub></b>	Fe2B	140		x		x								
<b>MU_PHASE</b>	W6Fe7	166				x								
<b>M6C</b>	W3Fe3C	227				x								
<b>Cr<sub>2</sub>B<sub>Ortho</sub></b>	Mg2Cu	70							x	x	x	x		x
<b>PI</b>	Mo3Al2C	70										x	x	



# Ferritic Steel Matrix

□ BCC structure

□ Composition of the BCC matrix in 9-12% Cr steels

<b>Name</b>	<b>Fe</b>	<b>Cr</b>	<b>Ni</b>	<b>Mo</b>	<b>Si</b>	<b>Al</b>
P91	0.9898	5.87E-4		8.42E-9	6.64E-3	2.77E-3
E911	0.9969	5.29E-4		1.13E-8	2.03E-3	5.75E-12
P92	0.9944	5.55E-4	6.10E-4	2.30E-8	3.83E-3	6.14E-4
AXM	0.9964	5.45E-4	5.96E-4	1.97E-7	1.31E-3	1.15E-3
HCM12	0.9977	5.36E-4	1.03E-5	1.19E-8	1.72E-3	
P122	0.9986	5.15E-4	6.22E-4	1.08E-11	2.99E-4	4.18E-11

- ❑ Screening ferritic steel design based on properties of the solid solution **matrix**
  - Elastic properties
  - Low temperature ductility
  
- ❑ Develop efficient parallel software for large scale screening calculations
  - first principles quality for solid solution system
  - Automated solid solution structure sampling
  - Automated properties calculations



## Approach: Structure Modeling

- ❑ Dilute multi-component solid solution
  - requires huge atomic structure model
  - components of very low concentration considered as point defect
  
- ❑ Special quasi-random structures

## □ Properties calculations

### ➤ *Supercell Approaches*

➤ *Ensemble Average of Supercells:* 
$$F(\vec{\sigma}, T) \approx \sum_{i \in \vec{\sigma}} w_i(T) F_i(T)$$

*supercells are local snapshots in the infinite solid solution lattice  $\vec{\sigma}$*

### ➤ *Cluster Expansion Methods*

➤ *Weighted average of clusters:* 
$$F(\vec{\sigma}, T) \cong \sum_{\alpha, s} K_{\alpha}^s(T) \Phi_{\alpha}^s$$

*$\alpha, s$  are cluster indices and cluster order indices*

*clusters are local structures in the infinite solid solution lattice  $\vec{\sigma}$*

➤ *Mathematically rigorous*

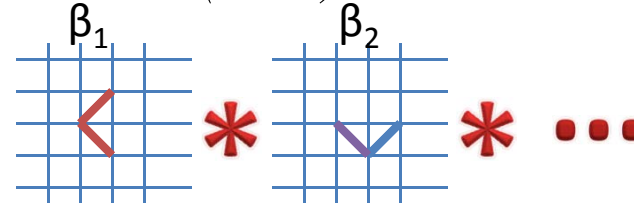
# G(P,T) Module: UnitCell Expansion

Cluster Expansion Method for multi-component multi-sublattice systems:

*P.D. Tepesch, et al PRL 74, 12 (1995)*

$$F(\vec{\sigma}, T) \cong \sum_{\alpha, s} K_{\alpha}^s(T) \Phi_{\alpha}^s,$$

$$\Phi_{\alpha}^s = \prod_i \Phi_{\beta_i}^{s_i}; \alpha = \bigcup_i \beta_i$$



**Challenge:** number of cluster expansion terms  $n$

$$n \sim (N-1)^{|\alpha| N_{\text{sublattice}}}$$

UnitCell Expansion Method for multi-component multi-sublattice systems:

$$F(\vec{\sigma}, T) \cong \sum_{\gamma, s} K_{\gamma}(T) \Phi_{\gamma}^s,$$



**Rationale:** Coarse grained cluster (CGC) expansion,

- Unitcells are treated as pseudo atom types
- Simplify lattice
- Expected must faster cluster interaction decaying over distance (*up to pair*)
- Much larger number of components (pseudo atoms) (*unitcell types*)

# Special Quasirandom Structure

- Poor man's approximation to cluster expansion method

$$F(\vec{\sigma}, T) \cong \sum_{\alpha, s} K_{\alpha}^s(T) \Phi_{\alpha}^s,$$

$$\langle F \rangle_{SQS} \cong \sum_{\alpha, s} K_{\alpha}^s(T) \langle \Phi_{\alpha}^s \rangle_{SQS},$$

$$\langle \Phi_{\alpha}^s \rangle_{SQS} \approx \langle \Phi_{\alpha}^s \rangle$$

## □ At high temperature limit

- site occupation is complete random
- correlation function is known

$$\rho_{\alpha}(\sigma_{HT}) = \prod_{i \in \alpha} \left\langle \gamma_{\alpha_i, M_i}(\sigma_i) \right\rangle_{\alpha}$$

- match SQS correlation with the known correlation function
  - ✓ Exhaustive search
  - ✓ Genetic algorithm
  - ✓ Other global optimization approach may also be used

## ***B. Application to 9-12Cr Ferritic Steels***

### **□ B.1 Properties of known 9-12Cr ferritic steel**

- Positive control using well characterized 9-12Cr ferritic steels
  - P91, E911, P92, AXM, HCM12, P122, T122, NF12, FN5, TB12, VM12 and X20
  - Formation energy and Elastic constants will be assessed initially.
  - Assess ductility using the ratio of bulk modulus and shear modulus.
  - Stacking fault energy and surface cleavage energy will be carried out to estimate the Rice-Thomson parameter which is widely used as ductility criterion.
  - Trend analysis of indicative parameter of ductility.



