Understanding Information Mediation Issues in Multiscale Design

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Multiscale Design of Materials Simulation, Modeling, & Decision Science Increasing energy use Increasing impact on the environment Increasing resource scarcity



Energy and environmental challenges





Why create models?





Design across scales

- models
- simulations
- databases
- sensors

. . .

"models"



Information at multiple scales

What's needed

Information

- 1. Integration
- 2. Mediation
- 3. Interaction



Actionable information

What's needed

Information

- 1. Integration
- 2. Mediation
- 3. Interaction



Actionable information

- the development of the needed models
- the integration of these models to form federated model sets
- the establishment of a unified design environment based on the integrated model sets



Developing a new architecture

 organize interconnected models to optimize solution







Organization of solutions

Constituency

the capability of models to come together in groups that have coherence and substitutability

Articulation

a simple and precise mechanism for describing how the models are chosen, linked, executed, and results reported

Convergence

a knowledge of the topological mapping of the federation and the capability to route and converge information through the federation to complete the assigned tasks



Federated model set requirements

- enable models to couple together "on-the-fly" without intervention
- models must "know" whether they can link and what information that they require and deliver (identifiers)
- must be able to ensure that the information has the right units, attributes, ...
- must be able to identify the boundaries that models need with other models

model to model communication









Create a hybrid system (a "testbed") to examine key aspects of information mediation for linked (concurrent) multiscale simulations

- information transfer between models
- boundaries between models
- convergence of the solution
- stability



- upper velocity is set as boundary condition
- examine atomistic-level effects of fluid/surface interactions (bottom boundary) on fluid flow



http://en.wikipedia.org/wiki/File:Laminar_shear.svg



Test problem: Couette flow

- Fluid flow simulations
 - Lattice Boltzmann method
 - lattice-based solution to Navier-Stokes equation
 - very useful for situations with complex boundary conditions
- Atomistic-level simulations
 - molecular dynamics



- single-particle distribution functions ($f_i(\vec{r},t)$) move along lattice sites
- dynamics

$$f_{i}\left(\vec{r}+\vec{v}_{i}\Delta t,t+\Delta t\right)=f_{i}\left(\vec{r},t\right)+\frac{\Delta t}{\tau}\left(f_{i}^{eq}\left(\vec{r},t\right)-f_{i}\left(\vec{r},t\right)\right)$$



 "collisions" lead to equilibrium distribution

$$f_{i}^{eq}(\vec{r},t) = W_{i}\rho \left(1 + \frac{\vec{v}_{i}\cdot\vec{u}}{c_{s}^{2}} + \frac{(\vec{v}_{i}\cdot\vec{u})^{2}}{2c_{s}^{4}} - \frac{u^{2}}{2c_{s}^{2}}\right)$$

measurable quantities:

$$\rho = \sum_{i} f_{i}, \quad \rho \vec{u} = \sum_{i} \vec{v}_{i} f_{i}$$



Chen and Doolen, Annu. Rev. Fluid Mech. 30, 329 (1998)



Lattice Boltzmann method

Force on atoms:

$$\vec{F}_{k} = -\nabla_{k} U(\vec{r}_{1}, \vec{r}_{2}, \dots, \vec{r}_{N}) = -\nabla_{k} \sum_{j>i=1}^{N} \phi_{ij}(r_{ij})$$
$$\phi_{ij}(r_{ij}) = 4\varepsilon_{ij} \left(\left(\sigma_{ij}/r_{ij}\right)^{12} - \left(\sigma_{ij}/r_{ij}\right)^{6} \right)$$

Solve Newton's equations:

$$m_{k} \frac{\partial^{2} \vec{r}_{k}}{\partial t^{2}} = \vec{F}_{k} \left(\vec{r}_{1}, \vec{r}_{2}, \dots, \vec{r}_{N} \right)$$
$$\vec{r}_{k} \left(t + \Delta t \right) = \vec{r}_{k} \left(t \right) + f \left(\vec{F}_{k} \left(t \right), \Delta t \right)$$



Discrete time steps: Δt ~10⁻¹⁵ -10⁻¹⁴ seconds

e.g., LeSar, Introduction to Computational Materials Science (Cambridge, 2013)



Molecular dynamics

- Lattice Boltzmann solved on the 3D grid (one column shown)
 - upper velocity set as a boundary condition
 (u = 1)
 - LB yields the velocity at top of MD cell
- Molecular dynamics solved in bottom grid volume
 - determines the velocity at fluid/solid interface
 - that velocity sets lower boundary condition for LB
- Iterate until converged solution





Boundary between LB/MD

- Varying strength of solid/fluid interaction (potential parameters)
- Effect of the roughness of the surface on the fluid flow
- Extend the LB/MD method to larger scales using standard multigrid methods.





e.g., Asproulis et al., Advances Engin. Software 46, 85–92 (2012)





- Our current focus is on understanding the boundary between the methods
 - convergence
 - stability
- Examining different methods of coupling
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 - gradient



iteration cycle

fluid-solid interaction 0.75 of fluid-fluid interactions





- create independent models
- develop language for model-model communication
 - compatibility of information
 - boundaries
 - convergence
 - stability
- "snap" models together
 - substitute different models

mediation



Path forward



Körner et al, J. Mater. Processing Tech. 211, 978–987 (2011)



Additive manufacturing design tool

- "Accurate" simulation and modeling of real systems
- Interactive decision tools
- Realtime communication and decision making
- Easily understood graphical interface



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