# Challenges In Structure Modeling

## ❑ Incomplete structure information about the phases in the steel

- Missing information about site distribution
  - Phase compositions are known
  - Multiple non-equivalent solid solution sites

## ❑ Composition requires exceedingly large model

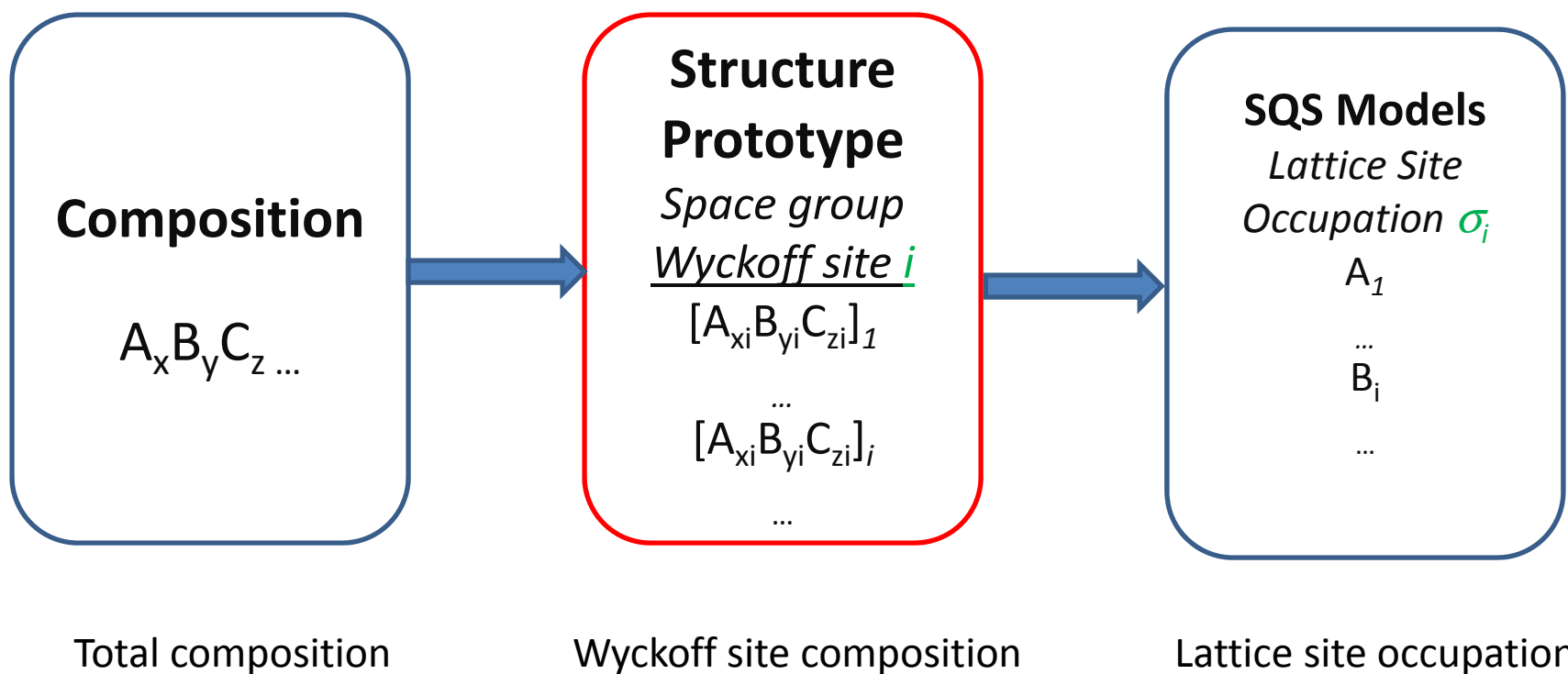
- Dopant concentration between 1000ppm to 1ppm
  - Need to assess the dopant-dopant interaction
  - Model requires > 1000 atoms
- Dilute dopant can be treated as point defect
- Using the scaling law to estimate the effect of dopant with intermediate concentration:  $G \sim c^\alpha$



# AXM Steel Facts

<u>Phase</u>	<u>Vol fract</u>	<u>Composition</u>	<u>Crystal</u>	<u>Microstructure</u>
BCC-A2#2	0.8464	$\text{Fe}_{0.996}\text{Si}_{0.002}\text{Al}_{0.001}$	cI2	Matrix phase
BCC-A2#1	0.1006	$\text{Cr}_{0.957}\text{Mn}_{0.043}$	cI2	Precipitation
$\text{M}_{23}\text{C}_6$	0.0203	$(\text{Cr}_{0.864}\text{Mn}_{0.130}\text{Fe}_{0.006})_{23}\text{C}_6$	cF116	Precipitation
$\mu$ -Phase	0.0112	$(\text{Fe}_{0.992}\text{Cr}_{0.008})_7(\text{W}_{0.650}\text{Mo}_{0.350})_6$	hR39	Precipitation
FCC-A1#1	0.0100	$\text{Ni}_{0.584}\text{Fe}_{0.370}\text{Si}_{0.046}$	cF4	Precipitation
$\text{M}_6\text{C}$	0.0037	$(\text{Mo}_{0.992}\text{W}_{0.008})\text{MoFe}_2\text{C}$	cF112	Precipitation
Z-Phase	0.0051	$(\text{Cr}_{0.898}\text{Fe}_{0.102})\text{VN}_{0.669}$	tP6	Precipitation
$\text{NbNi}_3$	0.0010	$\text{Ni}_3\text{Nb}$	oP8	Precipitation
AlN	0.0012	AlN	hP4	Precipitation
FCC-A1#3	0.0003	$\text{Cu}_{0.999}\text{Ni}_{0.001}$	cF4	Precipitation
$\text{M}_2\text{B}$	0.0003	$(\text{Mo}_{0.953}\text{Cr}_{0.047})_2\text{B}$	tI12	Precipitation

# Structure Modeling



## ❑ Structure models generation

- Based on structure prototype
  - Limited to size < 250 atoms
  - Site-distribution based on prior knowledge

## ❑ Composition requires exceedingly large model

- Dopant concentration between 1000ppm to 1ppm
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# Elastic Constants Calculations

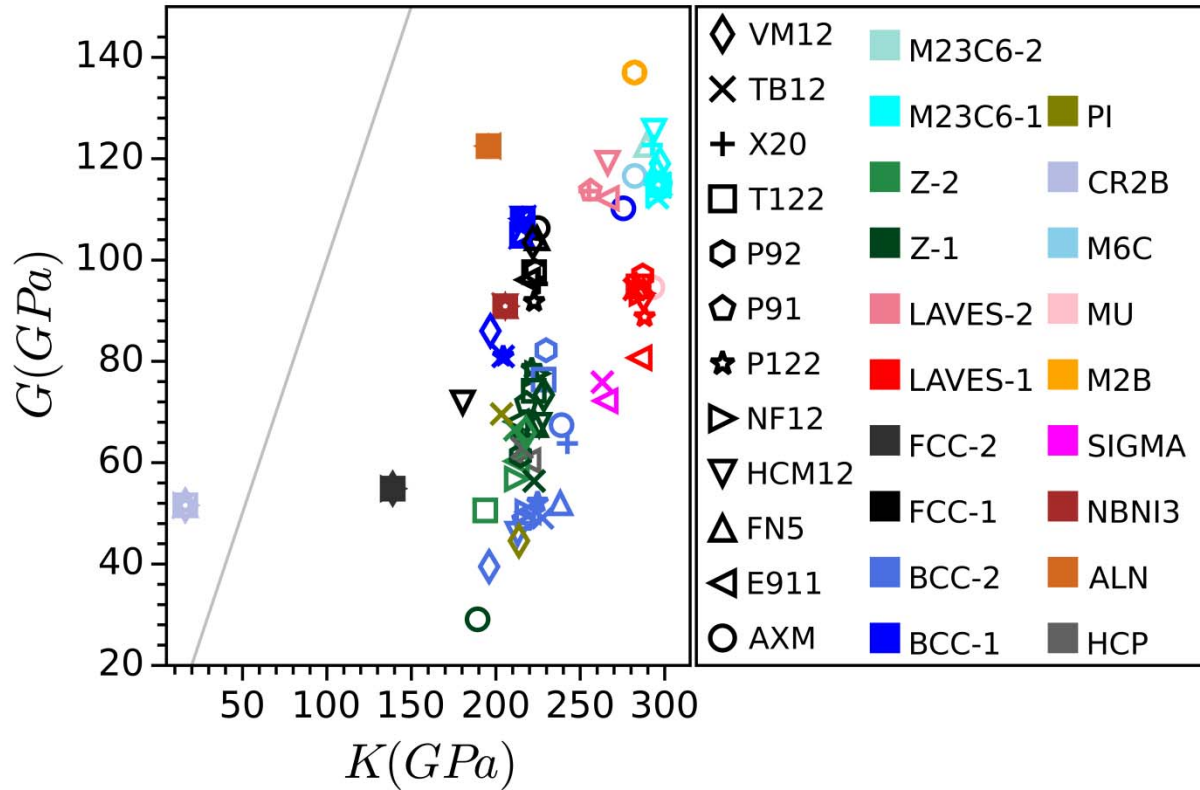
- ❑ Calculated use the in-home developed  $G(p,T)$  package
  - Employed VASP as the computing engine
  - Automate the calculation and fully taking advantages of symmetry
  - Both stress and energy based calculations are available
  - Accuracy setting:
    - Standard 400eV energy cutoff
    - Standard K-point sampling: metal (cutoff 35), others (cutoff 25)
    - Energy convergence  $10^{-6}$  eV
    - Spin polarized calculation for selected phases
  - More than 100 SQS models have been calculated. Many involves more than 4 elements are for the first time been calculated.

# Elastic Constants Calculations: AXM

Phases	$C_{11}, C_{22}, C_{33}$	$C_{44}, C_{55}, C_{66}$	$C_{12}, C_{13}, C_{23}$	K	G	E	$\nu$	G/K
BCC-A2#1	396	126	215	275	110	292	0.323	0.400
BCC-A2#2	395	53	168	242	72	196	0.365	0.297
AlN	377 356	113 125	129 99	196	122	304	0.241	0.622
FCC-A1#1	322	147	179	225	106	275	0.296	0.473
Cu	181	83	121	140	56	147	0.324	0.399
$M_{23}C_6$	459	111	216	297	115	306	0.328	0.388
$M_2B$	440 504	141 136	199 190	282	137	353	0.291	0.486
$M_6C$	442	115	203	282	117	308	0.318	0.413
$\mu$ -phase	442 426 406	92 94 94	245 225 217	293	95	256	0.354	0.323
NbNi <sub>3</sub>	290 305	113 111	178 153	206	91	238	0.307	0.442
Zphase	278 250	45 8	180 167	189	29	83	0.427	0.154

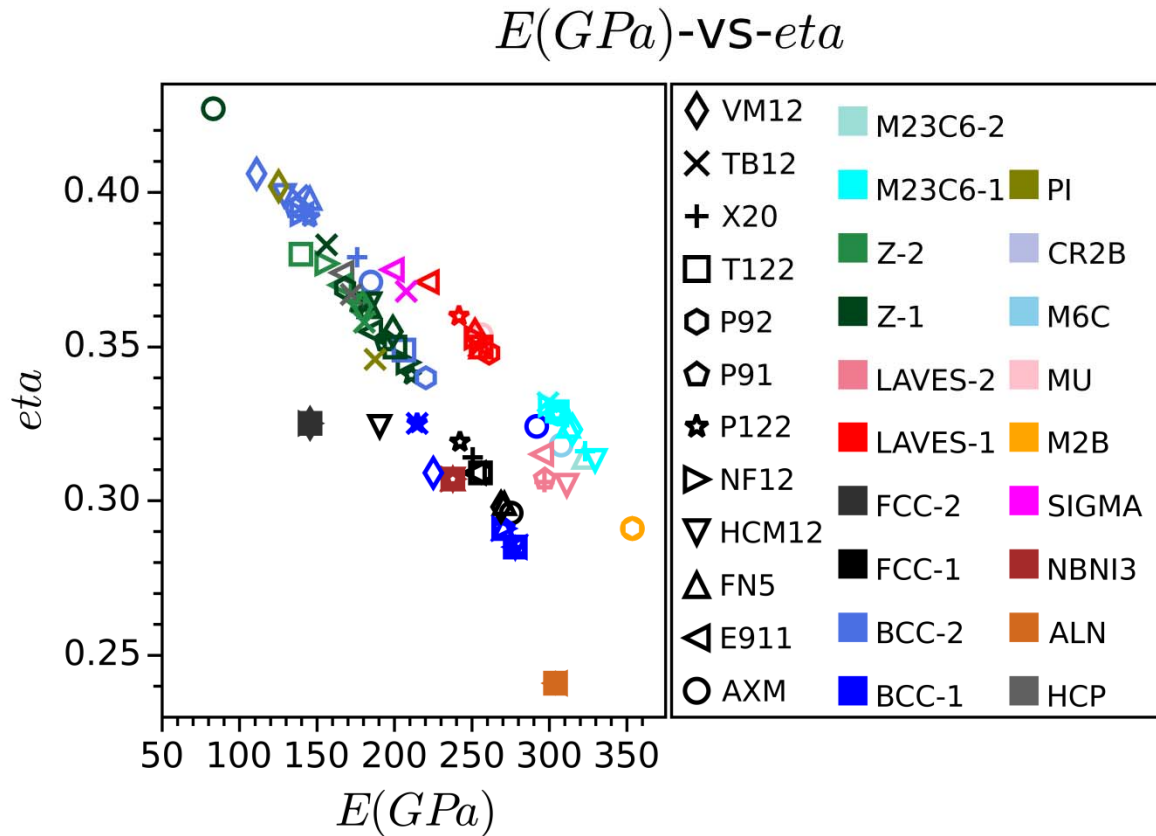
# Elastic Properties: Known 9-12 Cr Steel

$K(GPa)$ -vs- $G(GPa)$



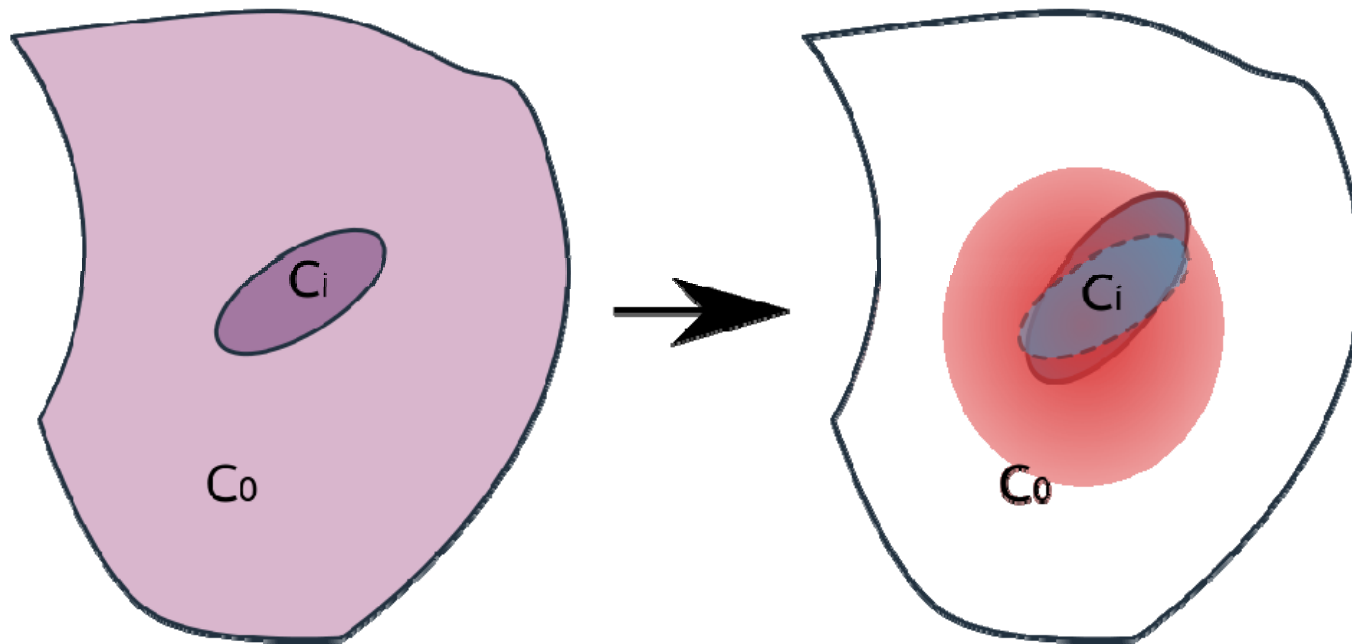


# Elastic Properties: Known 9-12 Cr Steel



# Precipitation Effects

- ❑ Homogenization scheme to assess the precipitation effects on elastic constants
  - Eshelby's inclusion theory:
    - ❖ uniform stress/strain field inside the inclusion



# Effective Self Consistent Scheme

- ❑ Iterative scheme
- ❑ Multiple inclusion phases allowed
- ❑ Only volume fraction and bulk elastic constants used in the scheme \*

\* Precipitation size and shape information described by Eshelby tensor. Assume isotropic spherical inclusion for calculating Eshelby tensor  $S$

$$C^* = (H + C_M^{-1})^{-1}$$

$$H = \text{sum} (H_{l,i}^d (I - \Omega_{DI,i} H)^{-1})$$

$$H_{l,i}^d = c_i \{ (C_{l,i}^{-1} - C_M^{-1})^{-1} + C_M (I - S_{l,i}^M) \}^{-1}$$

$$\Omega_{DI,i} = C^* (I - S_{l,i}^*)$$

# Elastic properties of steel

- Homogenized elastic modulus (GPa)

	K	G	Y	$\eta$
AXM	271	102	272	0.333
P92	251	84	228	0.349
T122	248	77	209	0.359

\* Other steels have unstable precipitation phases are shown in the table.

## *B. Application to 9-12Cr Ferritic Steels*

### □ B.2 Screening studies of Ferritic Steels

- Screening in a progressive manner with 4 components BCC solid solutions examined first.
- Precipitation effects to be assessed through homogenization
- Global optimization methods such as simulated annealing and genetic algorithm to locate the optimal ferritic design.



# Search For Optimal Ferritic Design

## □ From composition to phase distribution

- Concentration dependent chemical potential in phases estimated from computed and measured properties of known steel phases
- Energy minimization process to compute the phase distribution

## □ Homogenization to evaluate the overall mechanical properties

- Mechanical properties of solid solution estimated using empirical laws based on computed and measured properties for given composition.



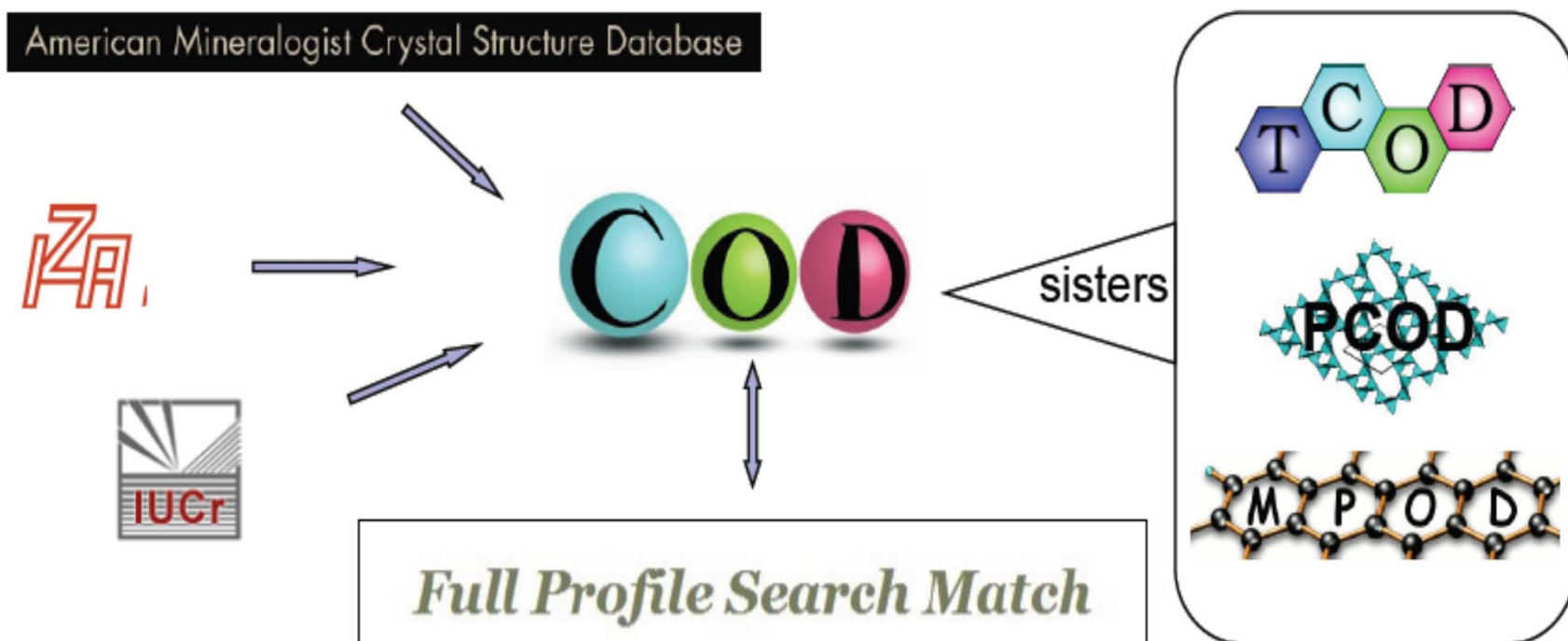
# Inverse: Properties → Structure

- ❑ First principles method brings chemical accuracy for properties calculation with known structure
- ❑ The inverse process from properties to predict structure remains the greatest challenge to material science
- ❑ Two-step approach/Material genome approach
  - Properties -> Composition -> prototype library



# HCOD: A High Performance Database

- **Crystallography Open Database (COD)** is an **open-access** database for crystal structures.
- collects the information of **all small to medium sized** unit cell crystallographic structures, including **organic, inorganic, metal-organic compounds and minerals**.

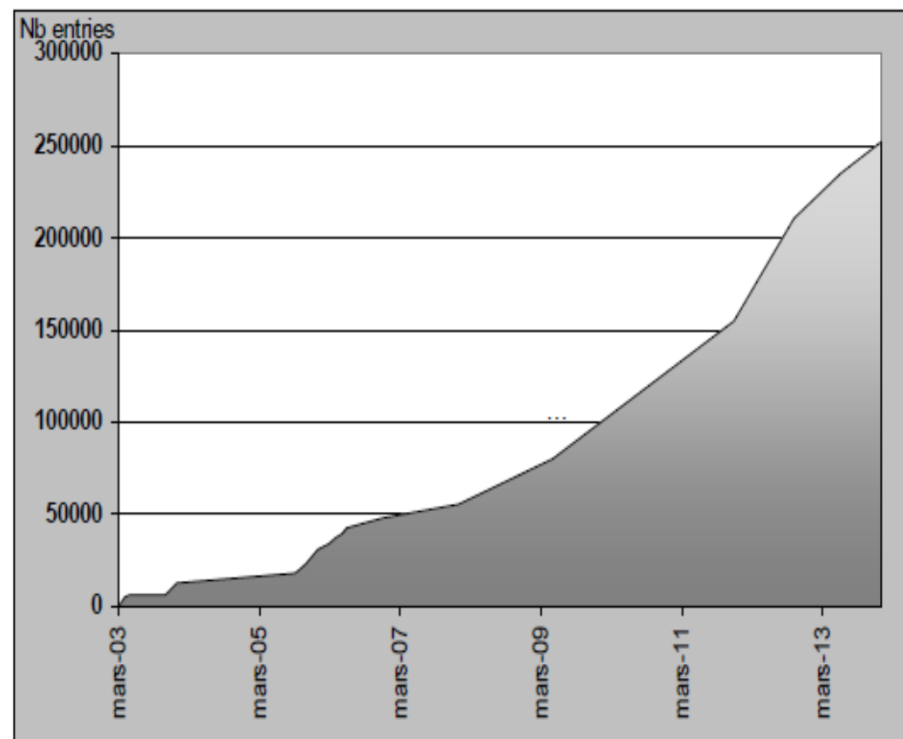




# HCOD: A High Performance Database

- All **registered users** can deposit published and unpublished structures into COD database.
- **COD can be extended by large number of users simultaneously**, which greatly increases the growth rate of COD.
- COD stores data in a uniform format: **Crystallographic Information File (CIF)**, one structure per file.

As Feb 2016, there are more than 350,000 entries in COD





# HCOD: A High Performance Database

## **Research Goal:**

- ❖ Build a high performance COD (H-COD) database with efficient query system on distributed computer cluster

## **Research Objectives:**

- ❖ Design a well-organized structure for H-COD database.
- ❖ Design efficient query operations including search, updating, insertion and deletion.
- ❖ Implement the database in a distributed and parallel computing system;
- ❖ Develop Web APIs that provide user-friendly query interfaces to the database.



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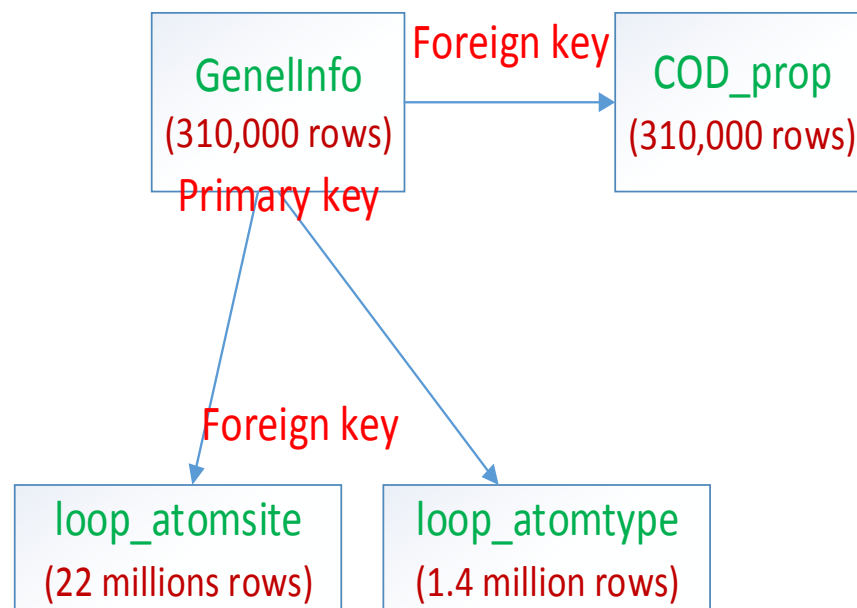
# HCOD: A High Performance Database

## Table design

### Four tables

- ❖ First three tables are GenellInfo, Atom-site and Atom-type, where the information come from the CIFS in COD.
- ❖ The fourth table: COD\_prop contains new attributes and values generated by the LatMGA method.

To maintain referential integrity of data, we use foreign key constraint: COD number is chosen as primary key in GenellInfo table and foreign key in loop tables.



## HCOD: Web Query Interface

### Search COD CIF List by Fields

Year of Journal	<input type="text" value="2005"/>
Journal Name	<input type="text"/>
Journal Issue	<input type="text"/>
Journal Volume	<input type="text"/>
Journal Paper DOI	<input type="text"/>
Elements	Al <input type="checkbox"/> S <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/> Only
Number of distinct elements	Min: <input type="text" value="2"/> Max: <input type="text" value="6"/>
Crystal type	<input type="text"/>
Composition	<input type="text"/>
Hermann-Mauguin symmetry space group	<input type="text" value="P 1 21/n 1"/>
Space group id	<input type="text"/>
Cell length A	Min: <input type="text"/> Max: <input type="text"/>
Cell length B	Min: <input type="text"/> Max: <input type="text"/>
Cell length C	Min: <input type="text"/> Max: <input type="text"/>
Cell angle Alpha	Min: <input type="text"/> Max: <input type="text"/>
Cell angle Beta	Min: <input type="text"/> Max: <input type="text"/>
Cell angle Gamma	Min: <input type="text"/> Max: <input type="text"/>
Unit Z	Min: <input type="text"/> Max: <input type="text"/>
Wyck sites	Min: <input type="text"/> Max: <input type="text"/>
SCC NA	<input type="text"/>
SCC NB	<input type="text"/>
SCC NC	<input type="text"/>
SCC OCC	<input type="text"/>
IS ORGANIC	<input type="text"/>
	<input type="button" value="Search"/>

LatMGA indices

## ❑ Ordered lattice structures:

- Crystal and Solid Solution
- Common description:  $\{ \mathbf{L}_i \} \otimes \{ \mathbf{r}_j; \boldsymbol{\sigma}_j \}$   
where  $\{ \mathbf{L}_i \}$  is the set of lattice symmetry operators  
 $\{ \mathbf{r}_j \}$  is the set of lattice basis  
 $\{ \boldsymbol{\sigma}_j \}$  is the set of composition vector

## ❑ Composition vector $\boldsymbol{\sigma}$

- $\boldsymbol{\sigma} = \sum_i \eta_i \boldsymbol{\varepsilon}_i$
- Each vector basis  $\boldsymbol{\varepsilon}_i$  represents an element or a structure unit
- The component  $\eta_i$  represents the probability of the basis at the site
- Vacancy is also a basis

## ❑ Material Genome Approach

- The challenge is how to **traverse** the enormous configuration space
- Uniform structure indices are highly desired for data mining

## ❑ **LatMGA**: separate lattice from composition

- Structure =  $\{ L_i \} \otimes \{ r_j; \sigma_j \} = [\{ L_i \} \otimes \{ r_j \}] \oplus [\{ L_i \} \otimes \{ \sigma_j \}]$
- Structure is indexed by lattice prototype and composition type
- Observation: **any lattice basis sets is a subset of a fine grid insider the unit cell**. For any stable structure at room temperature, **the grid needs not to be finer than the range of atomic vibration**. Therefore, any lattice may be a subset of supercell of a simple lattice such as simple cubic and hexagonal.

## □ LatMGA:

### ➤ A systematic approach to index structure prototype

- ❖ { # lattice prototype
- ❖ { lattice unit type<fcc,hcp, etc.>,  
supercell <n<sub>x</sub>n<sub>x</sub>n<sub>x</sub>>,  
space group }
- ❖ # composition space
- ❖ { mask vector,  
composition vectors }
- ❖ }

### ➤ Three stage material configuration space exploration

#### { lattice prototype discovery:

traverse the structure prototype indices; }

#### { composition space discovery:

rules based selection of mask/composition vectors;

combine with lattice prototype to produce structure sample;

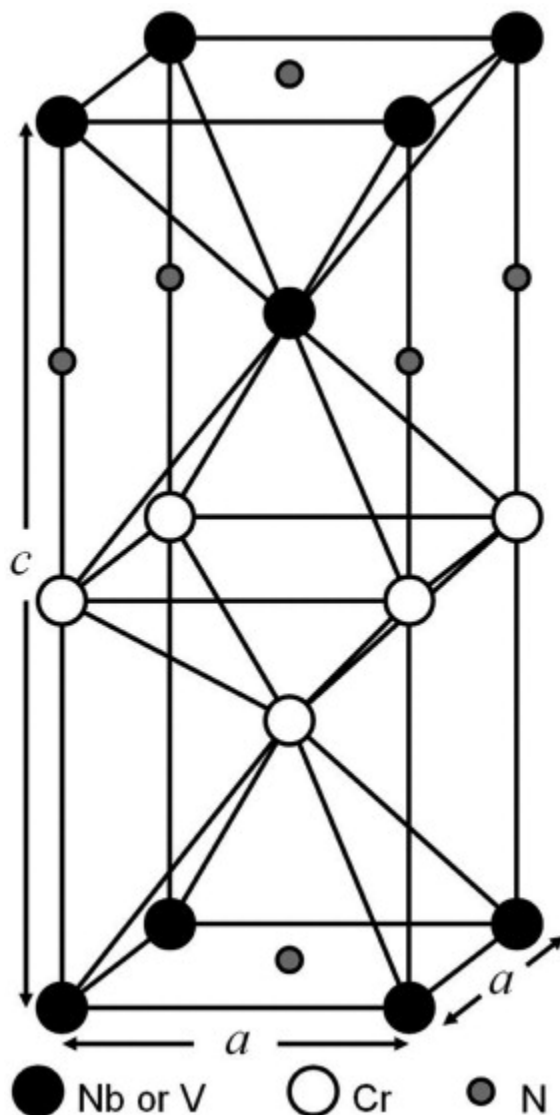
structure sample can be evaluated using first principles methods; }

#### { material genome approach:

big data analysis on the high dimension structure indices space;

inverse map from properties to structure; }





Z-phase indices:

Lattice prototype:

space group: 129 (P4/nmm)

irreducible sites:

Site\_1 2 c 1/4 1/4 7/8

Site\_2 2 c 1/4 1/4 5/8

Site\_3 2 c 1/4 1/4 1/8

\*\* it is a subset of 2x2x8 **supercell** of  
1 basis simple cubic lattice **casted**  
into space group 129

Composition:

$\epsilon_1 = \text{Nb}$ ,  $\epsilon_2 = \text{V}$   $\epsilon_3 = \text{Cr}$   $\epsilon_4 = \text{N}$   $\epsilon_5 = \text{Vac}$

Site\_1 (0.5 0.5 0 0 0)

Site\_2 (0 0 1 0 0)

Site\_3 (0 0 0 1 0)

### casted from scc-2-2-8 to 129 :: size= 2 2 8 ###

space\_group 129

origin 2

Aa1	0.75000	0.25000	0.00000	#	2 a Aa
Ab1	0.75000	0.25000	0.87500	#	4 f Ab
Ac1	0.75000	0.25000	0.75000	#	4 f Ac
Ad1	0.75000	0.25000	0.62500	#	4 f Ad
Ae1	0.75000	0.25000	0.50000	#	2 b Ae
Af1	0.25000	0.25000	0.00000	#	2 c Af
<b>Ag1</b>	<b>0.25000</b>	<b>0.25000</b>	<b>0.12500</b>	#	<b>2 c Ag</b>
Ah1	0.25000	0.25000	0.25000	#	2 c Ah
Ai1	0.25000	0.25000	0.37500	#	2 c Ai
Aj1	0.25000	0.25000	0.50000	#	2 c Aj
<b>Ak1</b>	<b>0.25000</b>	<b>0.25000</b>	<b>0.62500</b>	#	<b>2 c Ak</b>
Al1	0.25000	0.25000	0.75000	#	2 c Al
<b>Am1</b>	<b>0.25000</b>	<b>0.25000</b>	<b>0.87500</b>	#	<b>2 c Am</b>



# Continue: LatMGA

## Progress:

- Tested against all cubic phases found in the [Crystallography Open Database](#)
- Excluding wrongful data, all can be indexed using supercell of simple cubic casted into the specific space group and a mask to indicate the closely matched Wyckoff sites (for example, Ag1, Ak1, Am1 sites, a mask vector [ 0 0 0 0 0 0 1 0 0 0 1 0 1])
- We are now in the process of implementing programs to search for unexplored masks by combining with basis information of atoms such as atomic size, charge, etc.



# Continue: LatMGA

## Progress:

- ❑ All cubic phases with space group 225 (total 689 valid structures)
  - 304 mapped to SCC-2-2-2
  - 229 mapped to SCC-4-4-4
  - 10 mapped to SCC-6-6-6
  - 133 mapped to SCC-8-8-8
  - 13 mapped to SCC-12-12-12



# Conclusions and Discussions

- ❑ Mechanical properties of all phases found in the 9-12% Cr ferritic steels computed; several phases were found unstable using the SQS models.
- ❑ Homogenization method developed to evaluate overall mechanical properties. Search for optimal composition/phase distribution/volume fraction is in progress.
- ❑ Development of the LatMGA method for:
  - Prototype library generation based on composition
  - Automate structure model generation based on prototype library
  - Automate the properties calculation of structure models
  - Data mining to map properties to composition
- ❑ Developed a high performance distributed database system for data mining of crystal structure information.